

Chapter 2

# *Languages and Grammars*

- Grammars
- Regular expressions
- Finite state machines

*Techniques for describing a language's syntax*

- $N$ , a nonterminal alphabet
- $T$ , a terminal alphabet
- $P$ , a set of rules of production
- $S$ , the start symbol, an element of  $N$

*The four parts of a grammar*

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$N = \{\text{Identifier, Letter, Digit}\}$   
 $T = \{\text{a, b, c, 1, 2, 3}\}$   
 $P =$  the productions

1. Identifier  $\rightarrow$  Letter
2. Identifier  $\rightarrow$  Identifier Letter
3. Identifier  $\rightarrow$  Identifier Digit
4. Letter  $\rightarrow$  a
5. Letter  $\rightarrow$  b
6. Letter  $\rightarrow$  c
7. Digit  $\rightarrow$  1
8. Digit  $\rightarrow$  2
9. Digit  $\rightarrow$  3

$S = \text{Identifier}$

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**Figure 2.1**  
Grammar A for Component  
Pascal identifiers.

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$N = \{I, F, M\}$   
 $T = \{+, -, d\}$   
 $P =$  the productions

1.  $I \rightarrow FM$
2.  $F \rightarrow +$
3.  $F \rightarrow -$
4.  $F \rightarrow \epsilon$
5.  $M \rightarrow dM$
6.  $M \rightarrow d$

$S = I$

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**Figure 2.2**  
Grammar B for signed  
integers.

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$N = \{A, B, C\}$   
 $T = \{a, b, c\}$   
 $P =$  the productions

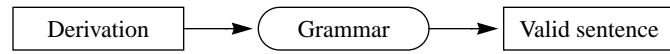
1.  $A \rightarrow a A B C$
2.  $A \rightarrow a b C$
3.  $C B \rightarrow B C$
4.  $b B \rightarrow b b$
5.  $b C \rightarrow b c$
6.  $c C \rightarrow c c$

$S = A$

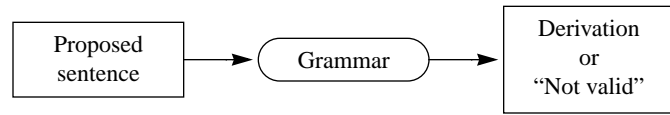
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**Figure 2.3**

Grammar C, a context sensitive grammar.



(a) Deriving a valid sentence.



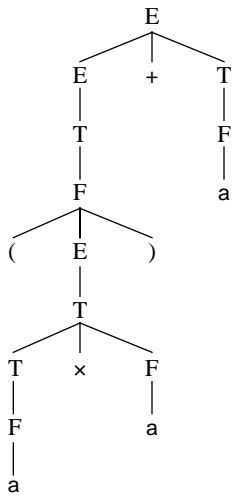
(b) The parsing problem.

**Figure 2.4**

The difference between deriving an arbitrary sentence and parsing a proposed sentence.

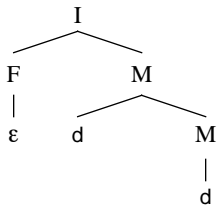
$N = \{E, T, F\}$   
 $T = \{+, \times, (, ), a\}$   
 $P =$  the productions  
     1.  $E \rightarrow E + T$   
     2.  $E \rightarrow T$   
     3.  $T \rightarrow T \times F$   
     4.  $T \rightarrow F$   
     5.  $F \rightarrow ( E )$   
     6.  $F \rightarrow a$   
 $S = E$

**Figure 2.5**  
Grammar D, a grammar for algebraic expressions.



**Figure 2.6**  
The syntax tree for the parse of  $(a \times a) + a$  in Grammar D.

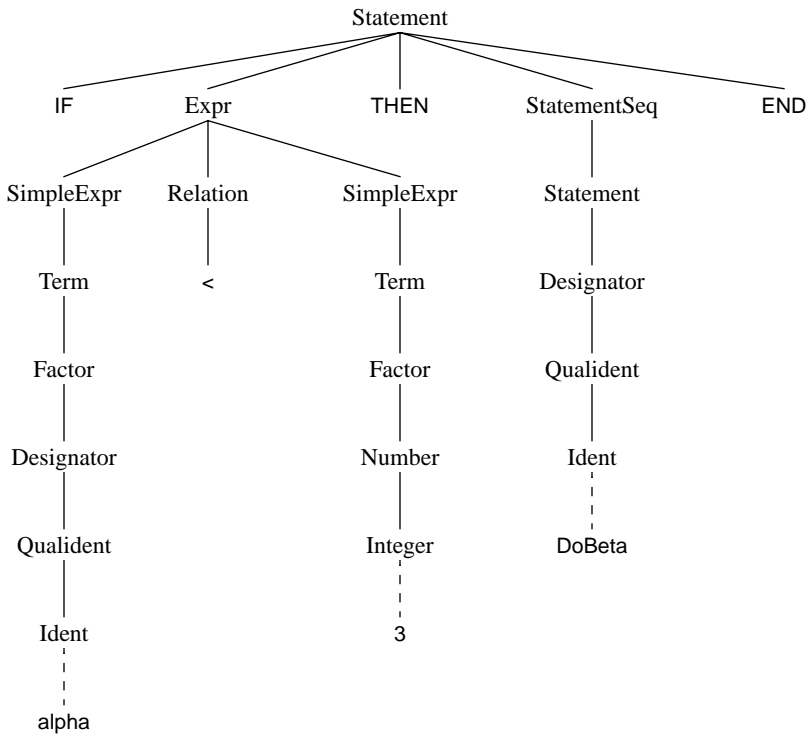


**Figure 2.7**

The syntax tree for the parse of `dd` in Grammar B.

- Alternation—select one of several alternatives
- Optional—include zero or one time
- Repetition—include zero or more times

*The three operations of EBNF*



**Figure 2.8**  
The syntax tree for the derivation in Example 2.13.