

# The Composite State Binary Tree

## BiTreeCS

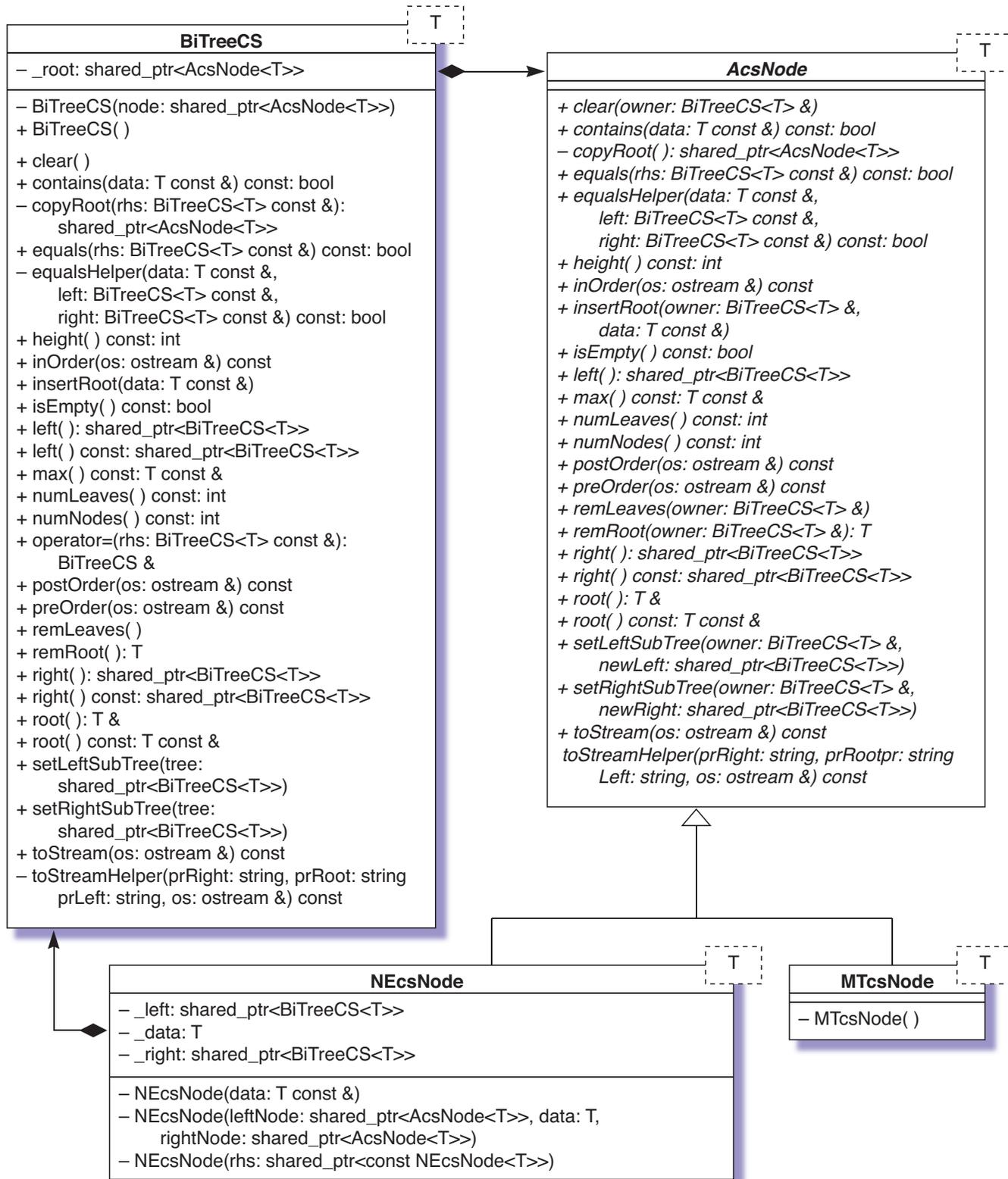
# The Composite State Binary Tree

## BiTreeCS

In a nonempty node

- `_left` is a binary tree
- `_right` is a binary tree

# Figure 8.24

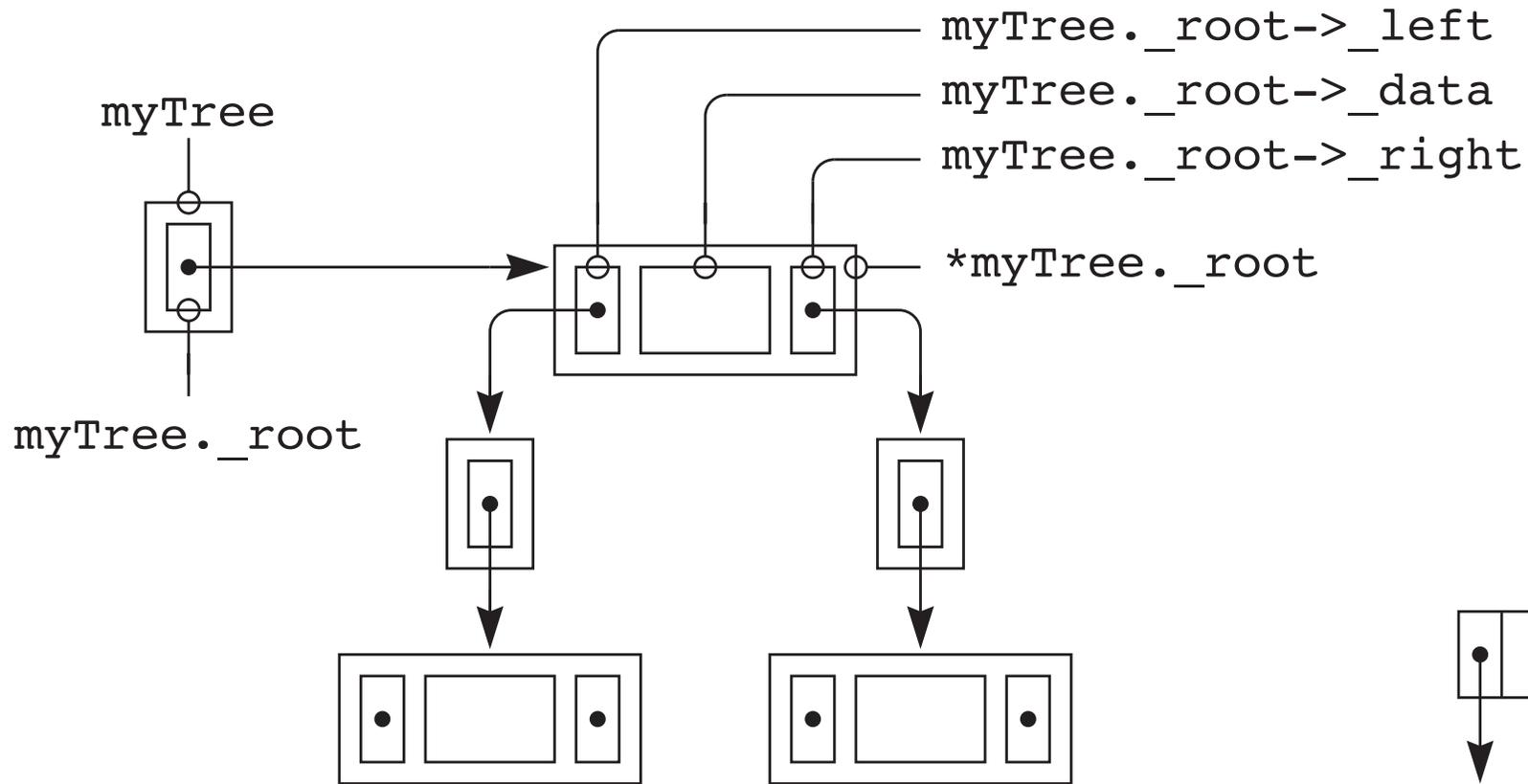


```
template<class T> class BiTreeCS {  
private:  
    shared_ptr<AcsNode<T>> _root;
```

```
template<class T> class NEcsNode : public AcsNode<T> {  
private:  
    shared_ptr<BiTreeCS<T>> _left;  
    T _data;  
    shared_ptr<BiTreeCS<T>> _right;
```

```
template<class T> class BiTreeCS {  
private:  
    shared_ptr<AcsNode<T>> _root;
```

```
template<class T> class NEcsNode : public AcsNode<T> {  
private:  
    shared_ptr<BiTreeCS<T>> _left;  
    T _data;  
    shared_ptr<BiTreeCS<T>> _right;
```



**(a)** A detailed rendering of a binary tree and a node.

**(b)** An abbreviated rendering.

# Methods for output and characterization

```
// ===== preOrder =====  
// Post: A preorder representation of this tree  
// is sent to os.  
  
template<class T>  
void BiTreeCS<T>::preOrder(ostream &os) const {  
    _root->preOrder(os);  
}  
  
template<class T>  
void MTcsNode<T>::preOrder(ostream &os) const {  
}  
  
template<class T>  
void NEcsNode<T>::preOrder(ostream &os) const {  
    os << _data << "  ";  
    _left->preOrder(os);  
    _right->preOrder(os);  
}
```

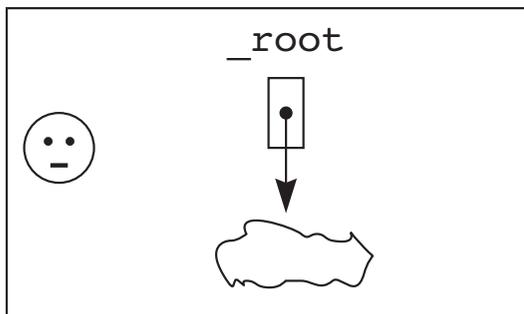
```
// ===== isEmpty =====  
// Post: true is returned if this tree is empty;  
// otherwise, false is returned.  
  
template<class T>  
bool BiTreeCS<T>::isEmpty() const {  
    return _root->isEmpty();  
}  
  
template<class T>  
bool MTcsNode<T>::isEmpty() const {  
    return true;  
}  
  
template<class T>  
bool NEcsNode<T>::isEmpty() const {  
    return false;  
}
```

```
// ===== isEmpty =====  
// Post: true is returned if this tree is empty;  
// otherwise, false is returned.
```

```
template<class T>  
bool BiTreeCS<T>::isEmpty() const {  
    return _root->isEmpty();  
}
```

```
template<class T>  
bool MTcsNode<T>::isEmpty() const {  
    return true;  
}
```

```
template<class T>  
bool NEcsNode<T>::isEmpty() const {  
    return false;  
}
```



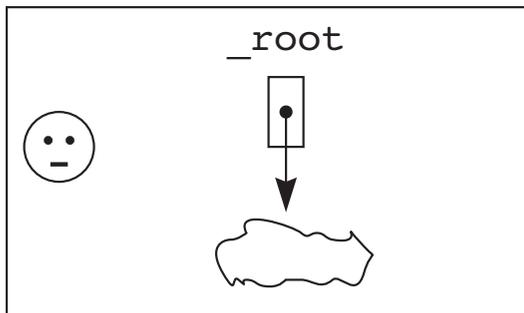
(a) The environment of a binary tree.

```
// ===== isEmpty =====  
// Post: true is returned if this tree is empty;  
// otherwise, false is returned.
```

```
template<class T>  
bool BiTreeCS<T>::isEmpty() const {  
    return _root->isEmpty();  
}
```

```
template<class T>  
bool MTcsNode<T>::isEmpty() const {  
    return true;  
}
```

```
template<class T>  
bool NEcsNode<T>::isEmpty() const {  
    return false;  
}
```



**(a)** The environment of a binary tree.



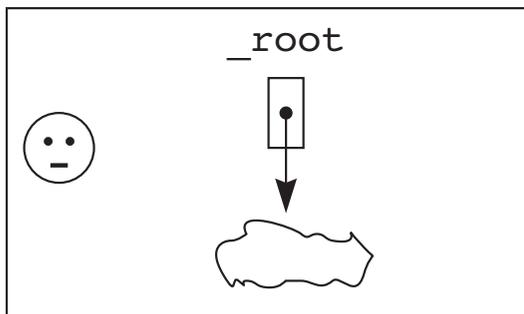
**(b)** The environment of an empty node.

```
// ===== isEmpty =====
// Post: true is returned if this tree is empty;
// otherwise, false is returned.
```

```
template<class T>
bool BiTreeCS<T>::isEmpty() const {
    return _root->isEmpty();
}
```

```
template<class T>
bool MTcsNode<T>::isEmpty() const {
    return true;
}
```

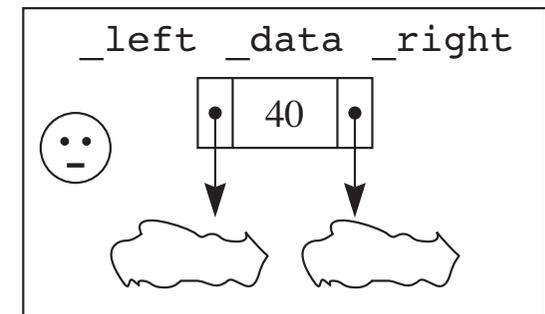
```
template<class T>
bool NEcsNode<T>::isEmpty() const {
    return false;
}
```



(a) The environment of a binary tree.



(b) The environment of an empty node.



(c) The environment of a nonempty node.

```
// ===== left =====
// Pre: This tree is not empty.
// Post: A shared_ptr to the left child of this tree is returned.

template<class T>
shared_ptr<BiTreeCS<T>> BiTreeCS<T>::left() {
    return _root->left();
};

template<class T>
shared_ptr<BiTreeCS<T>> MTcsNode<T>::left() {
    cerr << "left precondition violated: "
         << "An empty tree has has no left subtree."
         << endl;
    throw -1;
}

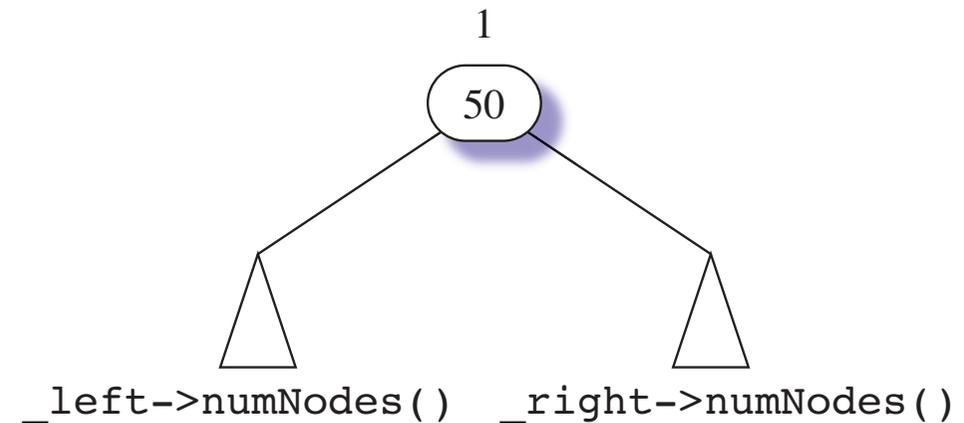
template<class T>
shared_ptr<BiTreeCS<T>> NEcsNode<T>::left() {
    return _left;
}
```

```
// ===== numNodes =====  
// Post: The number of nodes of this tree is returned.
```

```
template<class T>  
int BiTreeCS<T>::numNodes() const {  
    return _root->numNodes();  
}
```

```
template<class T>  
int MTcsNode<T>::numNodes() const {  
    return 0;  
}
```

```
template<class T>  
int NEcsNode<T>::numNodes() const {  
    return 1 + _left->numNodes() + _right->numNodes();  
}
```



```
// ===== max =====
// Pre: This tree is not empty.
// Post: The maximum element of this tree is returned.

template<class T>
T const &BiTreeCS<T>::max() const {
    return _root->max();
}

template<class T>
T const &MTcsNode<T>::max() const {
    cerr << "max precondition violated: "
         << "An empty tree has no maximum." << endl;
    throw -1;
}

template<class T>
T const &NEcsNode<T>::max() const {
    T const &leftMax = (_left->isEmpty()) ? _data : _left->max();
    T const &rightMax = (_right->isEmpty()) ? _data : _right->max();
    return (leftMax > rightMax) ?
        ((leftMax > _data) ? leftMax : _data) :
        ((rightMax > _data) ? rightMax : _data);
}
```

```
// ===== equals =====
// Post: true is returned if this tree equals tree rhs;
// otherwise, false is returned.
// Two trees are equal if they contain the same number
// of equal elements with the same shape.

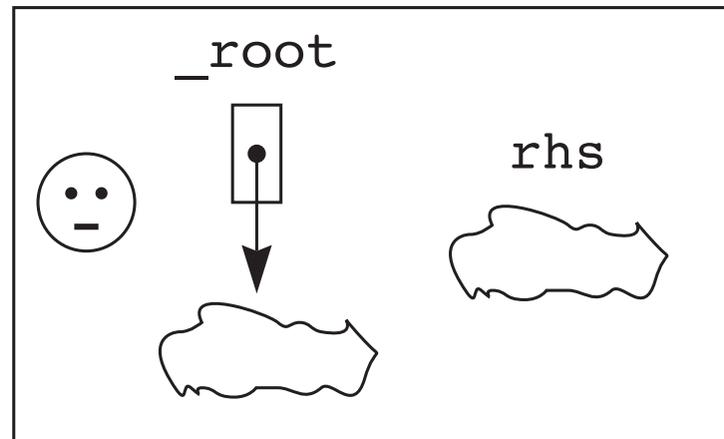
template<class T>
bool BiTreeCS<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "BiTreeCS<T>::equals: Exercise for the student." << endl;
    throw -1;
}

template<class T>
bool MTcsNode<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "MTcsNode<T>::equals: Exercise for the student." << endl;
    throw -1;
}

template<class T>
bool NEcsNode<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "NEcsNode<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```

```
template<class T>
bool BiTreeCS<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "BiTreeCS<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```

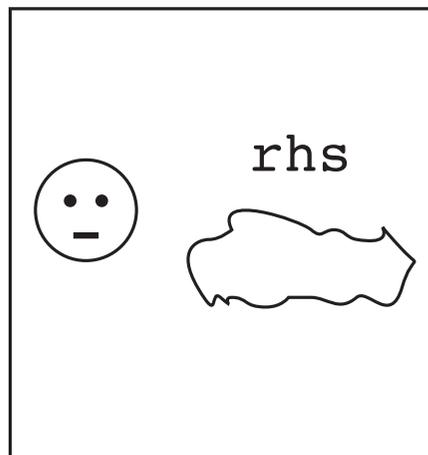
```
template<class T>
bool BiTreeCS<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "BiTreeCS<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```



(a) The environment of a binary tree.

```
template<class T>
bool MTcsNode<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "MTcsNode<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```

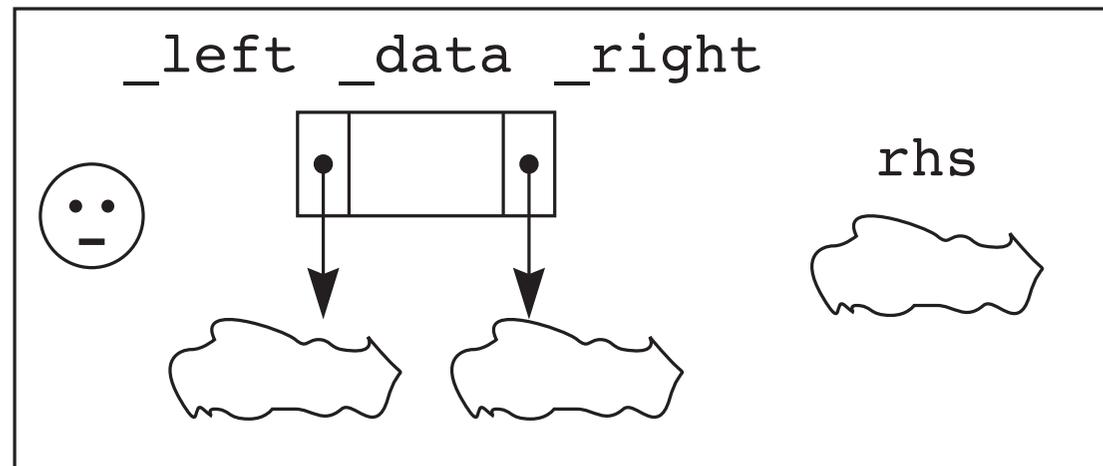
```
template<class T>
bool MTcsNode<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "MTcsNode<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```



**(b)** The environment of an empty node.

```
template<class T>
bool NEcsNode<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "NEcsNode<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```

```
template<class T>
bool NEcsNode<T>::equals(BiTreeCS<T> const &rhs) const {
    cerr << "NEcsNode<T>::equals: Exercise for the student." << endl;
    throw -1;
}
```



(c) The environment of a nonempty node.

```
// ----- equalsHelper -----
// Post: true is returned if root equals this->root(),
// left equals this->left(), and right equals this->right();
// otherwise, false is returned.

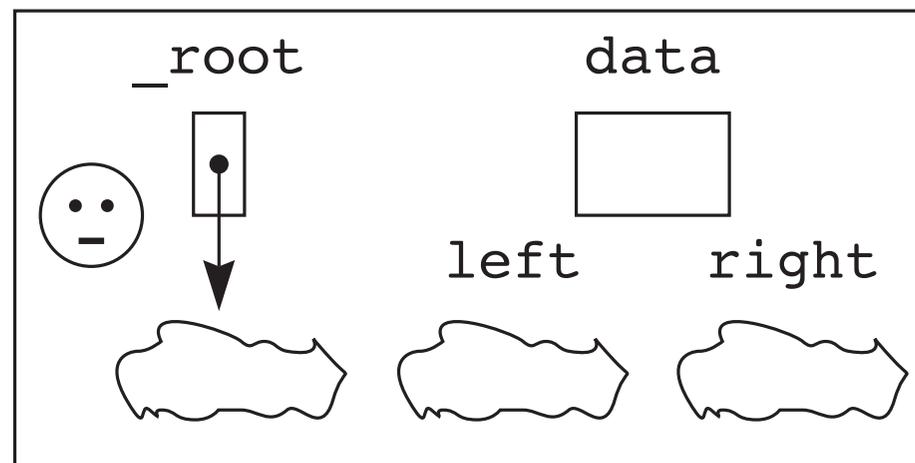
template<class T>
bool BiTreeCS<T>::equalsHelper(T const &data,
    BiTreeCS<T> const &left, BiTreeCS<T> const &right) const {
    cerr << "BiTreeCS<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}

template<class T>
bool MTcsNode<T>::equalsHelper(T const &,
    BiTreeCS<T> const &, BiTreeCS<T> const &) const {
    cerr << "MTcsNode<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}

template<class T>
bool NEcsNode<T>::equalsHelper(T const &data,
    BiTreeCS<T> const &left, BiTreeCS<T> const &right) const {
    cerr << "NEcsNode<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}
```

```
// ----- equalsHelper -----  
template<class T>  
bool BiTreeCS<T>::equalsHelper(T const &data,  
    BiTreeCS<T> const &left, BiTreeCS<T> const &right) const {  
    cerr << "BiTreeCS<T>::equalsHelper: Exercise for the student." << endl;  
    throw -1;  
}
```

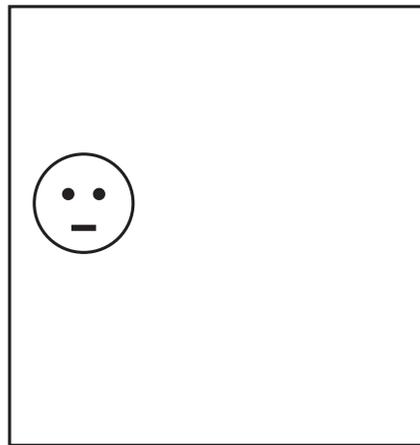
```
// ----- equalsHelper -----  
template<class T>  
bool BiTreeCS<T>::equalsHelper(T const &data,  
    BiTreeCS<T> const &left, BiTreeCS<T> const &right) const {  
    cerr << "BiTreeCS<T>::equalsHelper: Exercise for the student." << endl;  
    throw -1;  
}
```



(a) The environment of a binary tree.

```
template<class T>
bool MTcsNode<T>::equalsHelper(T const &,
    BiTreeCS<T> const &, BiTreeCS<T> const &) const {
    cerr << "MTcsNode<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}
```

```
template<class T>
bool MTcsNode<T>::equalsHelper(T const &,
    BiTreeCS<T> const &, BiTreeCS<T> const &) const {
    cerr << "MTcsNode<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}
```



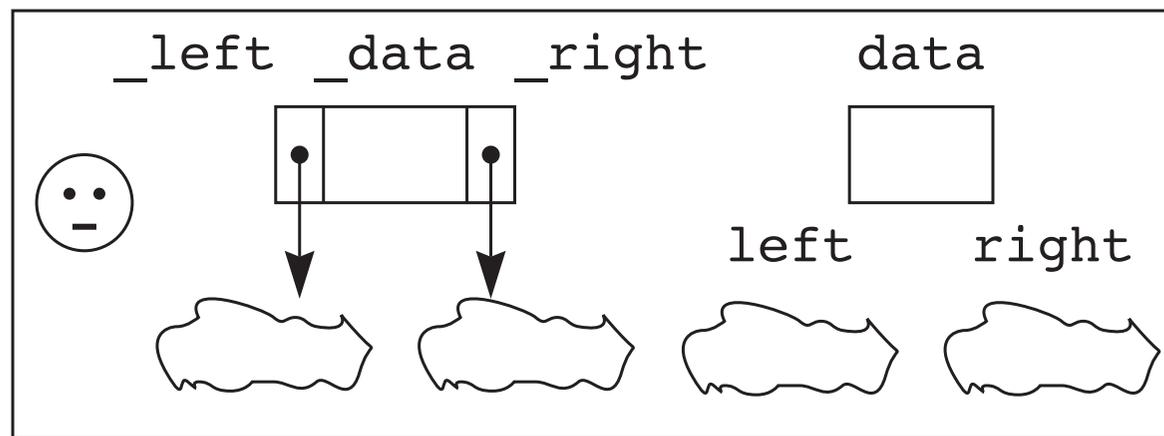
**(b)** The environment of an empty node.

```
template<class T>
bool NEcsNode<T>::equalsHelper(T const &data,
    BiTreeCS<T> const &left, BiTreeCS<T> const &right) const {
    cerr << "NEcsNode<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}
```

```

template<class T>
bool NEcsNode<T>::equalsHelper(T const &data,
    BiTreeCS<T> const &left, BiTreeCS<T> const &right) const {
    cerr << "NEcsNode<T>::equalsHelper: Exercise for the student." << endl;
    throw -1;
}

```

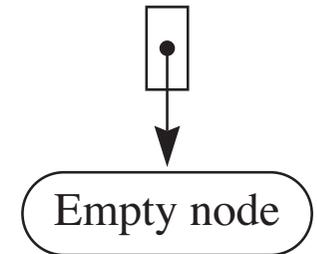


(c) The environment of a nonempty node.

# Methods for construction and insertion

## Two constructors for BiTreeCS

```
// ===== Constructors =====  
template<class T>  
BiTreeCS<T>::BiTreeCS():  
    _root(new MTcsNode<T>()) {  
}  
  
// Post: _root points to node with no allocation.  
template<class T>  
BiTreeCS<T>::BiTreeCS(shared_ptr<AcsNode<T>> node):  
    _root(node) {  
}
```



The empty tree created by `BiTreeCS()`.

## Three constructors for NEcsNode

```
// Post: _data is data.
template<class T>
NEcsNode<T>::NEcsNode(T const &data):
    _left(make_shared<BiTreeCS<T>>()),
    _data(data),
    _right(make_shared<BiTreeCS<T>>()) {
}
```

## Three constructors for NEcsNode

```
// Post: _left->_root and _right->_root point to leftNode
// and rightNode, and _data is data.
template<class T>
NEcsNode<T>::NEcsNode(shared_ptr<AcsNode<T>> leftNode,
                    T data,
                    shared_ptr<AcsNode<T>> rightNode):
    NEcsNode(data) {
    _left->_root = leftNode;
    _right->_root = rightNode;
}
```

## Three constructors for NEcsNode

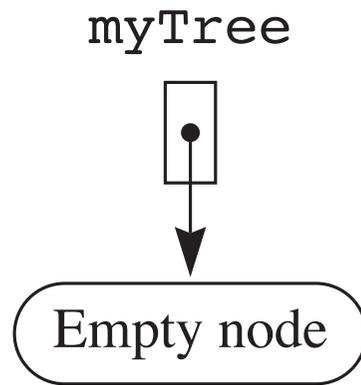
```
// Post: _left is rhs->_left, _data is rhs->_data,  
// and _right is rhs->_right.  
template<class T>  
NEcsNode<T>::NEcsNode(shared_ptr<const NEcsNode<T>> rhs):  
    _left(rhs->_left),  
    _data(rhs->_data),  
    _right(rhs->_right) {  
}
```

```
// ===== insertRoot =====
// Pre: This tree is empty.
// Post: This tree has one root node containing data.

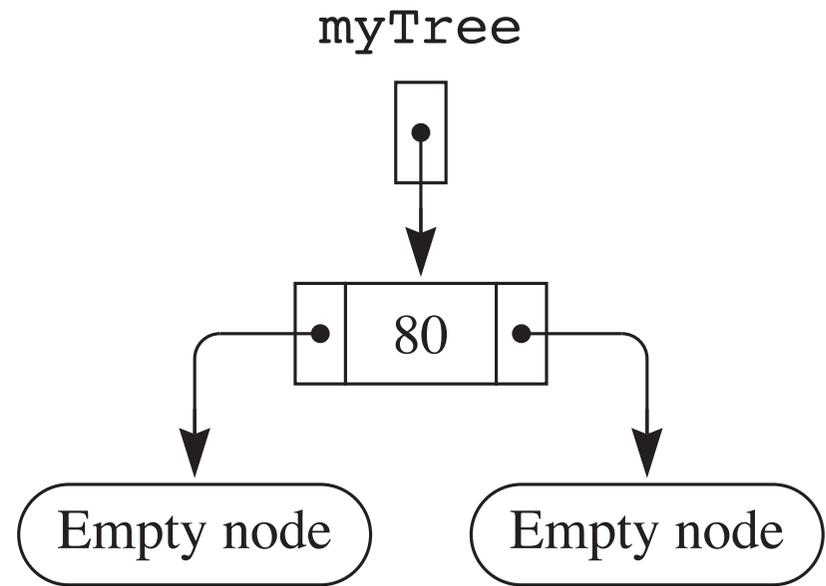
template<class T>
void BiTreeCS<T>::insertRoot(T const &data) {
    _root->insertRoot(*this, data);
}

template<class T>
void MTcsNode<T>::insertRoot(BiTreeCS<T> &owner, T const &data) {
    owner._root.reset(new NEcsNode<T>(data));
}

template<class T>
void NEcsNode<T>::insertRoot(BiTreeCS<T> &, T const &) {
    cerr << "insertRoot precondition violated: "
         << "Cannot insert root into a non empty tree" << endl;
    throw -1;
}
```



(a) Initial tree.



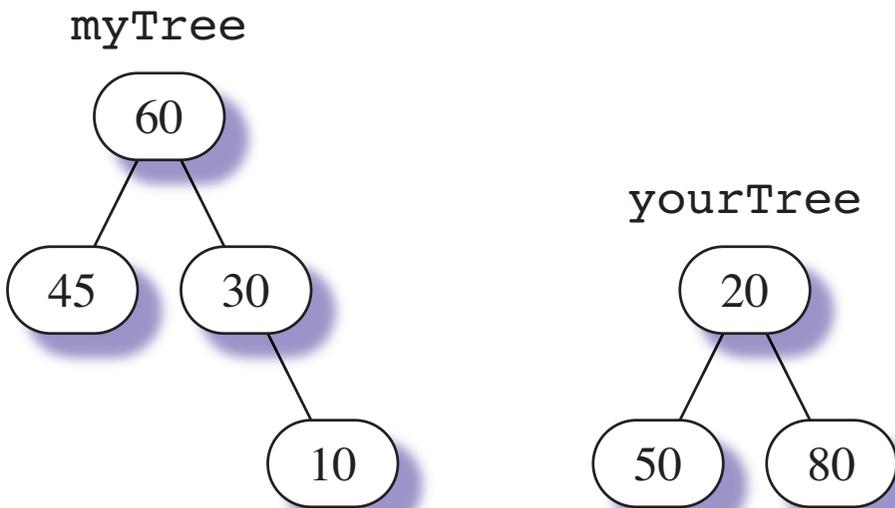
(b) `myTree.insertRoot(80);`

```
// ===== setLeftSubTree =====
// Pre: This tree is not empty.
// Post: The left subtree of this tree is replaced by newLeft.

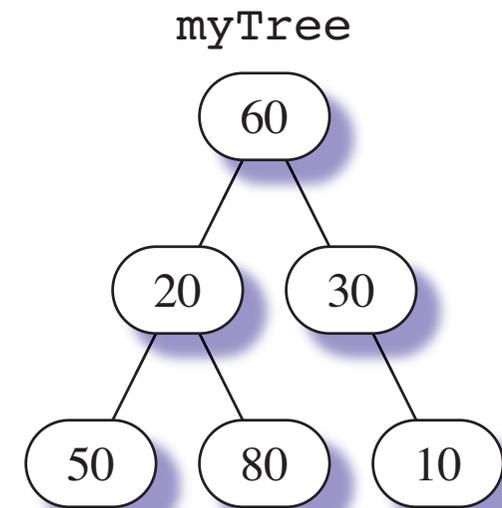
template<class T>
void BiTreeCS<T>::setLeftSubTree(shared_ptr<BiTreeCS<T>> newLeft) {
    _root->setLeftSubTree(*this, newLeft);
}

template<class T>
void MTcsNode<T>::setLeftSubTree(BiTreeCS<T>&,
                                shared_ptr<BiTreeCS<T>> ) {
    cerr << "setLeftSubTree precondition violated: "
         << "An empty list has no left subtree." << endl;
    throw -1;
}

template<class T>
void NEcsNode<T>::setLeftSubTree(BiTreeCS<T> &owner,
                                shared_ptr<BiTreeCS<T>> newLeft) {
    _left = newLeft;
}
```



(a) Initial trees.



(b) `myTree.setLeftSubTree(yourTree);`

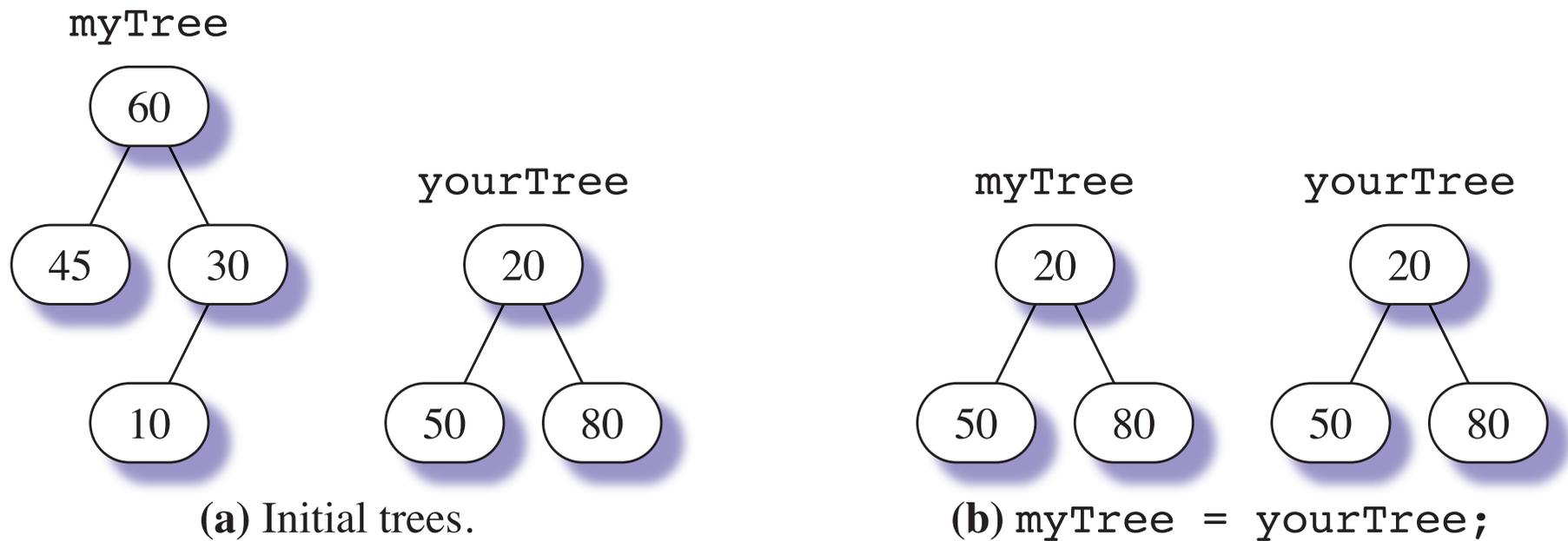
```
// ===== operator= =====  
// Post: A deep copy of rhs is returned.  
  
template<class T>  
BiTreeCS<T> &BiTreeCS<T>::operator=(BiTreeCS<T> const &rhs) {  
    if (this != &rhs) { // In case someone writes myTree = myTree;  
        _root = copyRoot(rhs);  
    }  
    return *this;  
}
```

```
// ===== copyRoot =====
// Post: A deep copy of the root of rhs is returned.

template<class T>
shared_ptr<AcsNode<T>> BiTreeCS<T>::copyRoot(BiTreeCS<T> const &rhs) {
    return rhs._root->copyRoot();
}

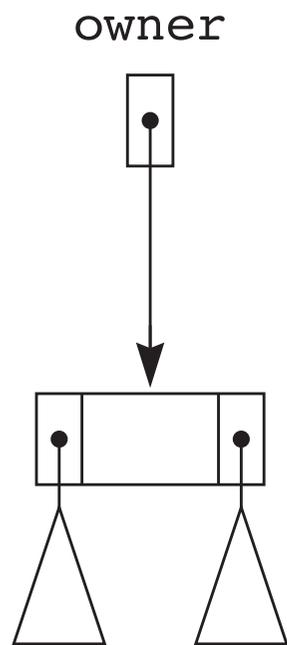
template<class T>
shared_ptr<AcsNode<T>> MTcsNode<T>::copyRoot() {
    return shared_ptr<MTcsNode<T>>(new MTcsNode<T>());
}

template<class T>
shared_ptr<AcsNode<T>> NEcsNode<T>::copyRoot() {
    return shared_ptr<NEcsNode<T>>(new NEcsNode<T>(
        _left->_root->copyRoot(),
        _data,
        _right->_root->copyRoot()));
}
```

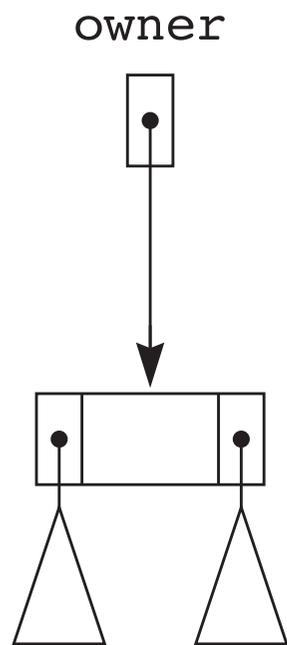


# Methods for removal

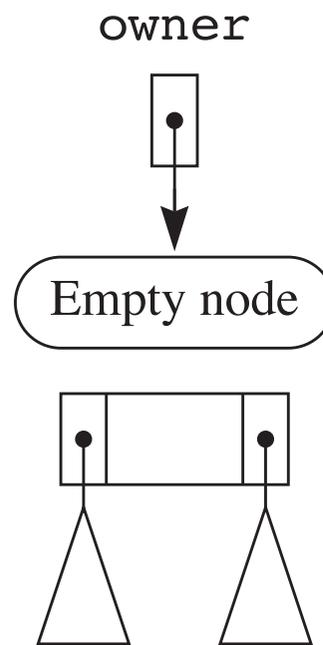
```
// ===== clear =====  
// Post: This tree is cleared to the empty tree.  
  
template<class T>  
void BiTreeCS<T>::clear() {  
    cerr << "BiTreeCS<T>::clear: Exercise for the student." << endl;  
    throw -1;  
}  
  
template<class T>  
void MTcsNode<T>::clear(BiTreeCS<T> &) {  
    cerr << "MTcsNode<T>::clear: Exercise for the student." << endl;  
    throw -1;  
}  
  
template<class T>  
void NEcsNode<T>::clear(BiTreeCS<T> &owner) {  
    cerr << "NEcsNode<T>::clear: Exercise for the student." << endl;  
    throw -1;  
}
```

The `clear()` operation for `BiTreeCS`

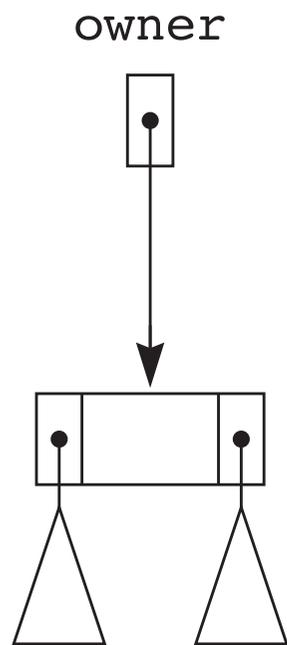
(a) Original.

The `clear()` operation for `BiTreeCS`

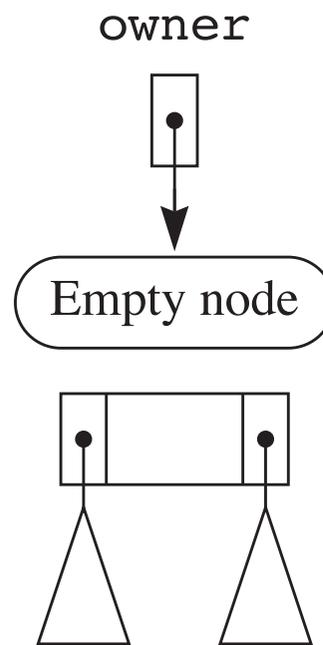
(a) Original.



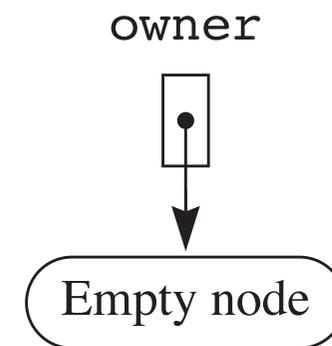
(b) Change owner.

The `clear()` operation for `BiTreeCS`

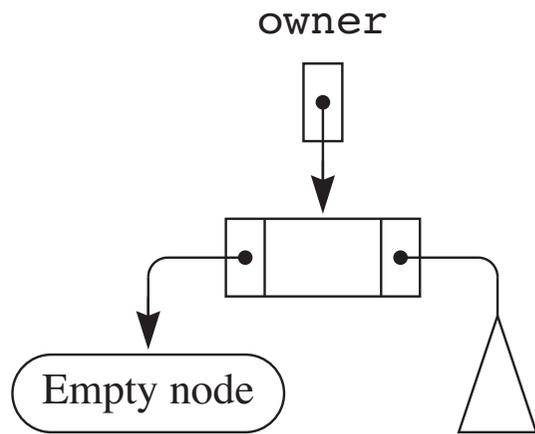
(a) Original.



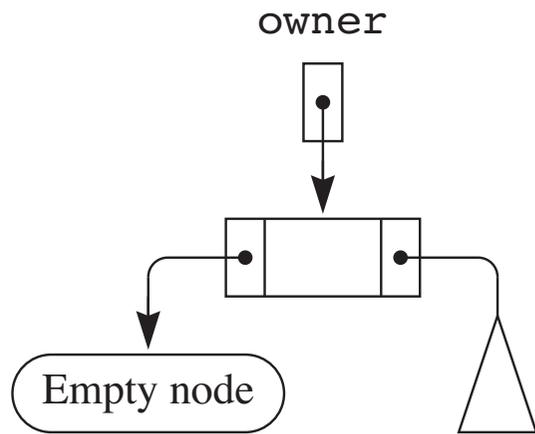
(b) Change owner.



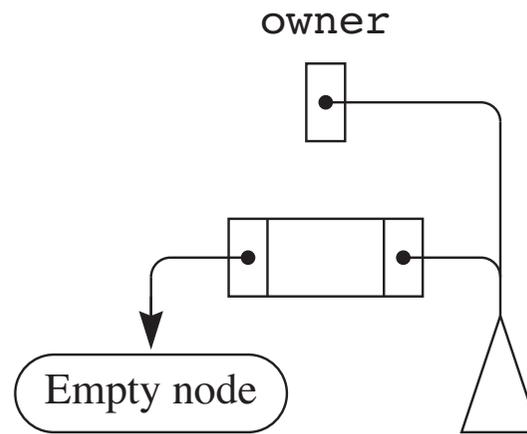
(c) Automatic garbage collection.

The `remRoot()` operation for `BiTreeCS`

(a) Original.

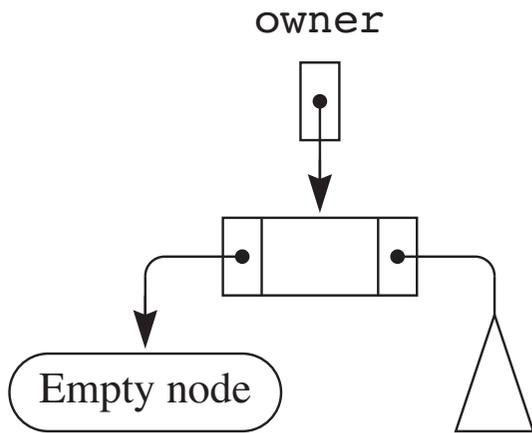
The `remRoot()` operation for `BiTreeCS`

(a) Original.

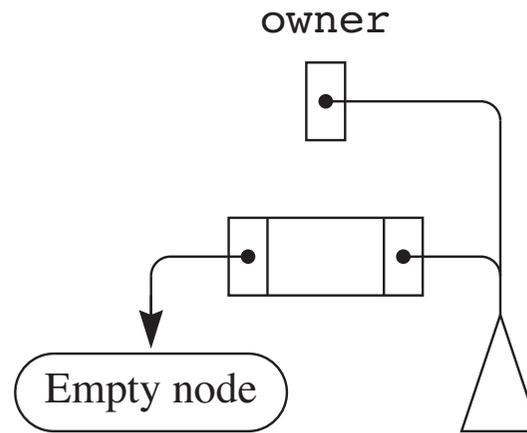


(b) Link owner.

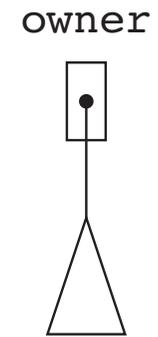
## The `remRoot ( )` operation for `BiTreeCS`



(a) Original.



(b) Link owner.



(c) Automatic garbage collection