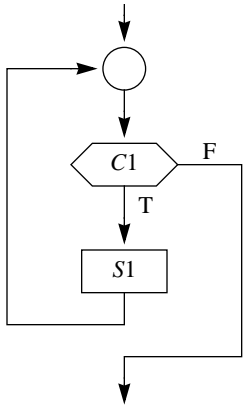


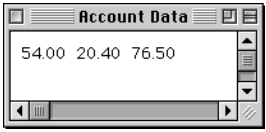
Chapter *10*

Loops

**Figure 10.1**

The flowchart for the WHILE statement.

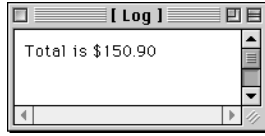
```
WHILE C1 DO  
  S1  
END
```



(a) The input window.



(b) The menu selection



(c) The output to the Log.

Figure 10.2

The input and output of the program in Listing 10.3.

```
MODULE Pbox10A;
  IMPORT TextModels, TextControllers, PboxMappers, PboxStrings, StdLog;

  PROCEDURE ComputeTotal*;
    VAR
      md: TextModels.Model;
      cn: TextControllers.Controller;
      sc: PboxMappers.Scanner;
      balance: REAL;
      sum: REAL;
      sumString: ARRAY 16 OF CHAR;
```

Figure 10.3

A program to find the total of all the data values in the focus window. It uses the eot technique.

```
BEGIN
  cn := TextControllers.Focus();
  IF cn # NIL THEN
    md := cn.text;
    sc.ConnectTo(md);
    sum := 0.0;
    sc.ScanReal(balance);
    WHILE ~sc.eot DO
      sum := sum + balance;
      sc.ScanReal(balance)
    END;
    PboxStrings.RealToString(sum, 1, 2, sumString);
    StdLog.String("Total is $");
    StdLog.String(sumString); StdLog.Ln
  END
END ComputeTotal;
```

```
END Pbox10A.
```

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	0			
IF cn # NIL THEN	0			
md := cn.text;	0			
sc.ConnectTo(md);	0			
sum := 0.0;	0			
sc.ScanReal(balance);	0			
WHILE ~sc.eot DO	0			
sum := sum + balance;	0			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	0			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
■ cn := TextControllers.Focus();	1			
IF cn # NIL THEN	0			
md := cn.text;	0			
sc.ConnectTo(md);	0			
sum := 0.0;	0			
sc.ScanReal(balance);	0			
WHILE ~sc.eot DO	0			
sum := sum + balance;	0			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	1			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1			
■ IF cn # NIL THEN	1			
md := cn.text;	0			
sc.ConnectTo(md);	0			
sum := 0.0;	0			
sc.ScanReal(balance);	0			
WHILE ~sc.eot DO	0			
sum := sum + balance;	0			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	2			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1			
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	0			
sum := 0.0;	0			
sc.ScanReal(balance);	0			
WHILE ~sc.eot DO	0			
sum := sum + balance;	0			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	3			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1			
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	0			
sc.ScanReal(balance);	0			
WHILE ~sc.eot DO	0			
sum := sum + balance;	0			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	4			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	0.0		
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	0			
WHILE ~sc.eot DO	0			
sum := sum + balance;	0			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	5			
-------	---	--	--	--

		sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	0.0	54.0	false	
IF cn # NIL THEN	1				
md := cn.text;	1				
sc.ConnectTo(md);	1				
sum := 0.0;	1				
sc.ScanReal(balance);	1				
WHILE ~sc.eot DO	0				
sum := sum + balance;	0				
sc.ScanReal(balance)	0				
END;					
PboxStrings.RealToString(sum, 1, 2, sumString);	0				
StdLog.String("Total is \$");	0				
StdLog.String(sumString); StdLog.Ln	0				
END					

Total	6				
-------	---	--	--	--	--

		sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	0.0	54.0	false	
IF cn # NIL THEN	1				
md := cn.text;	1				
sc.ConnectTo(md);	1				
sum := 0.0;	1				
sc.ScanReal(balance);	1				
WHILE ~sc.eot DO	1				
sum := sum + balance;	0				
sc.ScanReal(balance)	0				
END;					
PboxStrings.RealToString(sum, 1, 2, sumString);	0				
StdLog.String("Total is \$");	0				
StdLog.String(sumString); StdLog.Ln	0				
END					

Total	7				
-------	---	--	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	54.0	54.0	false
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	1			
sum := sum + balance;	1			
sc.ScanReal(balance)	0			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	8			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	54.0	20.4	false
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	1			
sum := sum + balance;	1			
sc.ScanReal(balance)	1			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	9			
-------	---	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	54.0	20.4	false
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	2			
sum := sum + balance;	1			
sc.ScanReal(balance)	1			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	10			
-------	----	--	--	--

		sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	74.4	20.4	false	
IF cn # NIL THEN	1				
md := cn.text;	1				
sc.ConnectTo(md);	1				
sum := 0.0;	1				
sc.ScanReal(balance);	1				
WHILE ~sc.eot DO	2				
sum := sum + balance;	2				
sc.ScanReal(balance)	1				
END;					
PboxStrings.RealToString(sum, 1, 2, sumString);	0				
StdLog.String("Total is \$");	0				
StdLog.String(sumString); StdLog.Ln	0				
END					

Total	11				
-------	----	--	--	--	--

		sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	74.4	76.5	false	
IF cn # NIL THEN	1				
md := cn.text;	1				
sc.ConnectTo(md);	1				
sum := 0.0;	1				
sc.ScanReal(balance);	1				
WHILE ~sc.eot DO	2				
sum := sum + balance;	2				
sc.ScanReal(balance)	2				
END;					
PboxStrings.RealToString(sum, 1, 2, sumString);	0				
StdLog.String("Total is \$");	0				
StdLog.String(sumString); StdLog.Ln	0				
END					

Total	12				
-------	----	--	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	74.4	76.5	false
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	3			
sum := sum + balance;	2			
sc.ScanReal(balance)	2			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	13			
-------	----	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	150.9	76.5	false
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	3			
sum := sum + balance;	3			
sc.ScanReal(balance)	2			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total 14

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	150.9	?	true
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	3			
sum := sum + balance;	3			
sc.ScanReal(balance)	3			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total	15			
-------	----	--	--	--

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	150.9	?	true
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	4			
sum := sum + balance;	3			
sc.ScanReal(balance)	3			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	0			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

 Total

16

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	150.9	?	true "150.90"
IF cn # NIL THEN	1			
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	4			
sum := sum + balance;	3			
sc.ScanReal(balance)	3			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	1			
StdLog.String("Total is \$");	0			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total 17

	sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	150.9	?	true
IF cn # NIL THEN	1			“150.90”
md := cn.text;	1			
sc.ConnectTo(md);	1			
sum := 0.0;	1			
sc.ScanReal(balance);	1			
WHILE ~sc.eot DO	4			
sum := sum + balance;	3			
sc.ScanReal(balance)	3			
END;				
PboxStrings.RealToString(sum, 1, 2, sumString);	1			
StdLog.String("Total is \$");	1			
StdLog.String(sumString); StdLog.Ln	0			
END				

Total 18

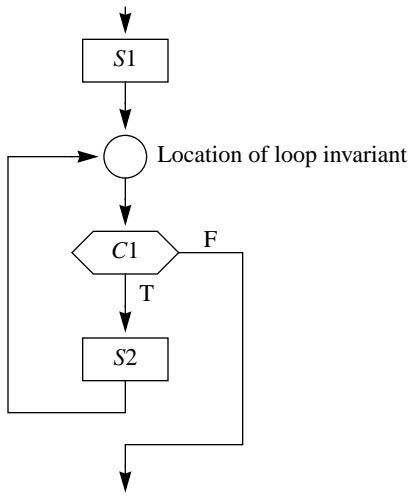
		sum	balance	sc.eot	sumString
cn := TextControllers.Focus();	1	150.9	?	true	“150.90”
IF cn # NIL THEN	1				
md := cn.text;	1				
sc.ConnectTo(md);	1				
sum := 0.0;	1				
sc.ScanReal(balance);	1				
WHILE ~sc.eot DO	4				
sum := sum + balance;	3				
sc.ScanReal(balance)	3				
END;					
PboxStrings.RealToString(sum, 1, 2, sumString);	1				
StdLog.String("Total is \$");	1				
StdLog.String(sumString); StdLog.Ln	1				
END					

Total 19

Statement	No data values	Three data values	n data values
(1)	1	1	1
(2)	1	1	1
(3)	1	1	1
(4)	1	1	1
(5)	1	1	1
(6)	1	1	1
(7)	1	4	$n + 1$
(8)	0	3	n
(9)	0	3	n
(10)	1	1	1
(11)	1	1	1
(12)	1	1	1
Total:	10	19	$3n + 10$

Figure 10.4

Statement execution count for the procedure ComputeTotal in Figure 10.3.



(a) Flowchart.

Figure 10.5

The location of the loop invariant for a WHILE loop.

```

Statement 1
(* Location of loop invariant *)
(* Loop invariant is true. *)
WHILE Condition1 DO
  Statement2
END
(* Loop invariant is true and Condition1 is false. *)
  
```

(b) Source code.

```
BEGIN
  cn := TextControllers.Focus();
  IF cn # NIL THEN
    md := cn.text;
    sc.ConnectTo(md);
    sum := 0.0;
    sc.ScanReal(balance);
    (* Here is where the loop invariant is true *)
    WHILE ~sc.eot DO
      sum := sum + balance;
      sc.ScanReal(balance)
    END;
    PboxStrings.RealToString(sum, 1, 2, sumString);
    StdLog.String("Total is $");
    StdLog.String(sumString); StdLog.Ln
  END
END ComputeTotal;
```

- sum is the total of all the values scanned, not including the current value scanned into balance.

The loop invariant for Figure 10.3

To prove that a statement is a loop invariant, you must show two things:

- The statement is true initially because of the execution of $S1$.
- The statement is true at the end of each loop because of the execution of $S2$.

Proving a loop invariant

- The loop invariant is true.
- The loop condition is false.

*When a WHILE loop
terminates*

PROCEDURE (VAR s: Scanner) **ScanReal** (OUT x: REAL), NEW

Pre

s is connected to a text model. 20

Characters scanned represent a real or integer value. 21

Post

~s.eot

x gets the next real or integer value scanned.

s.eot

x gets MAX(REAL)

PROCEDURE (VAR s: Scanner) **ScanInt** (OUT n: INTEGER), NEW

Pre

s is connected to a text model. 20

Characters scanned represent an integer value. 21

Post

~s.eot

n gets the next integer value scanned.

s.eot

n gets MAX(INTEGER)

```
sum := 0.0;
numAccts := 0;
sc.ScanReal(balance);
WHILE ~sc.eot DO
    sum := sum + balance;
    INC(numAccts);
    sc.ScanReal(balance)
END;
IF numAccts > 0 THEN
    Output sum / numAccts
ELSE
    Output a no accounts message
END
```

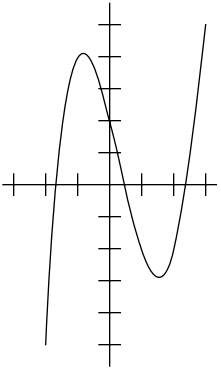
Figure 10.6

An algorithm to find the average of all the data values in the focus window.

```
sc.ScanInt(num)
IF sc.eot THEN
    Output empty window message
ELSE
    largest := num
    sc.ScanInt(num)
    WHILE ~sc.eot DO
        IF num > largest THEN
            largest := num
        END
        sc.ScanInt(num)
    END
    Output largest
END
```

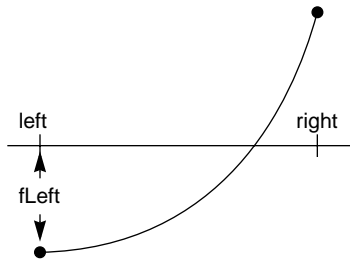
Figure 10.7

An algorithm to find the largest value in the focus window.

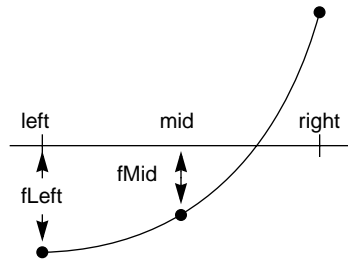
**Figure 10.8**

A graph of the function

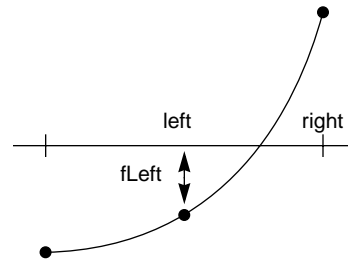
$$f(x) = x^3 - x^2 - 4x + 2$$



(a) Before the loop executes the first time.



(b) Computation of mid and fMid.



(c) Updating left and fLeft.

Figure 10.9

The bisection algorithm to find a root of $f(x)$.

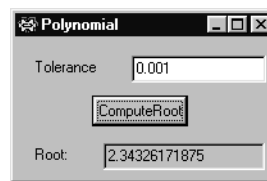
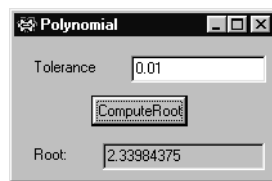
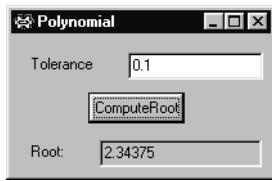


Figure 10.10

Three executions of the bisection algorithm of Listing 10.11.

```
MODULE Pbox10B;
IMPORT Dialog;
VAR
  d*: RECORD
    tolerance*: REAL;
    root*: REAL
  END;

PROCEDURE ComputeRoot*;
CONST
  a3 = 1.0; a2 = -1.0; a1 = -4.0; a0 = 2.0;
VAR
  left, fLeft: REAL;
  mid, fMid: REAL;
  right: REAL;
```

Figure 10.11

Computation of the root of a polynomial equation with the bisection algorithm.

```
BEGIN
  left := 2.0;
  fLeft := ((a3 * left + a2) * left + a1) * left + a0;
  right := 3.0;
  (* Assert: root is between left and right *)
  WHILE ABS(left - right) > d.tolerance DO
    mid := (left + right) / 2.0;
    fMid := ((a3 * mid + a2) * mid + a1) * mid + a0;
    IF fLeft * fMid > 0.0 THEN
      (* Assert: root is between mid and right *)
      left := mid;
      fLeft := fMid
    ELSE
      (* Assert: root is between left and mid *)
      right := mid
    END
  END
  d.root := (left + right) / 2.0;
  Dialog.Update(d)
END ComputeRoot;
```

```
BEGIN
  d.tolerance := 1.0;
  d.root := 0.0
END Pbox10B.
```

If the focus window contains the text

```
"123-A6002" 35.0 13.00  
"123-A6517" 45.0 10.00  
"561-B3882" 40.0 12.50  
"561-B4559" 40.0 11.00  
"561-B7384" 50.0 10.00
```

then the output to the Log should be

```
123-A6002 35.0 455.00  
123-A6517 45.0 475.00  
561-B3882 40.0 500.00  
561-B4559 40.0 440.00  
561-B7384 50.0 550.00  
Average wages: 484.00  
Number with overtime: 2
```


VAR

```
sc: PboxMappers.Scanner;  
empID: ARRAY 16 OF CHAR;  
hours, rate: REAL;  
wages, totalWages, aveWages: REAL;  
numEmp, numOvertime: INTEGER;
```

Initialize variables

Input empID, hours, rate

WHILE ~sc.eot DO

Process empID, hours, rate

Input empID, hours, rate

END

Compute the average

Output aveWages, numOvertime

Initialize variables

Input empID, hours, rate

WHILE ~sc.eot DO

 IF *employee did not work overtime* THEN

Compute wages without overtime

 ELSE

Compute wages with overtime

 END

Output empID, hours, wages

Input empID, hours, rate

END

Compute the average

Output aveWages, numOvertime

```
totalWages := 0.0
numEmp := 0
numOvertime := 0
Input empID, hours, rate
WHILE ~s.eot DO
  IF employee did not work overtime THEN
    wages := hours * rate
  ELSE
    wages := 40.0 * rate + (hours - 40.0) * 1.5 * rate
    INC(numOvertime)
  END
  totalWages := totalWages + wages
  INC(numEmp)
  Output empID, hours, wages
  Input empID, hours, rate
END
IF numEmp > 0 THEN
  aveWages := totalWages / numEmp
ELSE
  aveWages := 0.00
END;
Output aveWages, numOvertime
```

```
MODULE Pbox10C;
  IMPORT TextModels, TextControllers, PboxMappers, PboxStrings, StdLog;

  PROCEDURE ProcessPayroll*;
    VAR
      md: TextModels.Model;
      cn: TextControllers.Controller;
      sc: PboxMappers.Scanner;
      empID: ARRAY 16 OF CHAR;
      hours, rate: REAL;
      wages, totalWages, aveWages: REAL;
      numEmp, numOvertime: INTEGER;
      outString: ARRAY 32 OF CHAR;
    BEGIN
      cn := TextControllers.Focus();
      IF cn # NIL THEN
        md := cn.text;
        sc.ConnectTo(md);
        totalWages := 0.0; numEmp := 0; numOvertime := 0;
        sc.ScanString(empID); sc.ScanReal(hours); sc.ScanReal(rate);
```

Figure 10.12

A payroll report with summary information

```
WHILE ~sc.eot DO
  IF hours <= 40 THEN
    wages := hours * rate
  ELSE
    wages := 40.0 * rate + (hours - 40.0) * 1.5 * rate;
    INC(numOvertime)
  END;
  StdLog.String(empID);
  PboxStrings.RealToString(hours, 8, 1, outString); StdLog.String(outString);
  PboxStrings.RealToString(wages, 12, 2, outString); StdLog.String(outString);
  StdLog.Ln;
  totalWages := totalWages + wages;
  INC(numEmp);
  sc.ScanString(empID); sc.ScanReal(hours); sc.ScanReal(rate)
END;
IF numEmp > 0 THEN
  aveWages := totalWages / numEmp
ELSE
  aveWages := 0.00
END;
StdLog.String("Average wages: ");
PboxStrings.RealToString(aveWages, 1, 2, outString); StdLog.String(outString); StdLog.Ln;
StdLog.String("Number with overtime: ");
PboxStrings.IntToString(numOvertime, 1, outString); StdLog.String(outString); StdLog.Ln;
END
END ProcessPayroll;

END Pbox10C.
```

The structured programming theorem

Any algorithm, no matter how large or complicated, can be written with only three control statements—sequence, which is one statement following another, the IF statement, and the WHILE statement.

```
sum := 0
i := 1
WHILE i <= 100 DO
    sum := sum + i
    INC(i)
END
Output sum
```

Figure 10.13

An algorithm for the sum of consecutive integers with a WHILE loop.

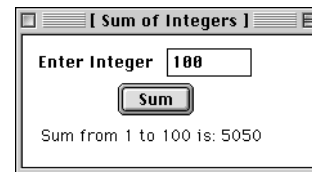

```
MODULE Pbox10D;
  IMPORT Dialog, PboxStrings;
  VAR
    d*: RECORD
      num*: INTEGER;
      message-: ARRAY 64 OF CHAR
    END;

  PROCEDURE ComputeSum*;
    VAR
      sum, i: INTEGER;
      intString: ARRAY 16 OF CHAR;
    BEGIN
      sum := 0;
      FOR i := 1 TO d.num DO
        sum := sum + i
      END;
      PboxStrings.IntToString(d.num, 1, intString);
      d.message := "Sum from 1 to " + intString + " is: ";
      PboxStrings.IntToString(sum, 1, intString);
      d.message := d.message + intString;
      Dialog.Update(d)
    END ComputeSum;

  BEGIN
    d.num := 0;
    d.message := ""
  END Pbox10D.
```

Figure 10.14

Computing the sum of the first `d.num` integers with a FOR loop.

**Figure 10.15**

The dialog box for the program of Figure 10.14.

```
sum := d.num * (d.num + 1) / 2  
Output sum
```

Figure 10.16

A better algorithm for the sum of consecutive integers.

```
WHILE  $C1$  DO  
   $S1$   
END
```

is written in GCL as

```
do  $C1 \rightarrow S1$  od
```

```
s := 0.0; nA := 0; sc.ScanR(b);  
do ¬sc.eot → s := s + b; nA := nA + 1; sc.ScanR(b) od  
if nA > 0 → Output s/nA  
  □ nA ≤ 0 → Output a no accounts message  
fi
```