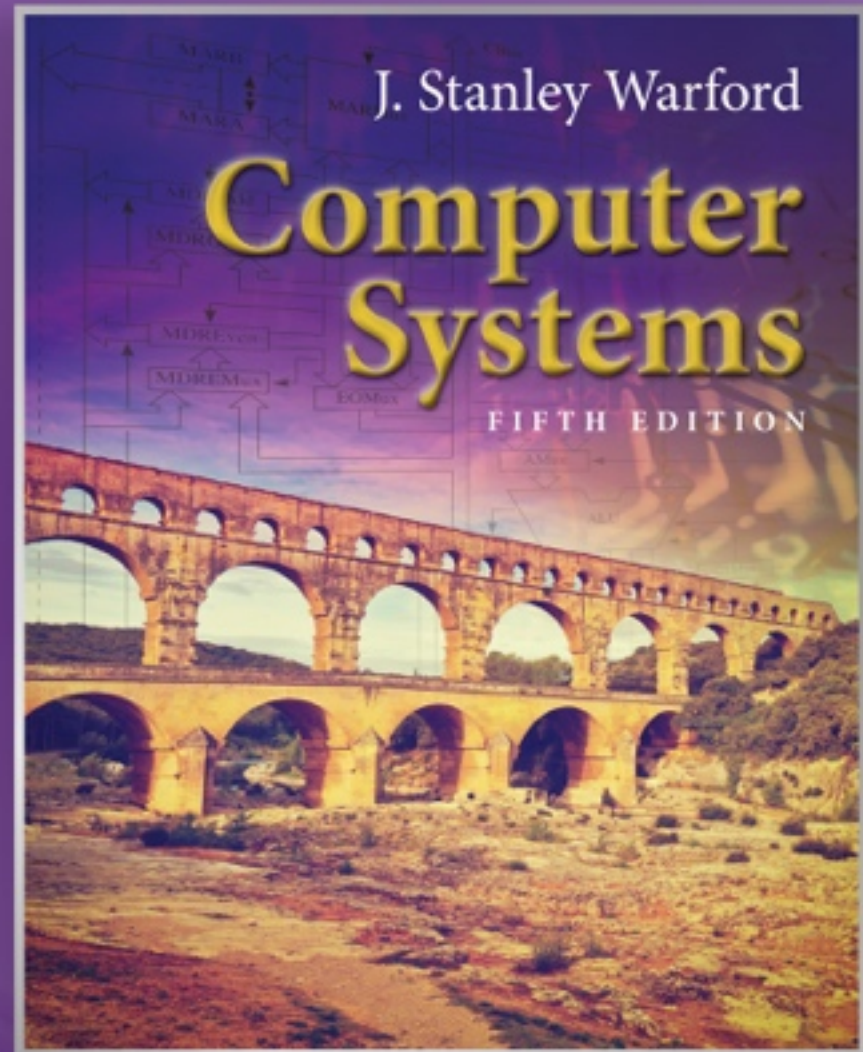


# Chapter 7

## Language Translation Principles



- The fundamental question of computer science:

“What can be automated?”

- One answer – Translation from one programming language to another.

- Alphabet – A nonempty set of characters.
- Concatenation – joining characters to form a string.
- The empty string – The identity element for concatenation.

# The C alphabet

{ a,b,c,d,e,f,g,h,i,j,k,l,m,n,  
o,p,q,r,s,t,u,v,w,x,y,z,A,B,  
C,D,E,F,G,H,I,J,K,L,M,N,O,P,  
Q,R,S,T,U,V,W,X,Y,Z,0,1,2,3,  
4,5,6,7,8,9,+,-,\*,/,=,<,>,[,  
,(,),{,},.,/, :, ;, &, !, %, ' , "  
\_, \, #, ?, }, |, ~ }

## The Pep/9 assembly language alphabet

{ a,b,c,d,e,f,g,h,i,j,k,l,m,n,  
o,p,q,r,s,t,u,v,w,x,y,z,A,B,  
C,D,E,F,G,H,I,J,K,L,M,N,O,P,  
Q,R,S,T,U,V,W,X,Y,Z,0,1,2,3,  
4,5,6,7,8,9,\,.,/, :, ;, ' , " }

# The alphabet for real numbers

$\{ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, +, -, \cdot \}$

# Concatenation

- Joining two or more characters to make a string
- Applies to strings concatenated to construct longer strings

# The empty string

- $\varepsilon$
- Concatenation property

$$\varepsilon x = x\varepsilon = x$$



# Languages

- The closure  $T^*$  of alphabet  $T$ 
  - ▶ The set of all possible strings formed by concatenating elements from  $T$
- Language
  - ▶ A subset of the closure of its alphabet

# Techniques to specify syntax

- Grammars
- Finite state machines
- Regular expressions

# The four parts of a grammar

- $N$ , a nonterminal alphabet
- $T$ , a terminal alphabet
- $P$ , a set of rules of production
- $S$ , the start symbol, an element of  $N$

$N = \{ \langle \text{identifier} \rangle , \langle \text{letter} \rangle , \langle \text{digit} \rangle \}$

$T = \{ a , b , c , 1 , 2 , 3 \}$

$P =$  the productions

1.  $\langle \text{identifier} \rangle \rightarrow \langle \text{letter} \rangle$
2.  $\langle \text{identifier} \rangle \rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle$
3.  $\langle \text{identifier} \rangle \rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$
4.  $\langle \text{letter} \rangle \rightarrow a$
5.  $\langle \text{letter} \rangle \rightarrow b$
6.  $\langle \text{letter} \rangle \rightarrow c$
7.  $\langle \text{digit} \rangle \rightarrow 1$
8.  $\langle \text{digit} \rangle \rightarrow 2$
9.  $\langle \text{digit} \rangle \rightarrow 3$

$S = \langle \text{identifier} \rangle$

## A derivation

<identifier>

## A derivation

$\langle \text{identifier} \rangle \Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$

Rule 3

# A derivation

$\langle \text{identifier} \rangle \Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$

Rule 3

$\Rightarrow \langle \text{identifier} \rangle 3$

Rule 9

# A derivation

$\langle \text{identifier} \rangle$	$\Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$	Rule 3
	$\Rightarrow \langle \text{identifier} \rangle 3$	Rule 9
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle 3$	Rule 2



# A derivation

$\langle \text{identifier} \rangle$	$\Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$	Rule 3
	$\Rightarrow \langle \text{identifier} \rangle 3$	Rule 9
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle b 3$	Rule 5

# A derivation

$\langle \text{identifier} \rangle$	$\Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$	Rule 3
	$\Rightarrow \langle \text{identifier} \rangle 3$	Rule 9
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle b 3$	Rule 5
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle b 3$	Rule 2

# A derivation

$\langle \text{identifier} \rangle$	$\Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$	Rule 3
	$\Rightarrow \langle \text{identifier} \rangle 3$	Rule 9
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle b 3$	Rule 5
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle b 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle a b 3$	Rule 4

# A derivation

$\langle \text{identifier} \rangle$	$\Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$	Rule 3
	$\Rightarrow \langle \text{identifier} \rangle 3$	Rule 9
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle b 3$	Rule 5
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle b 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle a b 3$	Rule 4
	$\Rightarrow \langle \text{letter} \rangle a b 3$	Rule 1

# A derivation

$\langle \text{identifier} \rangle$	$\Rightarrow \langle \text{identifier} \rangle \langle \text{digit} \rangle$	Rule 3
	$\Rightarrow \langle \text{identifier} \rangle 3$	Rule 9
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle b 3$	Rule 5
	$\Rightarrow \langle \text{identifier} \rangle \langle \text{letter} \rangle b 3$	Rule 2
	$\Rightarrow \langle \text{identifier} \rangle a b 3$	Rule 4
	$\Rightarrow \langle \text{letter} \rangle a b 3$	Rule 1
	$\Rightarrow c a b 3$	Rule 6

# A derivation

You can summarize the previous eight derivation steps as

$$\langle \text{identifier} \rangle \Rightarrow^* c \ a \ b \ 3$$

$$N = \{ I, F, M \}$$

$$T = \{ +, -, d \}$$

$P$  = the productions

1.  $I \rightarrow FM$

2.  $F \rightarrow +$

3.  $F \rightarrow -$

4.  $F \rightarrow \varepsilon$

5.  $M \rightarrow dM$

6.  $M \rightarrow d$

$$S = I$$

# Alternative notation for production rules

$$I \rightarrow FM$$

$$F \rightarrow + \mid - \mid \varepsilon$$

$$M \rightarrow d \mid dM$$



## Some derivations

$I \Rightarrow FM$

$\Rightarrow F\bar{d}M$

$\Rightarrow F\bar{d}\bar{d}M$

$\Rightarrow F\bar{d}\bar{d}\bar{d}$

$\Rightarrow -\bar{d}\bar{d}\bar{d}$

# Some derivations

$$I \Rightarrow FM$$

$$\Rightarrow FdM$$

$$\Rightarrow FddM$$

$$\Rightarrow Fddd$$

$$\Rightarrow -ddd$$

$$I \Rightarrow FM$$

$$\Rightarrow FdM$$

$$\Rightarrow Fdd$$

$$\Rightarrow dd$$

# Some derivations

$$I \Rightarrow FM$$

$$\Rightarrow F\bar{d}M$$

$$\Rightarrow F\bar{d}\bar{d}M$$

$$\Rightarrow F\bar{d}\bar{d}\bar{d}$$

$$\Rightarrow -\bar{d}\bar{d}\bar{d}$$

$$I \Rightarrow FM$$

$$\Rightarrow F\bar{d}M$$

$$\Rightarrow F\bar{d}\bar{d}$$

$$\Rightarrow \bar{d}\bar{d}$$

$$I \Rightarrow FM$$

$$\Rightarrow F\bar{d}M$$

$$\Rightarrow F\bar{d}\bar{d}M$$

$$\Rightarrow F\bar{d}\bar{d}\bar{d}M$$

$$\Rightarrow F\bar{d}\bar{d}\bar{d}\bar{d}$$

$$\Rightarrow +\bar{d}\bar{d}\bar{d}\bar{d}$$

## Grammars

- Context-free
  - ▶ A single nonterminal on the left side of every production rule
- Context-sensitive
  - ▶ Not context-free

$$N = \{ A , B , C \}$$

$$T = \{ a , b , c \}$$

$P$  = the productions

$$1. A \rightarrow aABC$$

$$2. A \rightarrow abC$$

$$3. CB \rightarrow BC$$

$$4. bB \rightarrow bb$$

$$5. bC \rightarrow bc$$

$$6. cC \rightarrow cc$$

$$S = A$$

## A

[illegible]

## A derivation

$A \Rightarrow aABC$

Rule 1

⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮

# A derivation

$$A \Rightarrow aABC$$

Rule 1

$$\Rightarrow aaABCBC$$

Rule 1

⋮

⋮

⋮

⋮

⋮

⋮

⋮

⋮

⋮



# A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2

⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮  
⋮

# A derivation

$$A \Rightarrow aABC$$

## Rule 1

$$\Rightarrow aaABCBC$$

## Rule 1

$\Rightarrow$  aaabCBCBC

## Rule 2

$\Rightarrow$  aaabBCCBC

## Rule 3

11

:

1

1

1

1

1

# A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3

⋮  
⋮  
⋮  
⋮  
⋮  
⋮

## A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3
$\Rightarrow aaabBBCCC$	Rule 3

⋮  
⋮  
⋮  
⋮  
⋮

# A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3
$\Rightarrow aaabBBCCC$	Rule 3
$\Rightarrow aaabbBCC$	Rule 4

⋮  
⋮  
⋮  
⋮  
⋮

## A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3
$\Rightarrow aaabBBCCC$	Rule 3
$\Rightarrow aaabbBCCC$	Rule 4
$\Rightarrow aaabbbbCCC$	Rule 4

⋮  
⋮  
⋮

# A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3
$\Rightarrow aaabBBCCC$	Rule 3
$\Rightarrow aaabbBCCC$	Rule 4
$\Rightarrow aaabbbbCCC$	Rule 4
$\Rightarrow aaabbbbcCC$	Rule 5

:

:

# A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3
$\Rightarrow aaabBBCCC$	Rule 3
$\Rightarrow aaabbBCCC$	Rule 4
$\Rightarrow aaabbbCCC$	Rule 4
$\Rightarrow aaabbbccCC$	Rule 5
$\Rightarrow aaabbbccC$	Rule 6



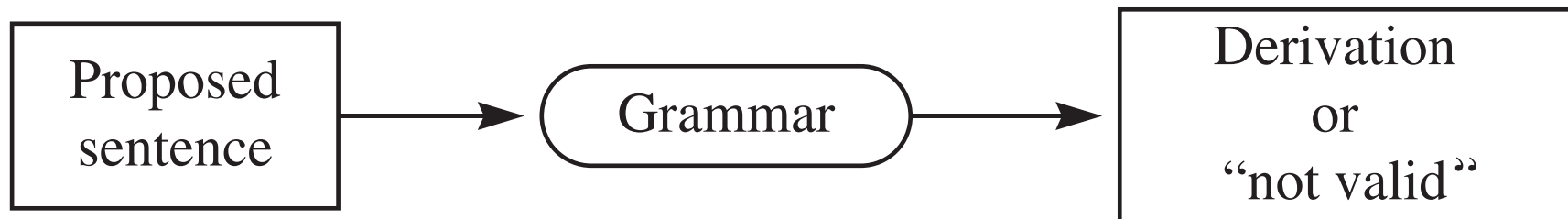
# A derivation

$A \Rightarrow aABC$	Rule 1
$\Rightarrow aaABCBC$	Rule 1
$\Rightarrow aaabCBCBC$	Rule 2
$\Rightarrow aaabBCCBC$	Rule 3
$\Rightarrow aaabBCBCC$	Rule 3
$\Rightarrow aaabBBCCC$	Rule 3
$\Rightarrow aaabbBCCC$	Rule 4
$\Rightarrow aaabbbCCC$	Rule 4
$\Rightarrow aaabbbccCC$	Rule 5
$\Rightarrow aaabbbcccC$	Rule 6
$\Rightarrow aaabbbcccc$	Rule 6

# The parsing problem



(a) Deriving a valid sentence.



(b) The parsing problem.

$$N = \{ E, T, F \}$$

$$T = \{ +, *, (, ), a \}$$

$P$  = the productions

$$1. E \rightarrow E + T$$

$$2. E \rightarrow T$$

$$3. T \rightarrow T * F$$

$$4. T \rightarrow F$$

$$5. F \rightarrow ( E )$$

$$6. F \rightarrow a$$

$$S = E$$

Parse ( a \* a ) + a  
E

Parse ( a \* a ) + a

$E \Rightarrow E + T$

Rule 1

Parse ( a \* a ) + a

$$\begin{aligned} E &\Rightarrow E + T \\ &\Rightarrow T + T \end{aligned}$$

Rule 1

Rule 2

## Parse ( a \* a ) + a

$E \Rightarrow E + T$

Rule 1

$\Rightarrow T + T$

Rule 2

$\Rightarrow F + T$

Rule 4

## Parse ( a \* a ) + a

$E \Rightarrow E + T$

Rule 1

$\Rightarrow T + T$

Rule 2

$\Rightarrow F + T$

Rule 4

$\Rightarrow ( E ) + T$

Rule 5



## Parse ( a \* a ) + a

$E \Rightarrow E + T$

Rule 1

$\Rightarrow T + T$

Rule 2

$\Rightarrow F + T$

Rule 4

$\Rightarrow ( E ) + T$

Rule 5

$\Rightarrow ( T ) + T$

Rule 2

## Parse ( a \* a ) + a

$E \Rightarrow E + T$

Rule 1

$\Rightarrow T + T$

Rule 2

$\Rightarrow F + T$

Rule 4

$\Rightarrow ( E ) + T$

Rule 5

$\Rightarrow ( T ) + T$

Rule 2

$\Rightarrow ( T * F ) + T$

Rule 3

## Parse ( a \* a ) + a

$E \Rightarrow E + T$

Rule 1

$\Rightarrow T + T$

Rule 2

$\Rightarrow F + T$

Rule 4

$\Rightarrow ( E ) + T$

Rule 5

$\Rightarrow ( T ) + T$

Rule 2

$\Rightarrow ( T * F ) + T$

Rule 3

$\Rightarrow ( F * F ) + T$

Rule 4

## Parse ( a \* a ) + a

$E \Rightarrow E + T$	Rule 1
$\Rightarrow T + T$	Rule 2
$\Rightarrow F + T$	Rule 4
$\Rightarrow ( E ) + T$	Rule 5
$\Rightarrow ( T ) + T$	Rule 2
$\Rightarrow ( T * F ) + T$	Rule 3
$\Rightarrow ( F * F ) + T$	Rule 4
$\Rightarrow ( a * F ) + T$	Rule 6

## Parse ( a \* a ) + a

$E \Rightarrow E + T$  Rule 1

$\Rightarrow T + T$  Rule 2

$\Rightarrow F + T$  Rule 4

$\Rightarrow ( E ) + T$  Rule 5

$\Rightarrow ( T ) + T$  Rule 2

$\Rightarrow ( T * F ) + T$  Rule 3

$\Rightarrow ( F * F ) + T$  Rule 4

$\Rightarrow ( a * F ) + T$  Rule 6

$\Rightarrow ( a * a ) + T$  Rule 6

## Parse ( a \* a ) + a

$E \Rightarrow E + T$  Rule 1

$\Rightarrow T + T$  Rule 2

$\Rightarrow F + T$  Rule 4

$\Rightarrow ( E ) + T$  Rule 5

$\Rightarrow ( T ) + T$  Rule 2

$\Rightarrow ( T * F ) + T$  Rule 3

$\Rightarrow ( F * F ) + T$  Rule 4

$\Rightarrow ( a * F ) + T$  Rule 6

$\Rightarrow ( a * a ) + T$  Rule 6

$\Rightarrow ( a * a ) + F$  Rule 4

## Parse ( a \* a ) + a

$E \Rightarrow E + T$  Rule 1

$\Rightarrow T + T$  Rule 2

$\Rightarrow F + T$  Rule 4

$\Rightarrow ( E ) + T$  Rule 5

$\Rightarrow ( T ) + T$  Rule 2

$\Rightarrow ( T * F ) + T$  Rule 3

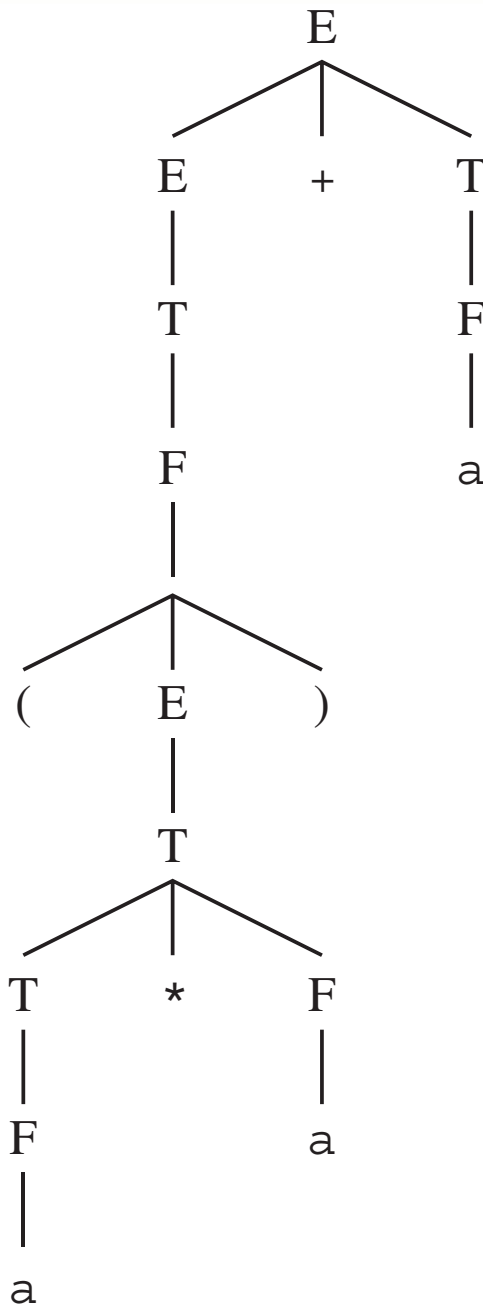
$\Rightarrow ( F * F ) + T$  Rule 4

$\Rightarrow ( a * F ) + T$  Rule 6

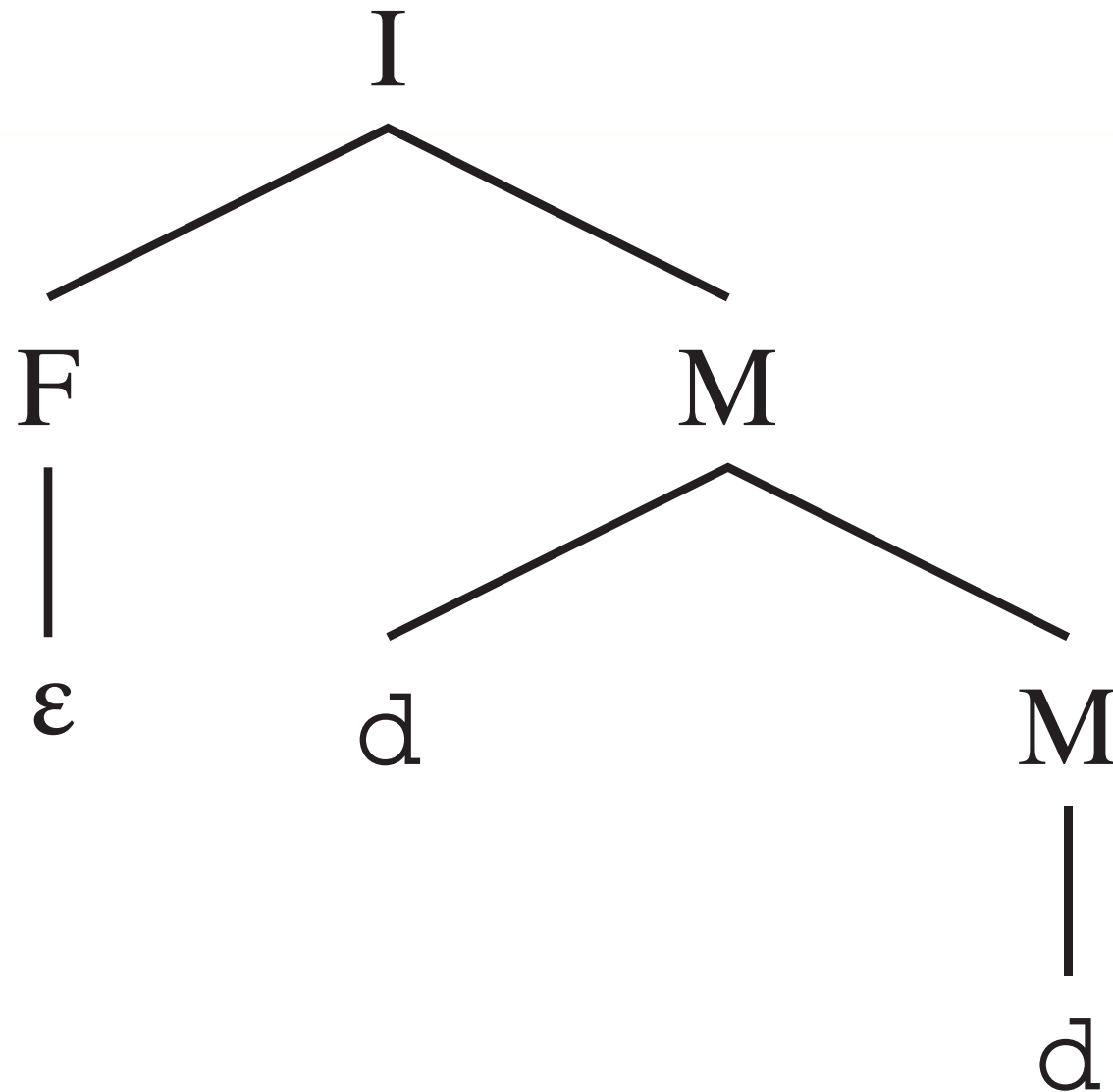
$\Rightarrow ( a * a ) + T$  Rule 6

$\Rightarrow ( a * a ) + F$  Rule 4

$\Rightarrow ( a * a ) + a$  Rule 6







`<translation-unit> →`  
    `<external-declaration>`  
    | `<translation-unit> <external-declaration>`

`<external-declaration> →`  
    `<function-definition>`  
    | `<declaration>`

`<function-definition> →`  
    `<type-specifier> <identifier> ( <parameter-list> ) <compound-statement>`  
    | `<identifier> ( <parameter-list> ) <compound-statement>`

`<declaration> → <type-specifier> <declarator-list> ;`

`<type-specifier> → void | char | int`

`<declarator-list> →`  
    `<identifier>`  
    | `<declarator-list> <identifier>`

<statement> →

    <compound-statement>

    | <expression-statement>

    | <selection-statement>

    | <iteration-statement>

<expression-statement> → <expression> ;

<selection-statement> →

    if ( <expression> ) <statement>

    | if ( <expression> ) <statement> else <statement>

<iteration-statement> →

    while ( <expression> ) <statement>

    | do <statement> while ( <expression> ) ;

<expression> →

    <relational-expression>

    | <identifier> = <expression>

<declarator-list> →

    <identifier>

    | <declarator-list> <identifier>

<parameter-list> →

    €

    | <parameter-declaration>

    | <parameter-list> , <parameter-declaration>

<parameter-declaration> → <type-specifier> <identifier>

<compound-statement> → { <declaration-list> <statement-list> }

<declaration-list> →

    €

    | <declaration>

    | <declaration> <declaration-list>

<statement-list> →

    €

    | <statement>

    | <statement-list> <statement>

$\langle \text{relational-expression} \rangle \rightarrow$   
     $\langle \text{additive-expression} \rangle$   
    |  $\langle \text{relational-expression} \rangle < \langle \text{additive-expression} \rangle$   
    |  $\langle \text{relational-expression} \rangle > \langle \text{additive-expression} \rangle$   
    |  $\langle \text{relational-expression} \rangle \leq \langle \text{additive-expression} \rangle$   
    |  $\langle \text{relational-expression} \rangle \geq \langle \text{additive-expression} \rangle$

$\langle \text{additive-expression} \rangle \rightarrow$   
     $\langle \text{multiplicative-expression} \rangle$   
    |  $\langle \text{additive-expression} \rangle + \langle \text{multiplicative-expression} \rangle$   
    |  $\langle \text{additive-expression} \rangle - \langle \text{multiplicative-expression} \rangle$

$\langle \text{multiplicative-expression} \rangle \rightarrow$   
     $\langle \text{unary-expression} \rangle$   
    |  $\langle \text{multiplicative-expression} \rangle * \langle \text{unary-expression} \rangle$   
    |  $\langle \text{multiplicative-expression} \rangle / \langle \text{unary-expression} \rangle$

$\langle \text{unary-expression} \rangle \rightarrow$   
     $\langle \text{primary-expression} \rangle$   
    |  $\langle \text{identifier} \rangle ( \langle \text{argument-expression-list} \rangle )$

<primary-expression> →  
    <identifier>  
    | <constant>

<argument-expression-list> →  
    <expression>  
    | <argument-expression-list> , <expression>

<constant> →  
    <integer-constant>  
    | <character-constant>

<integer-constant> →  
    <digit>  
    | <integer-constant> <digit>

<character-constant> → ' <letter> '

<identifier> →

<letter>

| <identifier> <letter>

| <identifier> <digit>

<letter> →

a | b | c | d | e | f | g | h | i | j | k | l | m |

n | o | p | q | r | s | t | u | v | w | x | y | z |

A | B | C | D | E | F | G | H | I | J | K | L | M |

N | O | P | Q | R | S | T | U | V | W | X | Y | Z

<digit> →

0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

The following example of a parse with this grammar shows that

```
while ( a <= 9 )  
    S1;
```

is a valid <statement>, assuming that *S1* is a valid <expression>.



<statement>

⇒ <iteration-statement>

⇒ while ( <expression> ) <statement>

⇒ while ( <relational-expression> ) <statement>

⇒ while ( <relational-expression> <= <additive-expression> ) <statement>

⇒ while ( <additive-expression> <= <additive-expression> ) <statement>

⇒ while ( <multiplicative-expression> <= <additive-expression> ) <statement>

⇒ while ( <unary-expression> <= <additive-expression> ) <statement>

⇒ while ( <primary-expression> <= <additive-expression> ) <statement>

⇒ while ( <identifier> <= <additive-expression> ) <statement>

⇒ while ( <letter> <= <additive-expression> ) <statement>

⇒ while ( a <= <additive-expression> ) <statement>

⇒ while ( a <= <multiplicative-expression> ) <statement>

⇒ while ( a <= <unary-expression> ) <statement>

⇒ while ( a <= <primary-expression> ) <statement>

⇒ while ( a <= <constant> ) <statement>

⇒ while ( a <= <integer-constant> ) <statement>

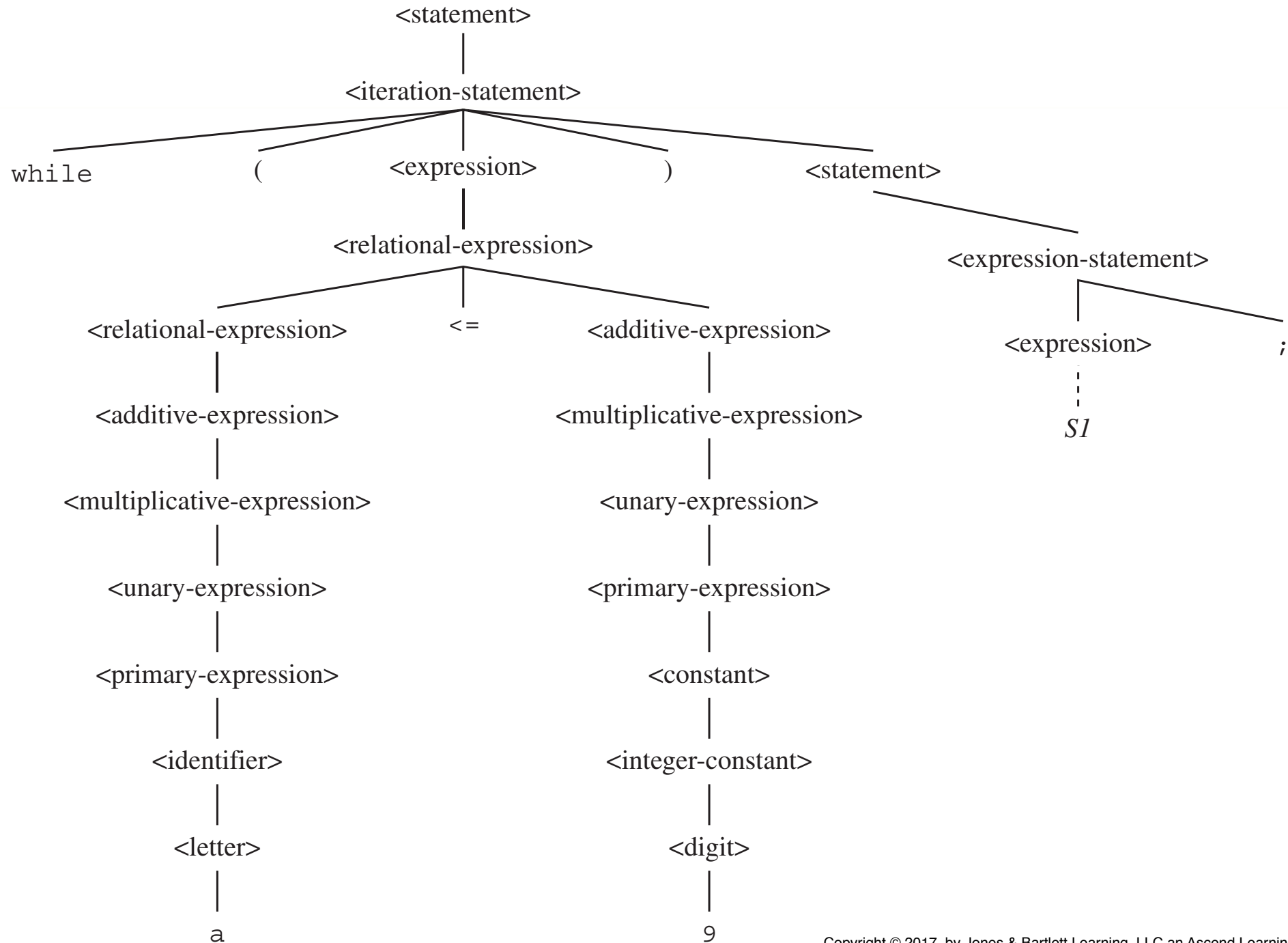
⇒ while ( a <= <digit> ) <statement>

⇒ while ( a <= 9 ) <statement>

⇒ while ( a <= 9 ) <expression-statement>

⇒ while ( a <= 9 ) <expression> ;

⇒\* while ( a <= 9 ) S1;

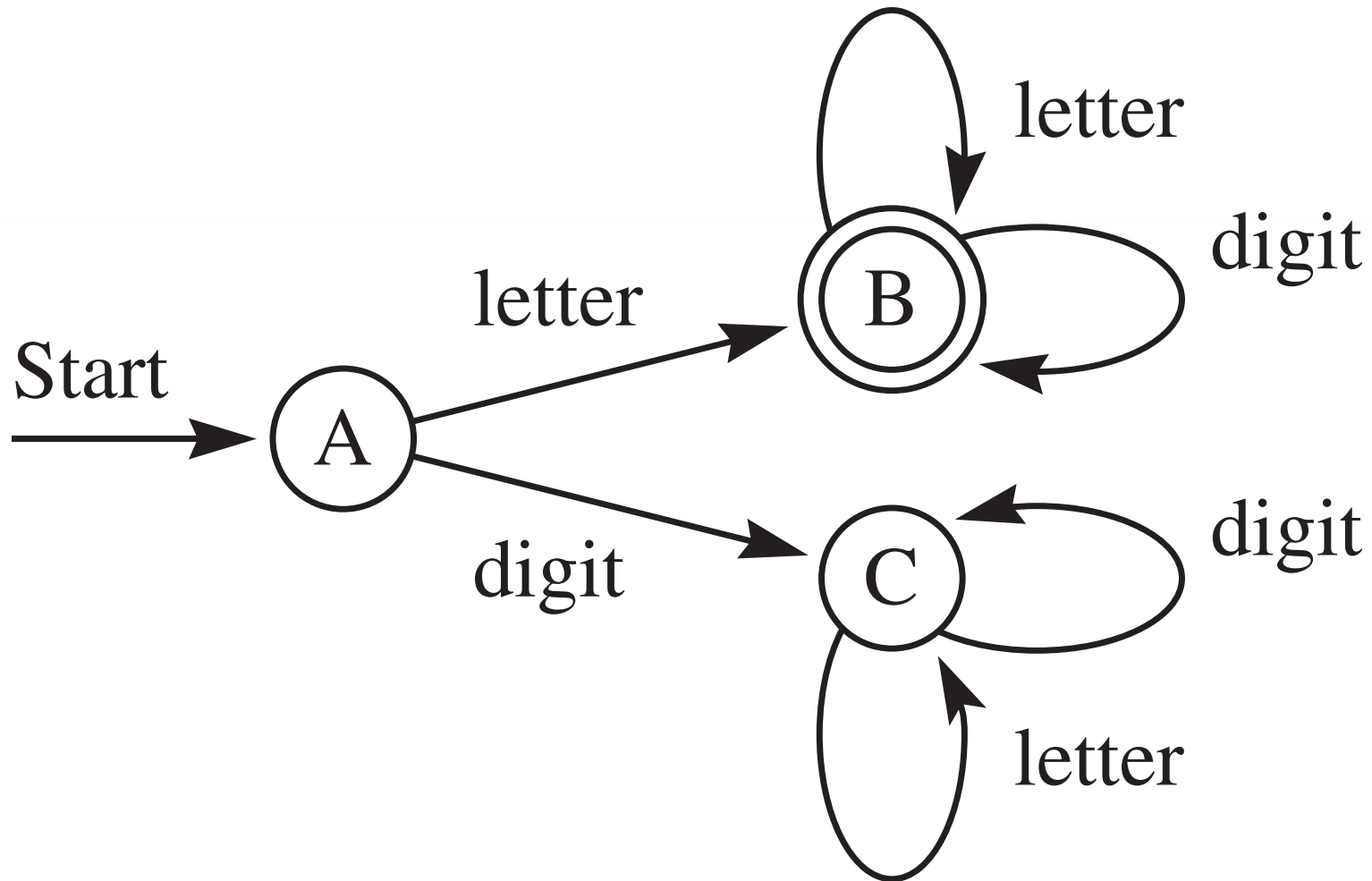


## The C language

- C has a context-free grammar.
- C is not a context-free language.

## Finite state machines

- Finite set of states called nodes represented by circles
- Transitions between states represented by directed arcs
- Each arc labeled by a terminal character
- One state designated the start state
- A nonempty set of states designated final states



## Parsing rules

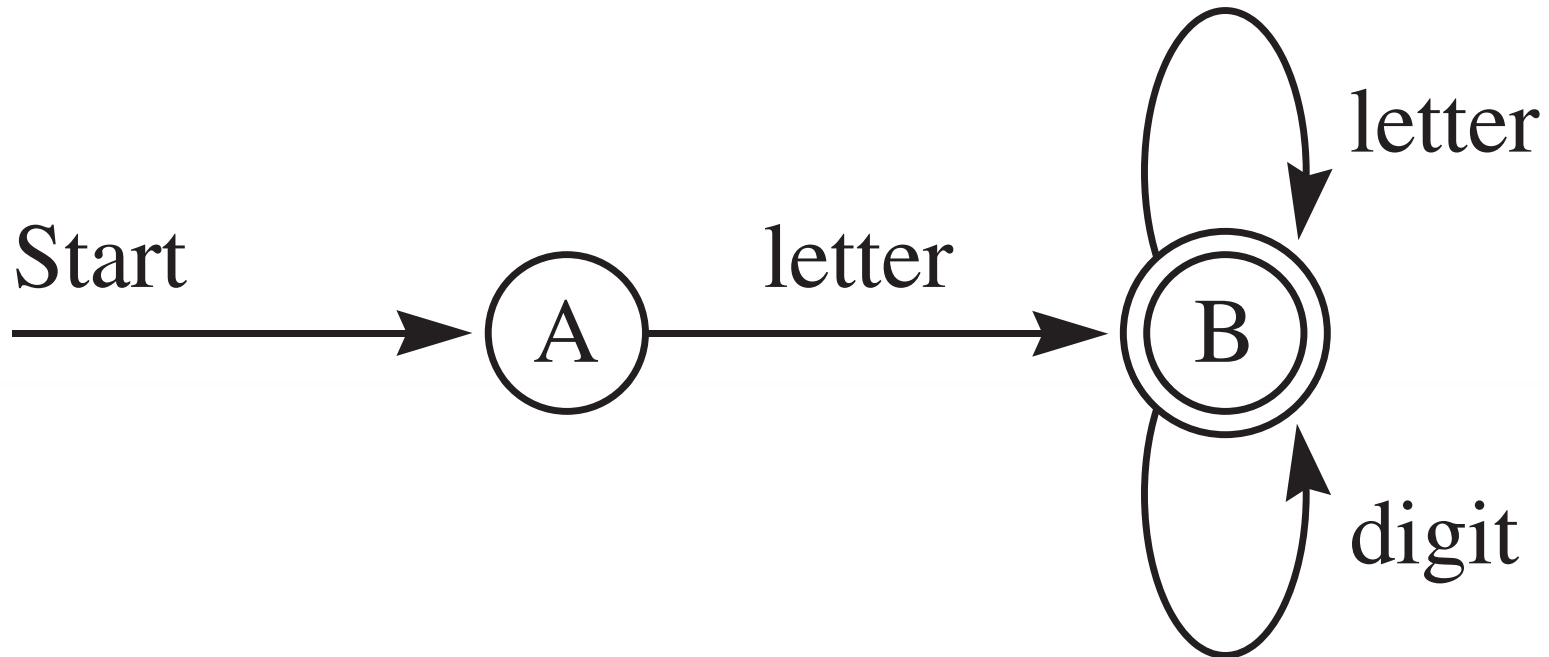
- Start at the start state
- Scan the string from left to right
- For each terminal scanned, make a transition to the next state in the FSM
- After the last terminal scanned, if you are in a final state the string is in the language
- Otherwise, it is not

Current State	Next State	
	Letter	Digit
→ A	B	C
ⓑ	B	B
C	C	C

## Simplified FSM

- Not all states have transitions on all terminal symbols
- Two ways to detect an illegal string
  - ▶ You may run out of input, and not be in a final state
  - ▶ You may be in some state, and the next input character does not correspond to any of the transitions from that state

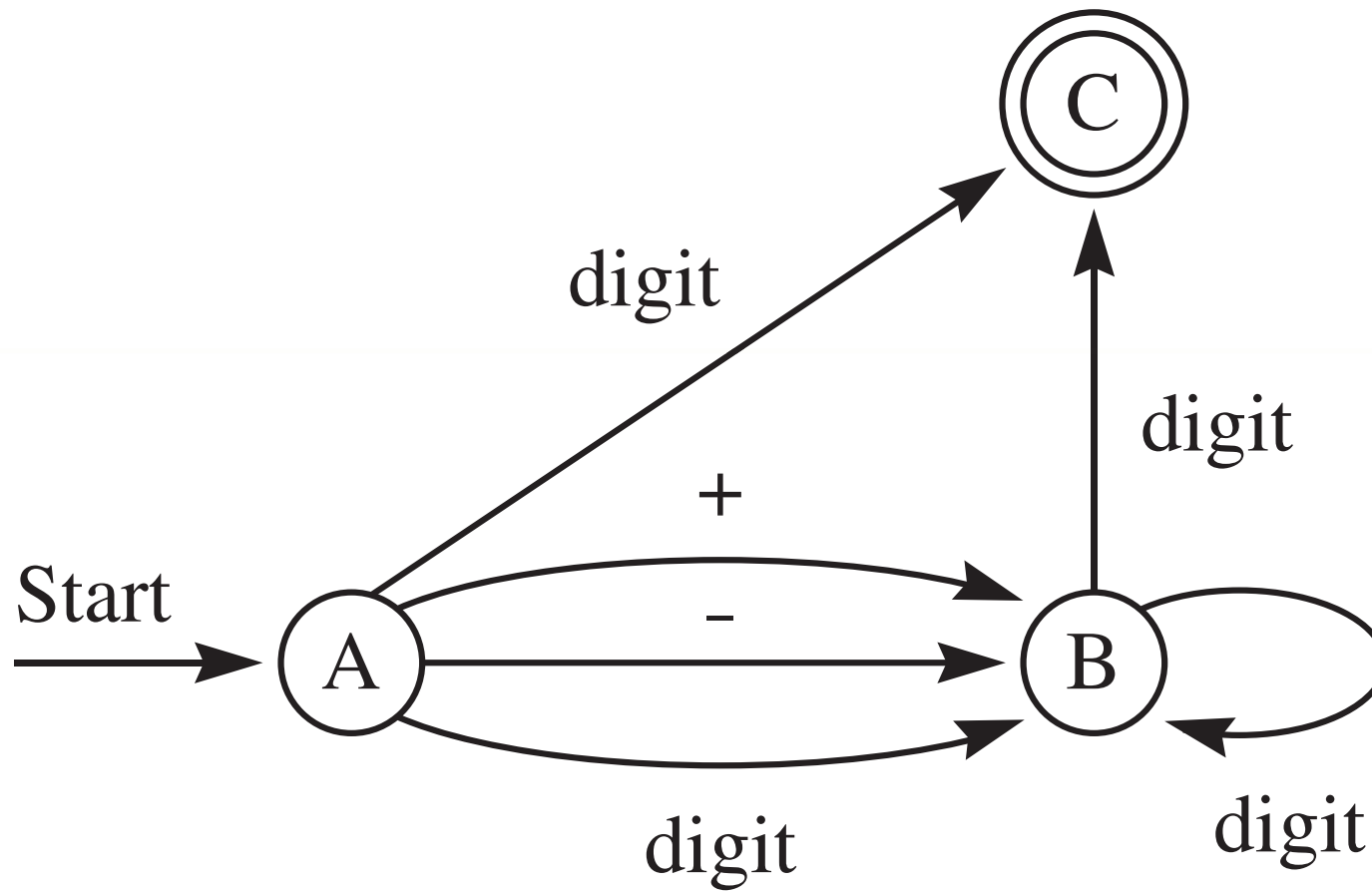




Current State	Next State	
	Letter	Digit
→ A	B	
ⓑ	B	B

## Nondeterministic FSM

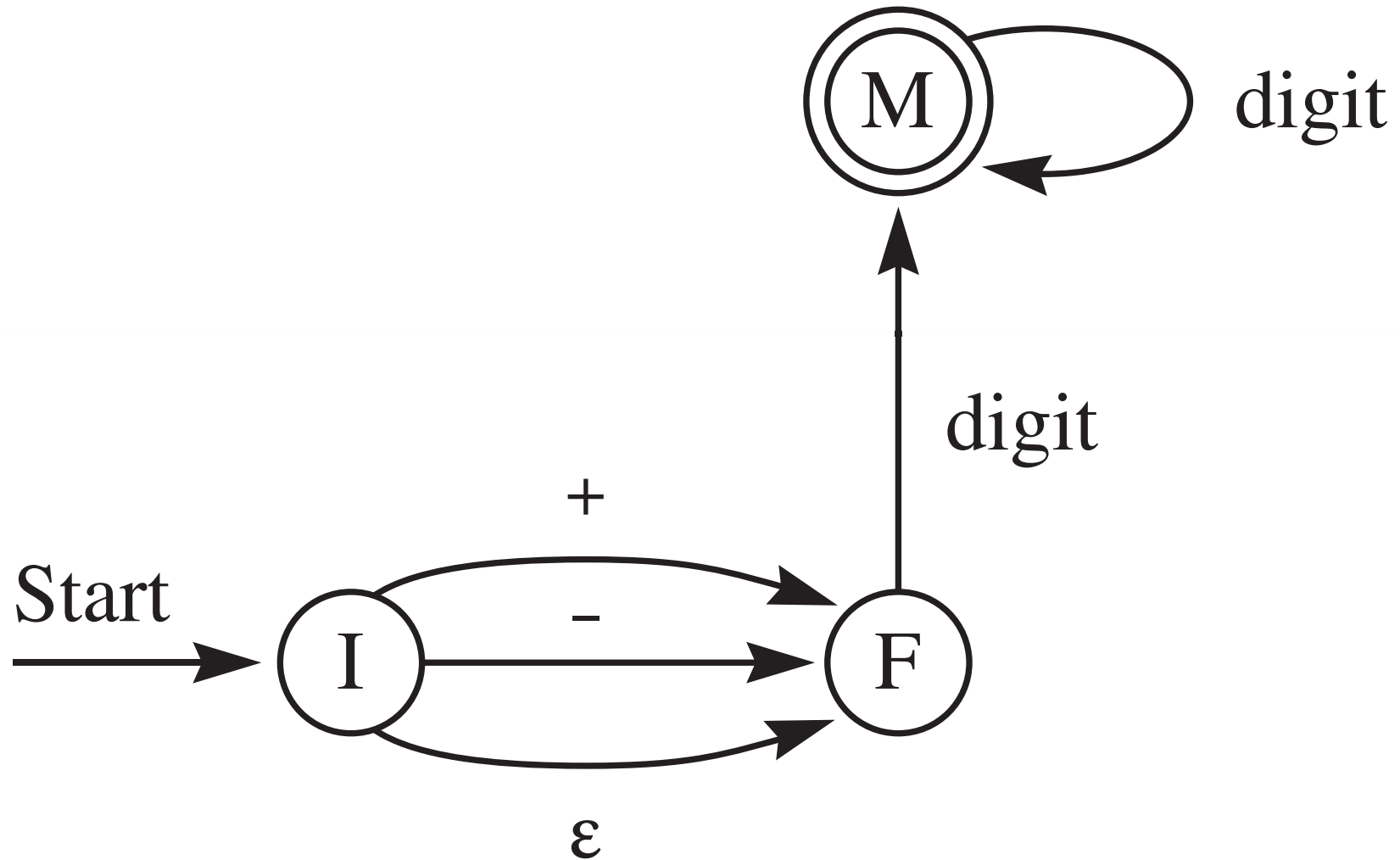
- At least one state has more than one transition from it on the same character
- If you scan the last character and you *are* in a final state, the string *is valid*
- If you scan the last character and you are *not* in a final state, the string *might be invalid*
- To prove invalid, you must try all possibilities with backtracking



Current State	Next State		
	+	-	Digit
→ A	B	B	B, C
B			B, C
©			

## Empty transitions

- An empty transition allows you to go from one state to another state without scanning a terminal character
- All finite state machines with empty transitions are considered nondeterministic

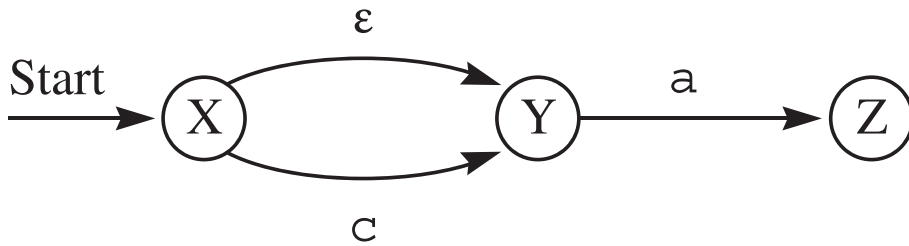


Current State	Next State			
	+	-	Digit	$\epsilon$
$\rightarrow$ I	F	F		F
F			M	
(M)			M	

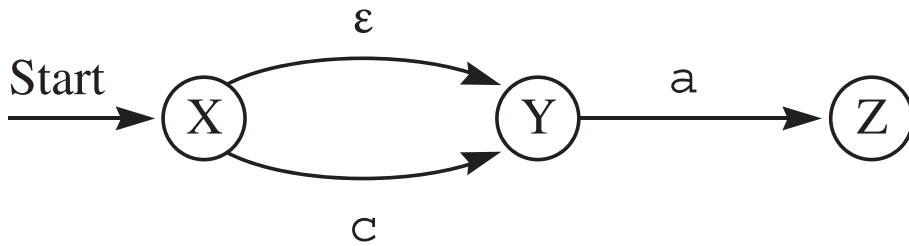


# Removing empty transitions

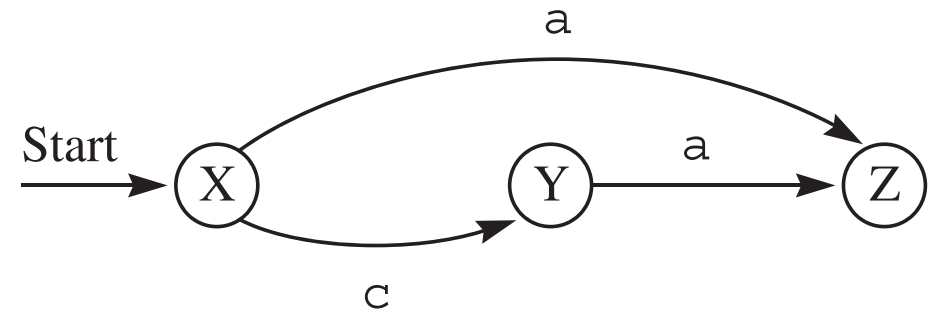
- Given a transition from  $p$  to  $q$  on  $\epsilon$ , for every transition from  $q$  to  $r$  on  $a$ , add a transition from  $p$  to  $r$  on  $a$ .
- If  $q$  is a final state, make  $p$  a final state



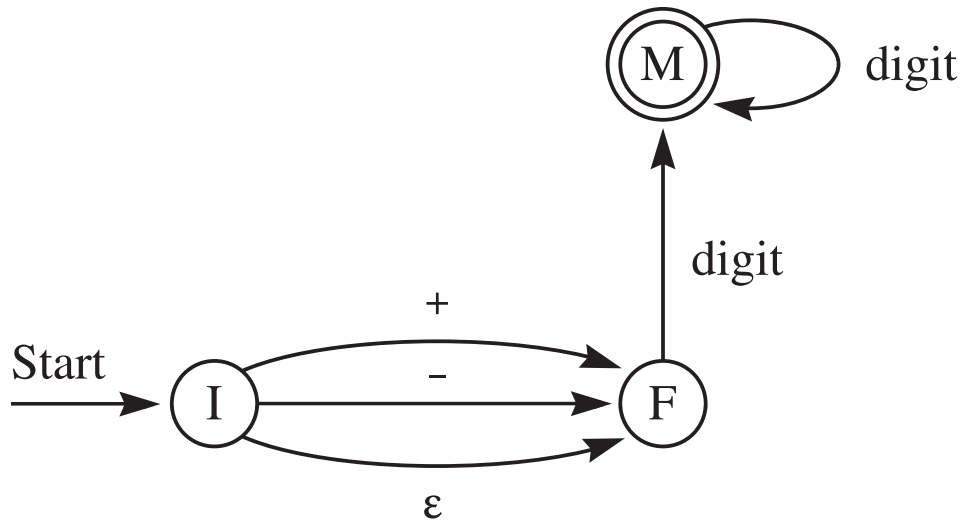
(a) The original FSM.



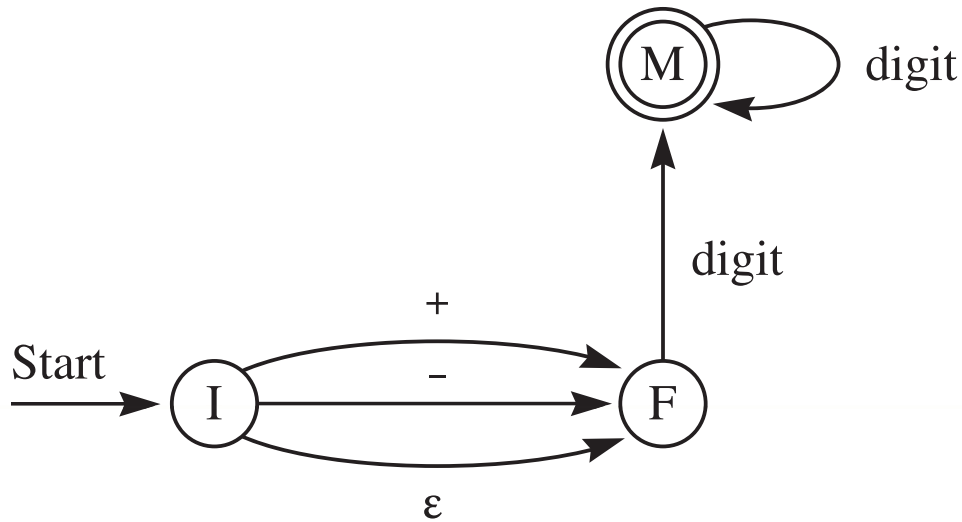
**(a)** The original FSM.



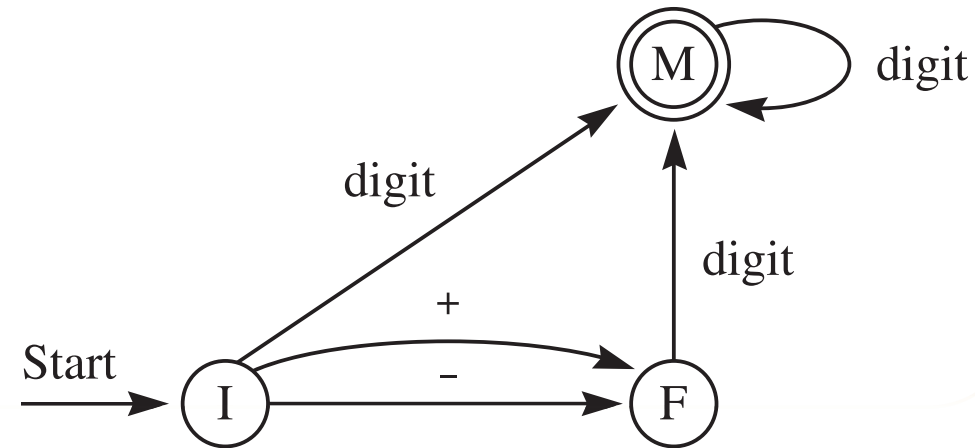
**(b)** The equivalent FSM without an empty transition.



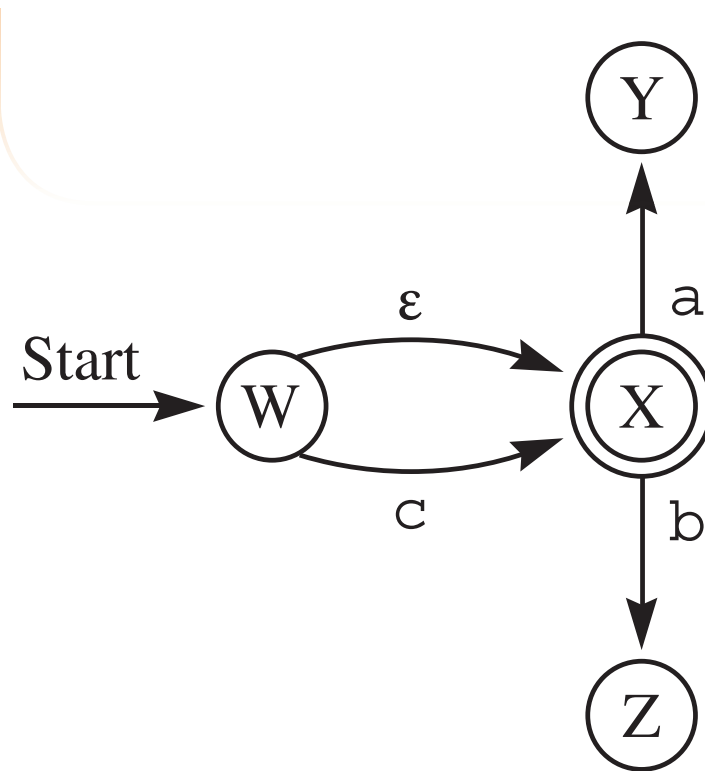
(a) The original FSM.



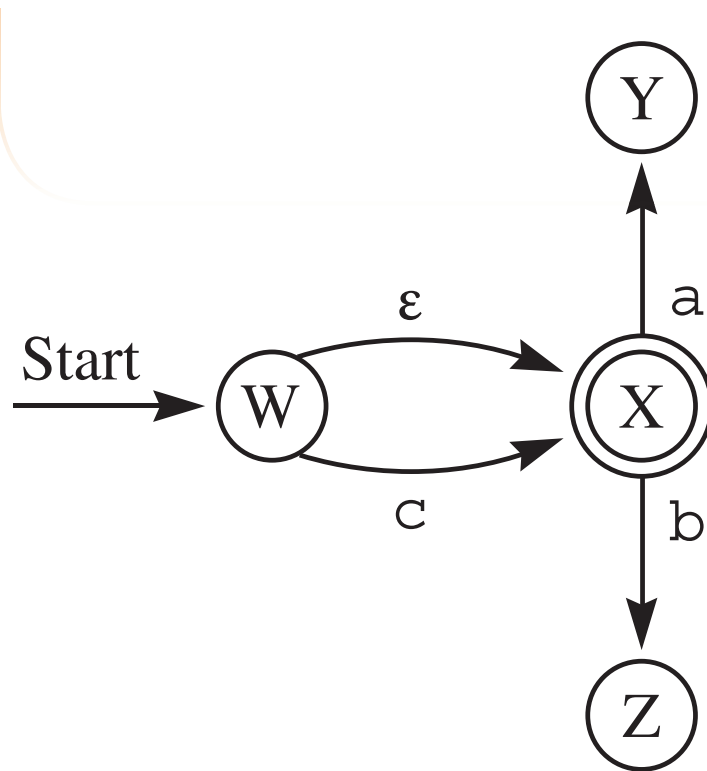
(a) The original FSM.



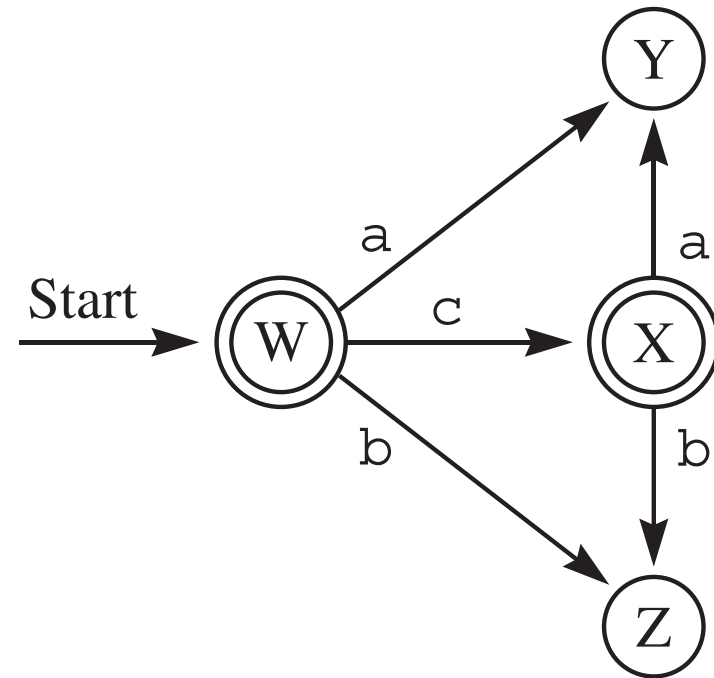
(b) The empty transition removed.



(a) The original FSM.



**(a)** The original FSM.

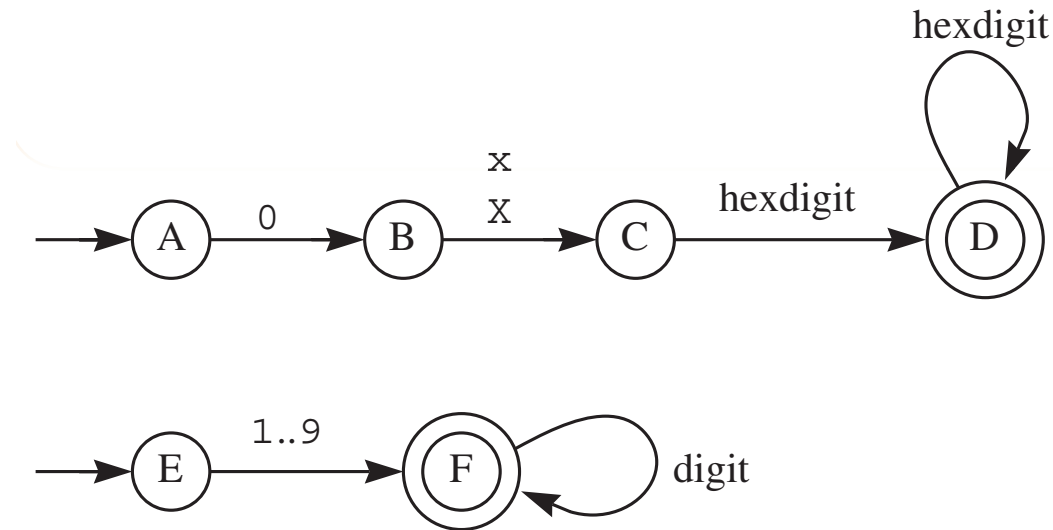


**(b)** The equivalent FSM without an empty transition.

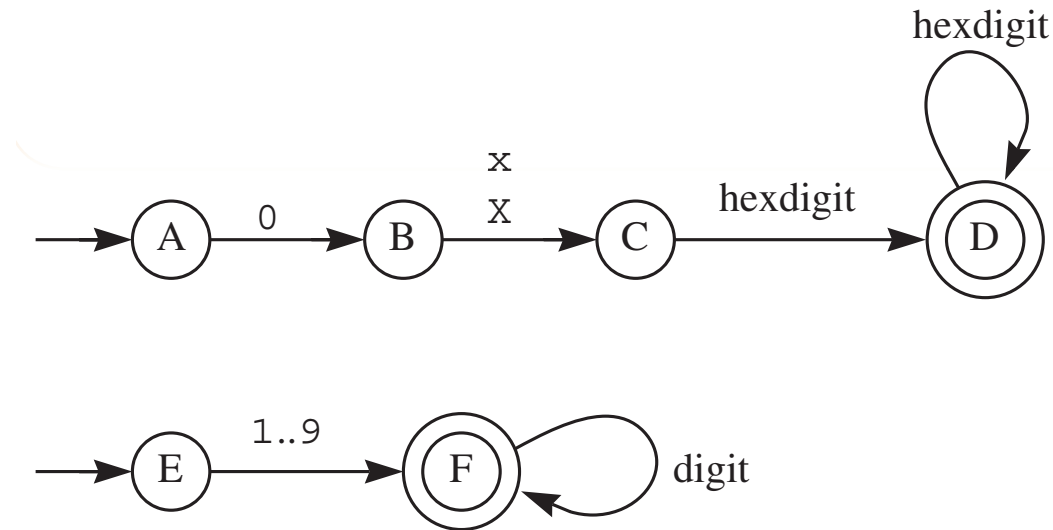
## Multiple token recognizers

- Token
  - ▶ A string of terminal characters that has meaning as a group
- FSM with multiple final states
- The final state determines the token that is recognized

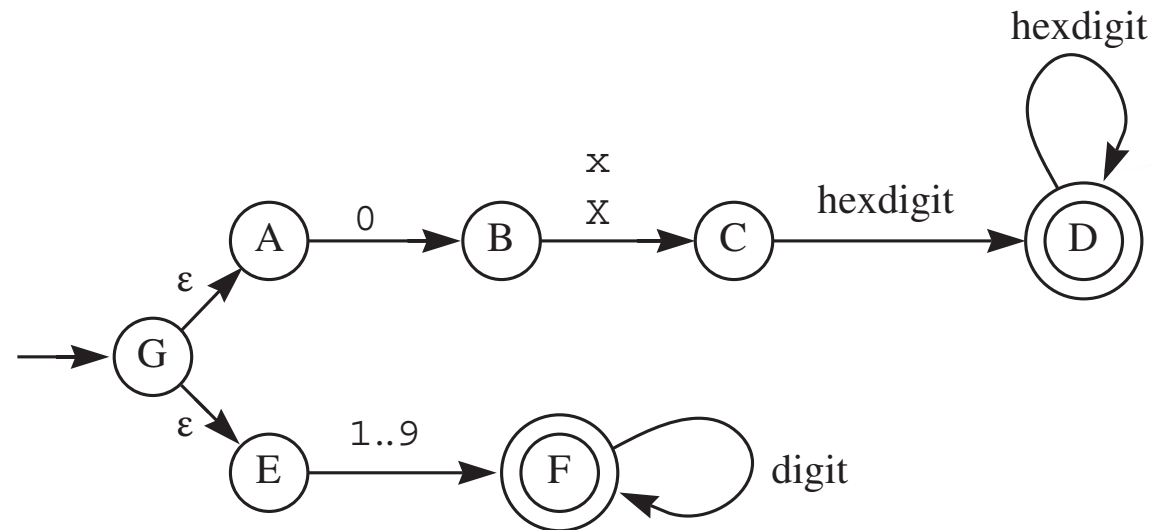




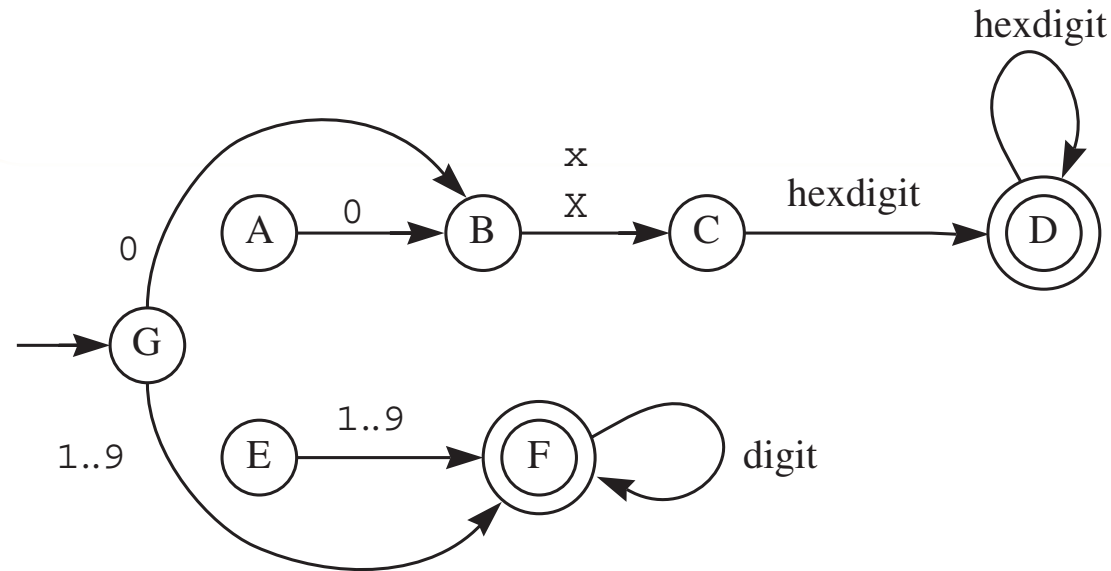
(a) Separate machines for a hexadecimal constant and an unsigned decimal integer.



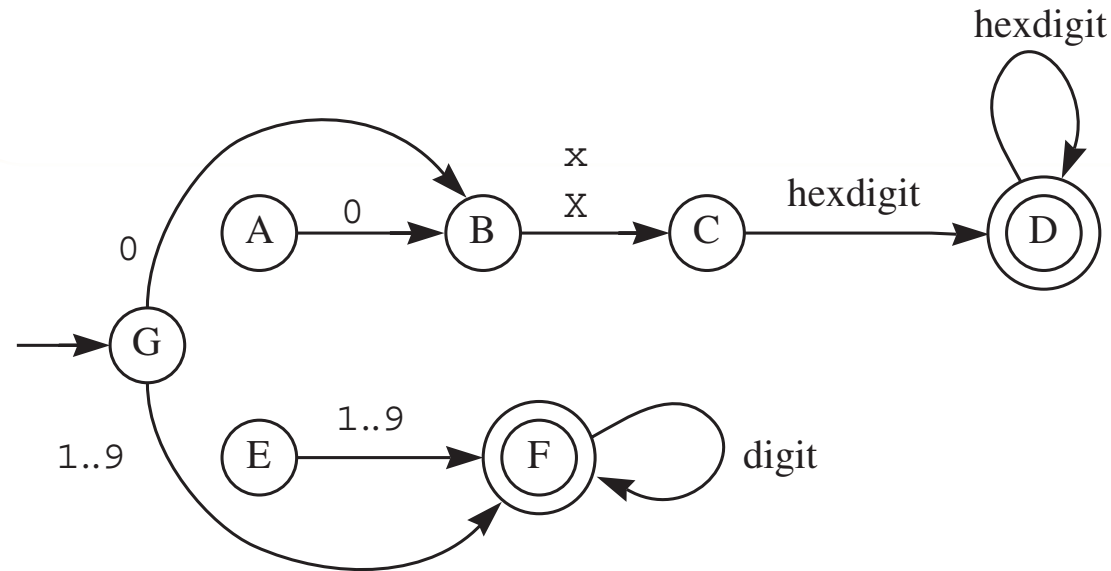
(a) Separate machines for a hexadecimal constant and an unsigned decimal integer.



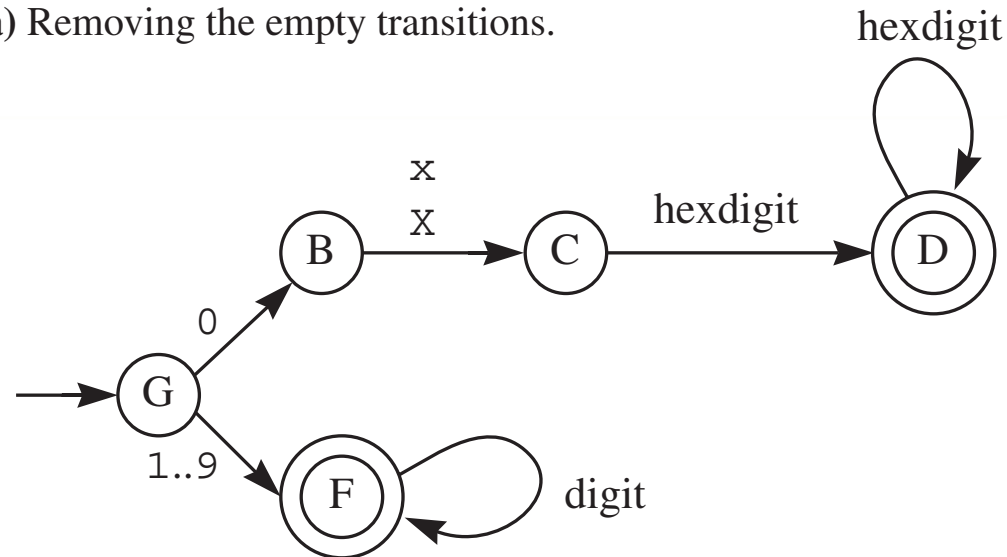
(b) One nondeterministic FSM that recognizes a hexadecimal constant or an unsigned integer token.



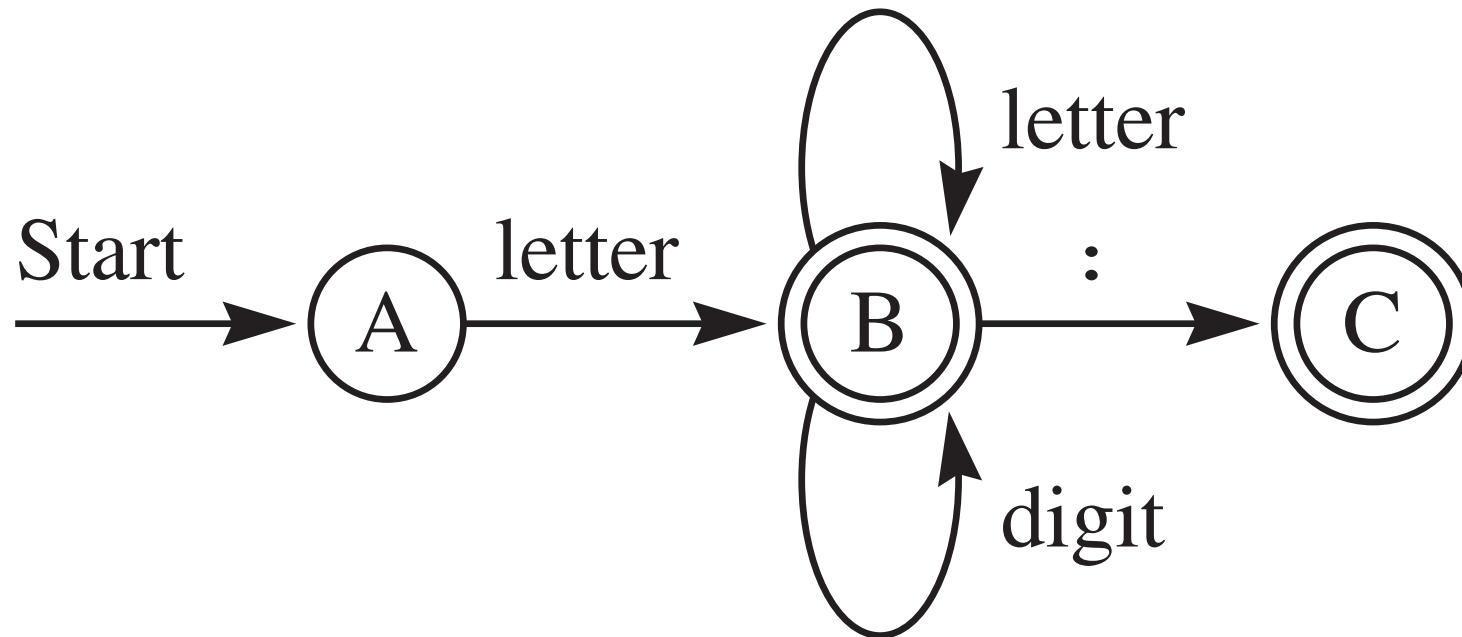
(a) Removing the empty transitions.

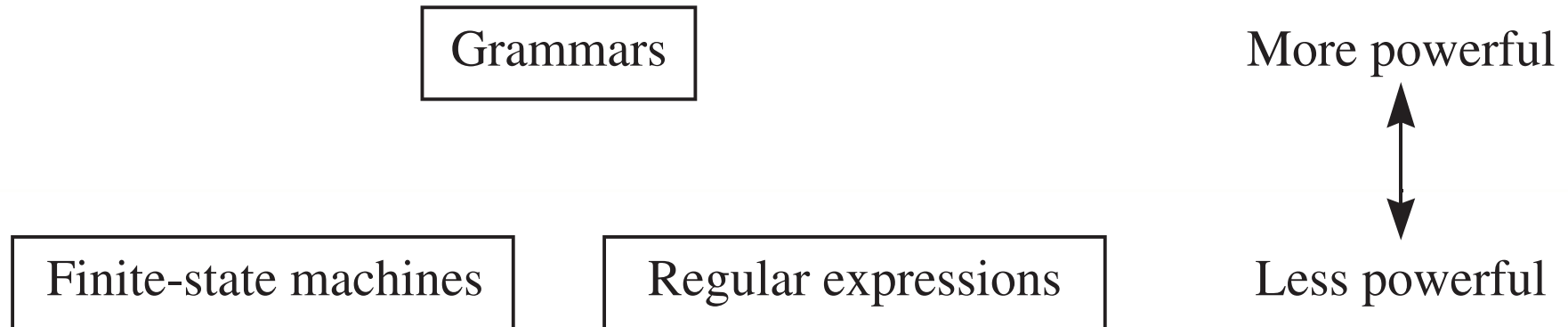


(a) Removing the empty transitions.

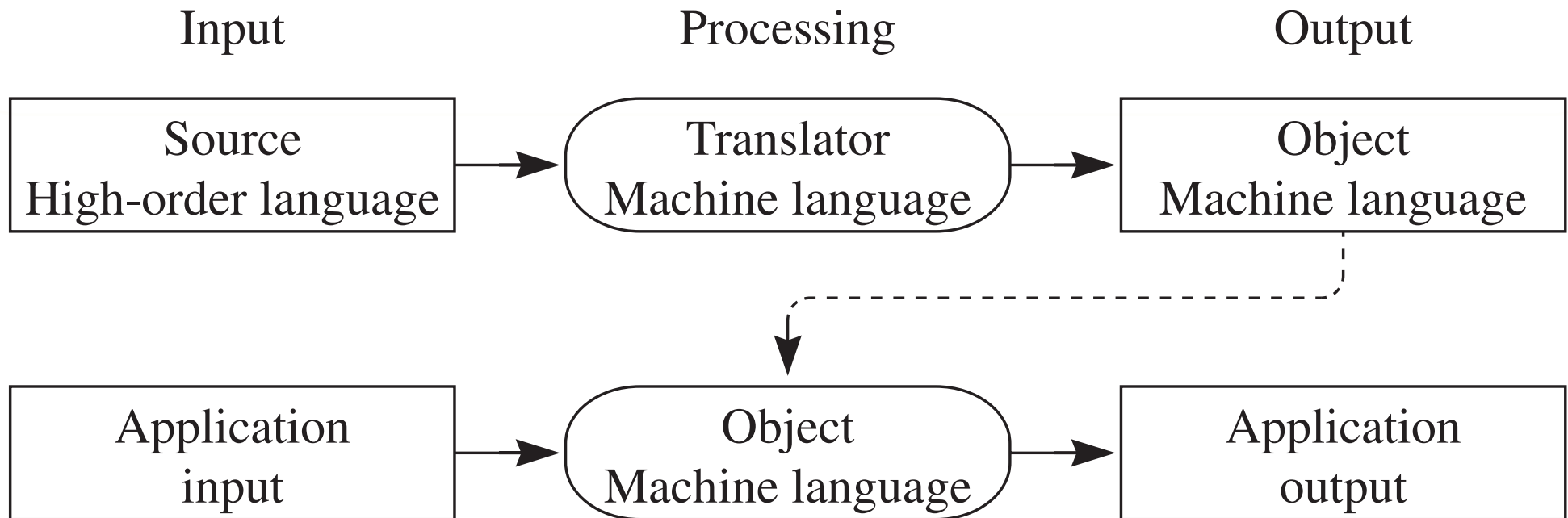


(b) Removing the inaccessible states.



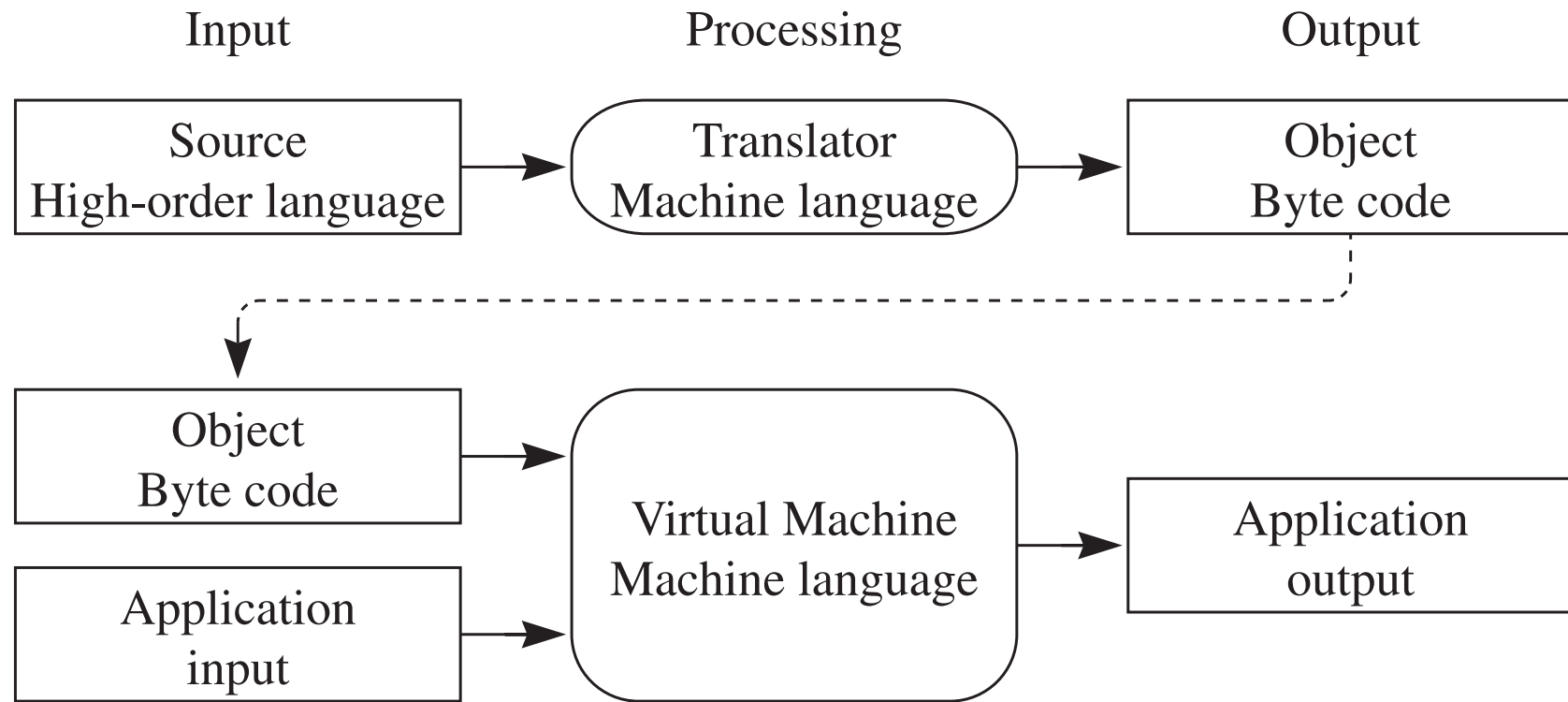


# Compilation



(a) Compilation.

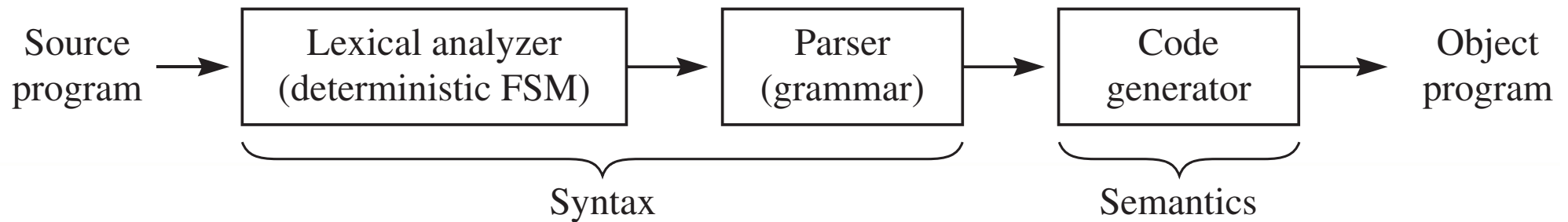
# Interpretation



(b) Interpretation.



# Stages of translation



## Stages of translation

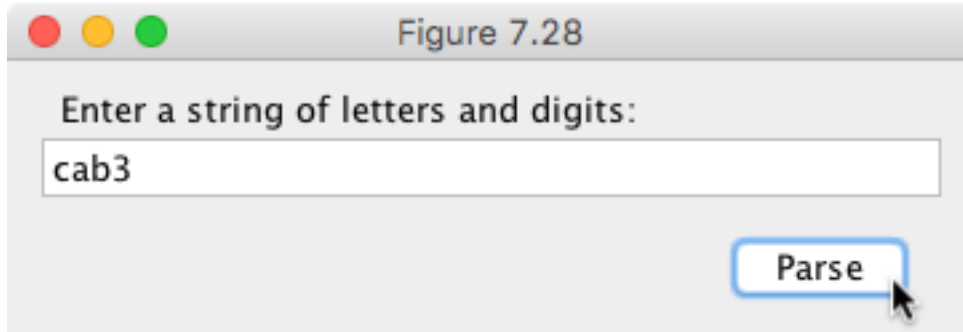
- Input of lexical analyzer – string of terminal characters
- Output of lexical analyzer and input of parser – stream of tokens
- Output of parser and input of code generator – syntax tree and/or program in low-level language
- Output of code generator – object program

# FSM implementation techniques

- Table-lookup
- Direct-code

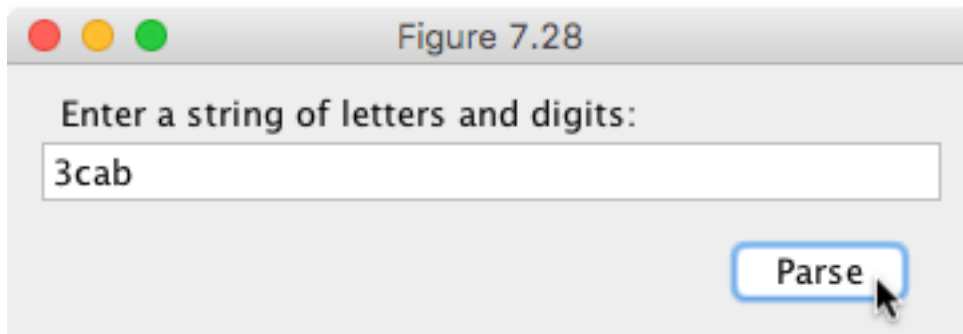
## A table-lookup implementation

Current State	Next State	
	Letter	Digit
→ A	B	C
ⓑ	B	B
C	C	C



## Console output

**cab3 is a valid identifier.**



## Console output

**3cab is not a valid identifier.**

```
package fig0728;

import java.awt.*;
import java.awt.event.*;
import javax.swing.*;

/**
 * Figure 7.28 of J Stanley Warford, <i>Computer Systems</i>, Fifth edition,
 * Jones & Bartlett, 2017.
 *
 * <p>
 * Implementation of the FSM of Figure 7.11 with the table-lookup technique.
 *
 * <p>
 * File: <code>Fig0728Main.java</code>
 *
 * @see <a href="http://computersystemsbook.com"><i>Computer Systems</i></a>
 * book home page,
 * <a href="http://www.cslab.pepperdine.edu/warford/cosc330/">course</a>
 * home page.
 * @author J. Stanley Warford
 */
```

# Javadoc

[PACKAGE](#) [CLASS](#) [TREE](#) [DEPRECATED](#) [INDEX](#) [HELP](#)

ALL CLASSES

SEARCH:

## Package fig0728

Class Summary	
Class	Description
<b>Fig0728Main</b>	Figure 7.28 of J Stanley Warford, <i>Computer Systems</i> , Fifth edition, Jones & Bartlett, 2017.

[PACKAGE](#) [CLASS](#) [TREE](#) [DEPRECATED](#) [INDEX](#) [HELP](#)

ALL CLASSES



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ALL CLASSES

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SUMMARY: [NESTED](#) | [FIELD](#) | [CONSTR](#) | [METHOD](#)    DETAIL: [FIELD](#) | [CONSTR](#) | [METHOD](#)

Package `fig0728`

## Class `Fig0728Main`

`java.lang.Object`  
    `fig0728.Fig0728Main`

All Implemented Interfaces:

`java.awt.event.ActionListener`, `java.util.EventListener`

---

```
public class Fig0728Main
  extends java.lang.Object
  implements java.awt.event.ActionListener
```

Figure 7.28 of J Stanley Warford, *Computer Systems*, Fifth edition, Jones & Bartlett, 2017.

Implementation of the FSM of Figure 7.11 with the table-lookup technique.

File: `Fig0728Main.java`

See Also:

*Computer Systems* book home page, [course](#) home page.

```
public class Fig0728Main implements ActionListener {  
  
    final JFrame mainWindowFrame;  
    final JPanel inputPanel;  
    final JLabel label;  
    final JTextField textField;  
    final JPanel buttonPanel;  
    final JButton button;
```

```
public Fig0728Main() {
    // Set up the main window.
    mainWindowFrame = new JFrame("Figure 7.28");
    mainWindowFrame.setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
    mainWindowFrame.setSize(new Dimension(240, 120));

    // Lay out the label and text field input panel from top to bottom.
    inputPanel = new JPanel();
    inputPanel.setLayout(new BoxLayout(inputPanel, BoxLayout.PAGE_AXIS));
    label = new JLabel("Enter a string of letters and digits:");
    inputPanel.add(label);
    textField = new JTextField(20);
    inputPanel.add(textField);
    inputPanel.setBorder(BorderFactory.createEmptyBorder(10, 10, 10, 10));

    // Lay out the button from left to right.
    buttonPanel = new JPanel();
    buttonPanel.setLayout(new BoxLayout(buttonPanel, BoxLayout.LINE_AXIS));
    buttonPanel.setBorder(BorderFactory.createEmptyBorder(0, 10, 10, 10));
    buttonPanel.add(Box.createHorizontalGlue());
    button = new JButton("Parse");
    buttonPanel.add(button);
    buttonPanel.add(Box.createRigidArea(new Dimension(10, 0)));
}
```

```
// Combine the input panel and the button panel in the main window.  
mainWindowFrame.add(inputPanel, BorderLayout.CENTER);  
mainWindowFrame.add(buttonPanel, BorderLayout.PAGE_END);  
  
textField.addActionListener(this);  
button.addActionListener(this);  
  
mainWindowFrame.pack();  
mainWindowFrame.setVisible(true);  
}
```

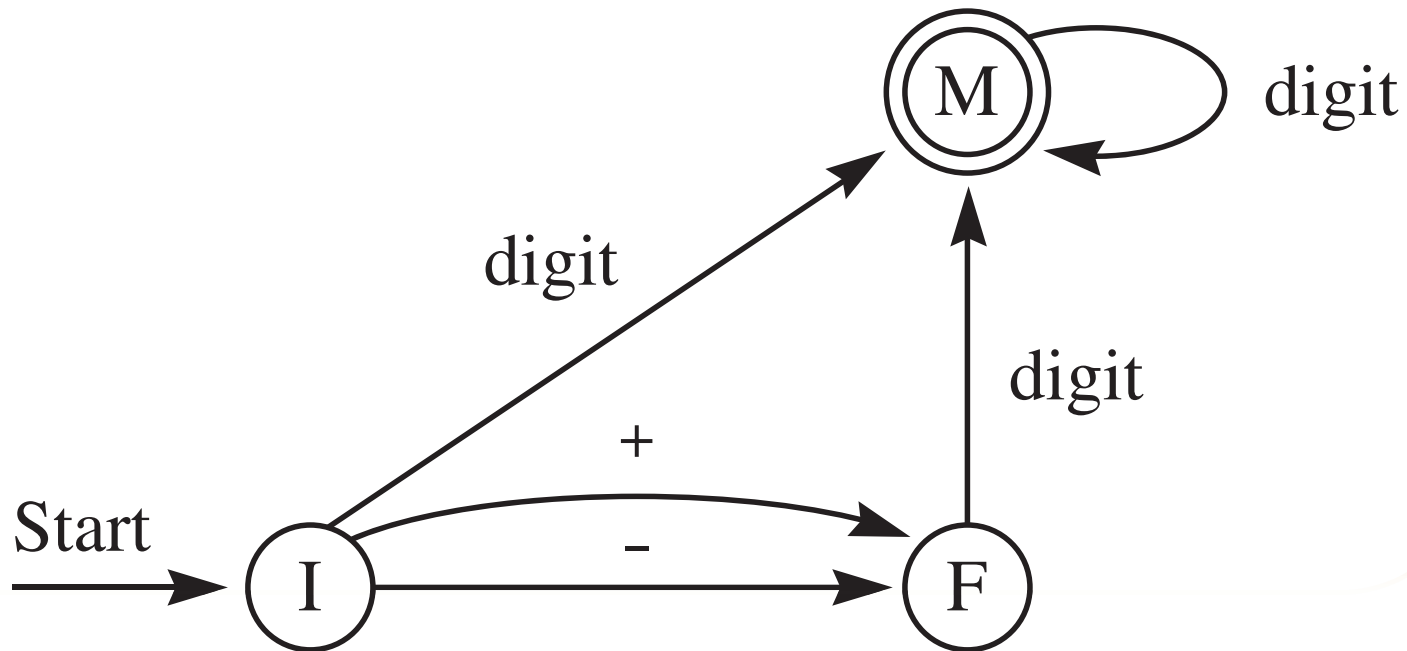
```
private static void createAndShowGUI() {  
    JFrame.setDefaultLookAndFeelDecorated(true);  
    new Fig0728Main();  
}  
  
public static void main(String[] args) {  
    javax.swing.SwingUtilities.invokeLater(Fig0728Main::createAndShowGUI);  
}
```

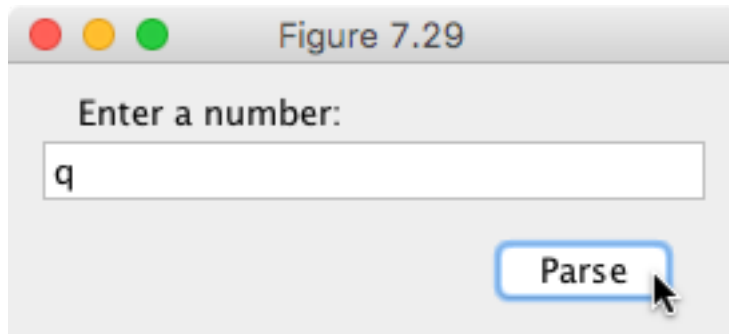
```
public static boolean isAlpha(char ch) {  
    return ('a' <= ch && ch <= 'z') || ('A' <= ch && ch <= 'Z');  
}  
// States  
static final int S_A = 0;  
static final int S_B = 1;  
static final int S_C = 2;  
// Alphabet  
static final int T_LETTER = 0;  
static final int T_DIGIT = 1;  
// State transition table  
static final int[][] FSM = {  
    {S_B, S_C},  
    {S_B, S_B},  
    {S_C, S_C}  
};
```

```
@Override
public void actionPerformed(ActionEvent event) {
    String line = textField.getText();
    char ch;
    int FSMChar;
    int state = S_A;
    for (int i = 0; i < line.length(); i++) {
        ch = line.charAt(i);
        FSMChar = isAlpha(ch) ? T_LETTER : T_DIGIT;
        state = FSM[state][FSMChar];
    }
    if (state == S_B) {
        System.out.printf("%s is a valid identifier.\n", line);
    } else {
        System.out.printf("%s is not a valid identifier.\n", line);
    }
}
}
```

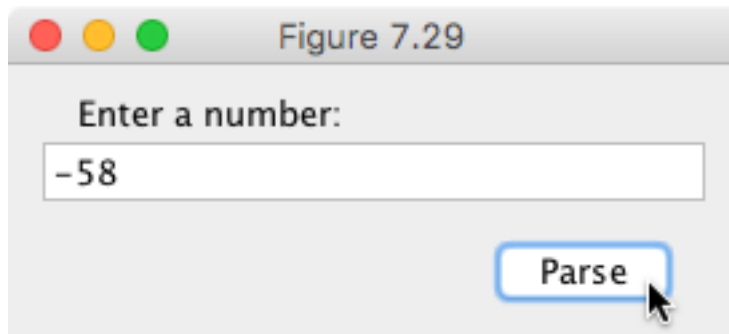
## A direct-code implementation







**Console output**  
**Invalid entry.**



**Console output**  
**Number = -58**

```
public class Fig0729Main implements ActionListener {

    final JFrame mainWindowFrame;
    final JPanel inputPanel;
    final JLabel label;
    final JTextField textField;
    final JPanel buttonPanel;
    final JButton button;

    ...

    @Override
    public void actionPerformed(ActionEvent event) {
        String line = textField.getText();
        Parser parser = new Parser();
        parser.parseNum(line);
        if (parser.isValid()) {
            System.out.printf("Number = %d\n", parser.getNumber());
        } else {
            System.out.print("Invalid entry.\n");
        }
    }
}
```

```
package fig0729;  
  
enum State {  
    S_I, S_F, S_M, S_STOP  
}
```

```
package fig0729;

public class Parser {

    private boolean valid = false;
    private int number = 0;

    public boolean getValid() {
        return valid;
    }

    public int getNumber() {
        return number;
    }

    private boolean isDigit(char ch) {
        return ('0' <= ch) && (ch <= '9');
    }
}
```

```
public void parseNum(String line) {
    line = line + '\n';
    int lineIndex = 0;
    char nextChar;
    int sign = +1;
    valid = true;
    State state = State.S_I;
    do {
        nextChar = line.charAt(lineIndex++);
        switch (state) {
            case S_I:
                if (nextChar == '+') {
                    sign = +1;
                    state = State.S_F;
                } else if (nextChar == '-') {
                    sign = -1;
                    state = State.S_F;
                } else if (isDigit(nextChar)) {
                    sign = +1;
                    number = nextChar - '0';
                    state = State.S_M;
                } else {
                    valid = false;
                }
            break;
        }
    }
```

```
case S_F:
    if (isDigit(nextChar)) {
        number = nextChar - '0';
        state = State.S_M;
    } else {
        valid = false;
    }
    break;
case S_M:
    if (isDigit(nextChar)) {
        number = 10 * number + nextChar - '0';
    } else if (nextChar == '\n') {
        number = sign * number;
        state = State.S_STOP;
    } else {
        valid = false;
    }
    break;
```

```
    }
} while ((state != State.S_STOP) && valid);
```

```
}
```

```
}
```

## An input buffer

- Used to process one character at a time from a Java String as if from an input stream
- Provides a special feature needed by multiple-token parsers
- Ability to back up a character into the input stream after being scanned



```
public class InBuffer {  
  
    private String inString;  
    private String line;  
    private int lineIndex;  
  
    public InBuffer(String string) {  
        inString = string + "\n\n";  
        // To guarantee inString.length() == 0 eventually  
    }  
}
```

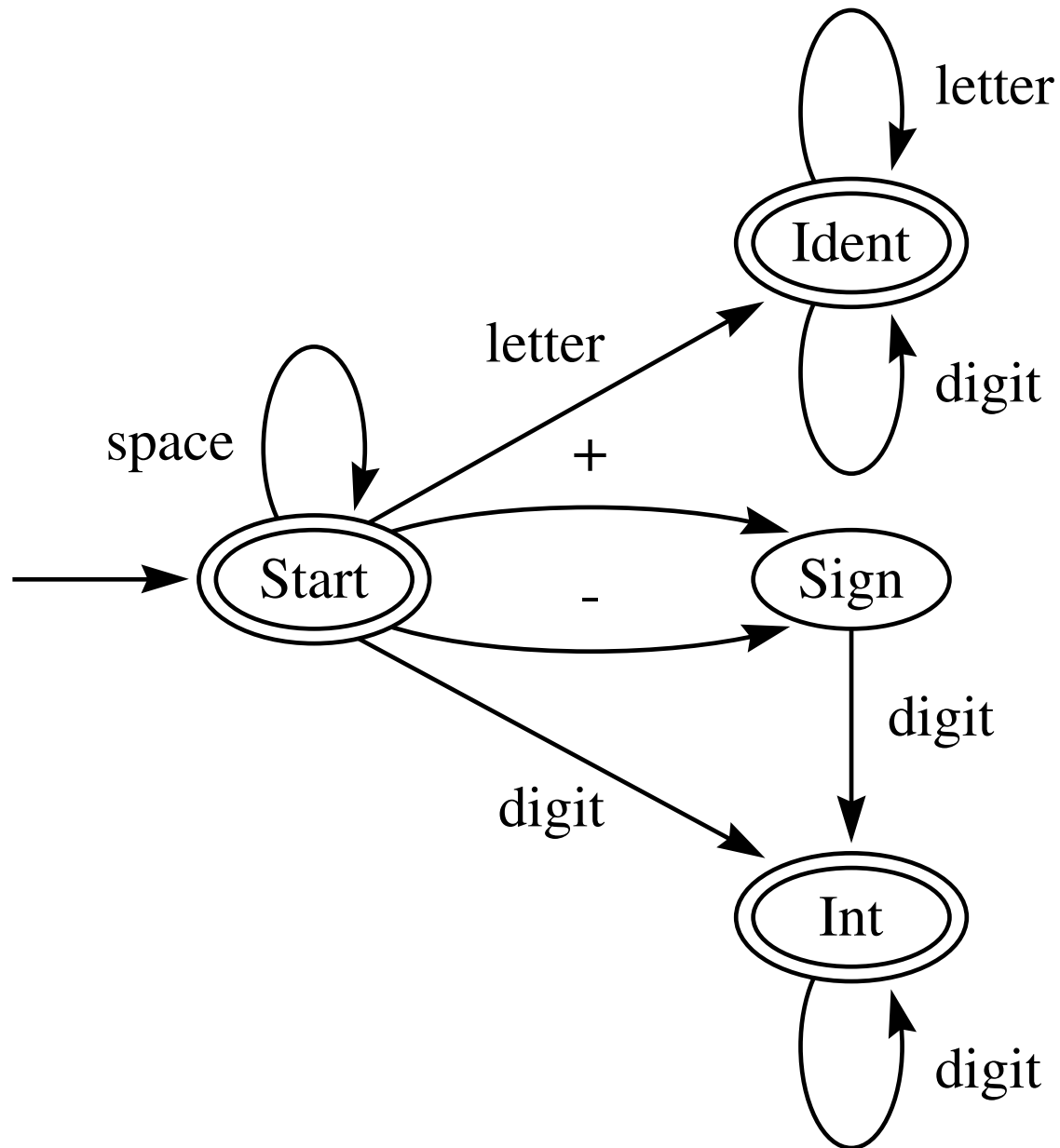
```
public void getLine() {
    int i = inString.indexOf('\n');
    line = inString.substring(0, i + 1);
    inString = inString.substring(i + 1);
    lineIndex = 0;
}

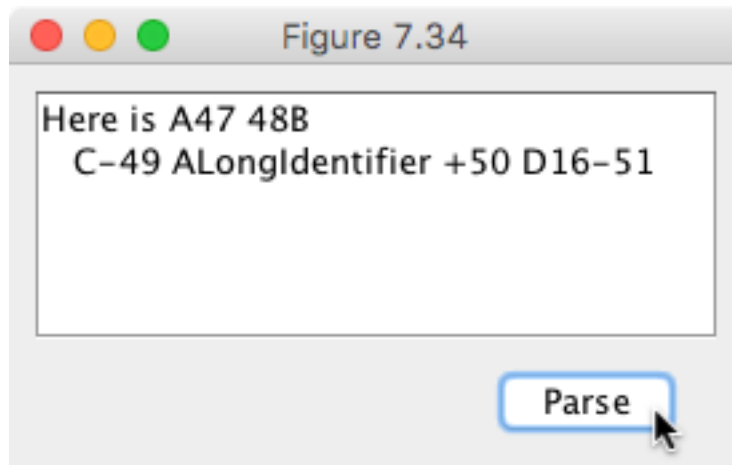
public boolean inputRemains() {
    return inString.length() != 0;
}

public char advanceInput() {
    return line.charAt(lineIndex++);
}

public void backUpInput() {
    lineIndex--;
}
}
```

## A multiple-token parser





## Console output

**Identifier = Here**

**Identifier = is**

**Identifier = A47**

**Integer = 48**

**Identifier = B**

**Empty token**

**Identifier = C**

**Integer = -49**

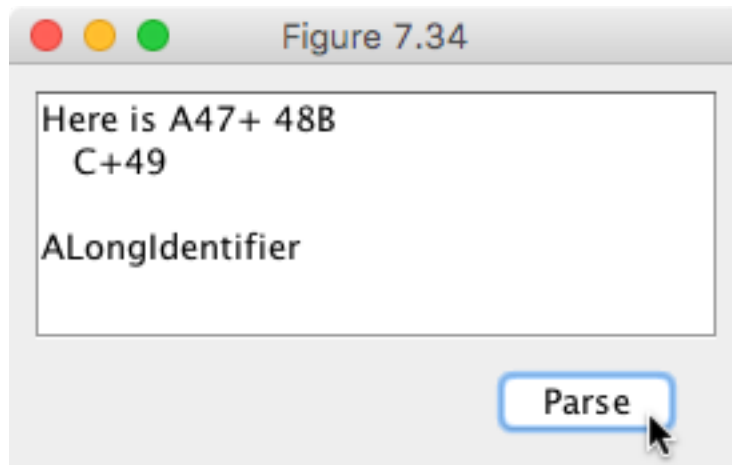
**Identifier = ALongIdentifier**

**Integer = 50**

**Identifier = D16**

**Integer = -51**

**Empty token**



## Console output

**Identifier = Here**

**Identifier = is**

**Identifier = A47**

**Syntax error**

**Identifier = C**

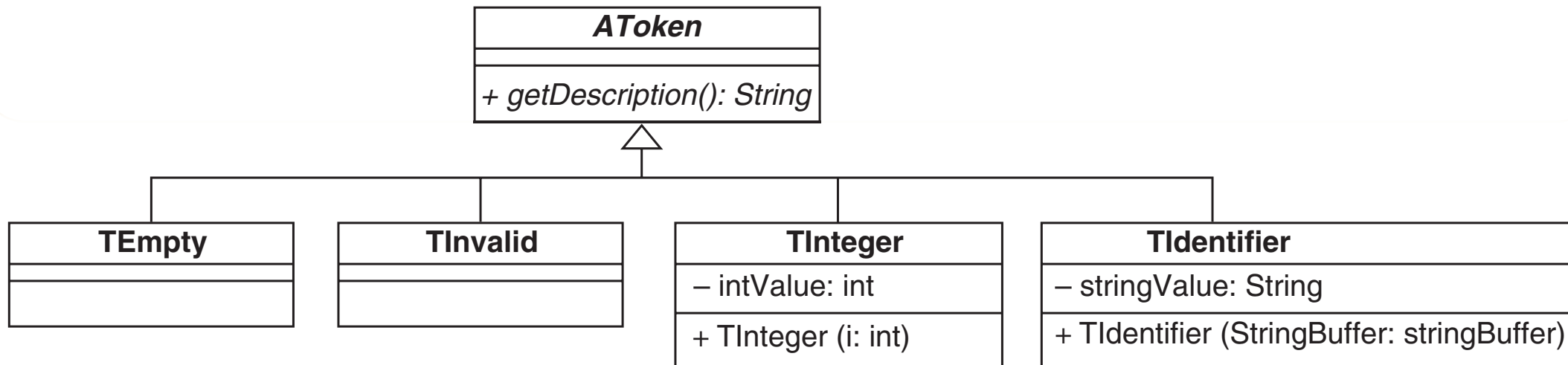
**Integer = 49**

**Empty token**

**Empty token**

**Identifier = ALongIdentifier**

**Empty token**



```
abstract public class AToken {
    public abstract String getDescription();
}

public class TEmpty extends AToken {

    @Override
    public String getDescription() {
        return "Empty token";
    }
}

public class TInvalid extends AToken {

    @Override
    public String getDescription() {
        return "Syntax error";
    }
}
```



```
public class TInteger extends AToken {
    private final int intValue;

    public TInteger(int i) {
        intValue = i;
    }

    @Override
    public String getDescription() {
        return String.format("Integer      = %d", intValue);
    }
}

public class TIdentifier extends AToken {
    private final String stringValue;

    public TIdentifier(StringBuffer stringBuffer) {
        stringValue = new String(stringBuffer);
    }

    @Override
    public String getDescription() {
        return String.format("Identifier = %s", stringValue);
    }
}
```

```
public class Util {  
  
    public static boolean isDigit(char ch) {  
        return ('0' <= ch) && (ch <= '9');  
    }  
  
    public static boolean isAlpha(char ch) {  
        return (('a' <= ch) && (ch <= 'z') || ('A' <= ch) && (ch <= 'Z'));  
    }  
}  
  
public enum LexState {  
    LS_START, LS_IDENT, LS_SIGN, LS_INTEGER, LS_STOP  
}
```

```
public class Tokenizer {  
  
    private final InBuffer b;  
  
    public Tokenizer(InBuffer inBuffer) {  
        b = inBuffer;  
    }  
  
    public AToken getToken() {  
        char nextChar;  
        StringBuffer localStringValue = new StringBuffer("");  
        int localIntValue = 0;  
        int sign = +1;  
        AToken aToken = new TEmpty();  
        LexState state = LexState.LS_START;  
    }  
}
```

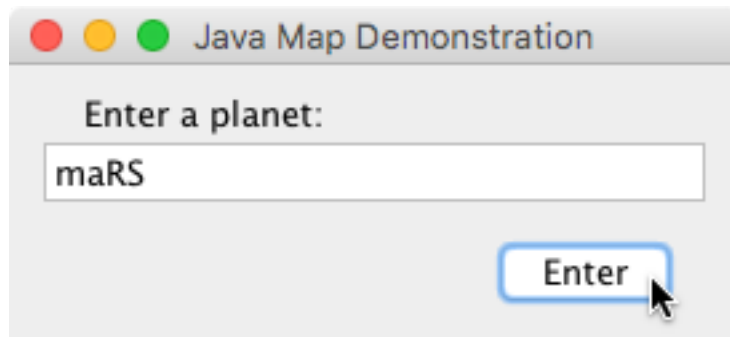
```
do {
    nextChar = b.advanceInput();
    switch (state) {
        case LS_START:
            if (Util.isAlpha(nextChar)) {
                localStringValue.append(nextChar);
                state = LexState.LS_IDENT;
            } else if (nextChar == '-') {
                sign = -1;
                state = LexState.LS_SIGN;
            } else if (nextChar == '+') {
                sign = +1;
                state = LexState.LS_SIGN;
            } else if (Util.isDigit(nextChar)) {
                localIntValue = nextChar - '0';
                state = LexState.LS_INTEGER;
            } else if (nextChar == '\n') {
                state = LexState.LS_STOP;
            } else if (nextChar != ' ') {
                aToken = new TInvalid();
            }
        }
    }
    break;
```

```
case LS_IDENT:
    if (Util.isAlpha(nextChar) || Util.isDigit(nextChar)) {
        localStringValue.append(nextChar);
    } else {
        b.backUpInput();
        aToken = new TIdentifier(localStringValue);
        state = LexState.LS_STOP;
    }
    break;
case LS_SIGN:
    if (Util.isDigit(nextChar)) {
        localIntValue = 10 * localIntValue + nextChar - '0';
        state = LexState.LS_INTEGER;
    } else {
        aToken = new TInvalid();
    }
    break;
```

```
        case LS_INTEGER:
            if (Util.isDigit(nextChar)) {
                localIntValue = 10 * localIntValue + nextChar - '0';
            } else {
                b.backUpInput();
                aToken = new TInteger(sign * localIntValue);
                state = LexState.LS_STOP;
            }
            break;
    }
} while ((state != LexState.LS_STOP) && !(aToken instanceof TInvalid));
return aToken;
}
}
```

```
public void actionPerformed(ActionEvent event) {
    InBuffer inBuffer = new InBuffer(textArea.getText());
    Tokenizer t = new Tokenizer(inBuffer);
    AToken aToken;
    inBuffer.getLine();
    while (inBuffer.inputRemains()) {
        do {
            aToken = t.getToken();
            System.out.println(aToken.getDescription());
        } while (!(aToken instanceof TEmpty)
            && !(aToken instanceof TInvalid));
        inBuffer.getLine();
    }
}
```

## Java map demo



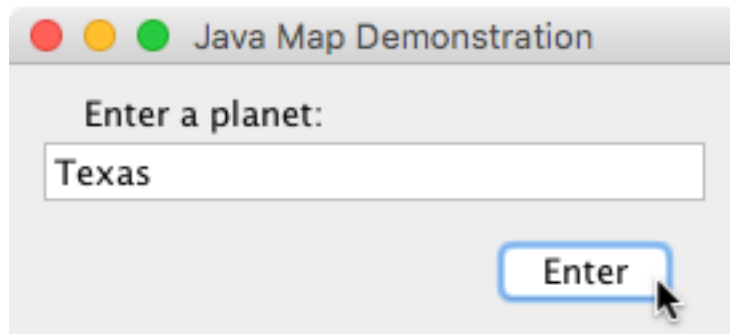
A screenshot of a Java application window titled "Java Map Demonstration". It features a label "Enter a planet:" above a text input field containing "maRS". Below the input field is a button labeled "Enter" with a mouse cursor hovering over it.

### Console output

**Planet Mars is red.**

**Enumerated output: P\_MARS**

**Ordinal output: 3**



A screenshot of a Java application window titled "Java Map Demonstration". It features a label "Enter a planet:" above a text input field containing "Texas". Below the input field is a button labeled "Enter" with a mouse cursor hovering over it.

### Console output

**Texas is not a planet.**



```
public enum Planet {
    P_MERCURY, P_VENUS, P_EARTH, P_MARS, P_JUPITER, P_SATURN,
    P_URANUS, P_NEPTUNE, P_PLUTO
}

public class Maps {

    public static final Map<String, Planet> planetTable;
    public static final Map<Planet, String> planetStringTable;

    static {
        planetTable = new HashMap<>();
        planetTable.put("mercury", Planet.P_MERCURY);
        planetTable.put("venus", Planet.P_VENUS);
        planetTable.put("earth", Planet.P_EARTH);
        planetTable.put("mars", Planet.P_MARS);
        planetTable.put("jupiter", Planet.P_JUPITER);
        planetTable.put("saturn", Planet.P_SATURN);
        planetTable.put("uranus", Planet.P_URANUS);
        planetTable.put("neptune", Planet.P_NEPTUNE);
        planetTable.put("pluto", Planet.P_PLUTO);
    }
}
```

```
planetStringTable = new EnumMap<>(Planet.class);
planetStringTable.put(Planet.P_MERCURY, "Mercury");
planetStringTable.put(Planet.P_VENUS, "Venus");
planetStringTable.put(Planet.P_EARTH, "Earth");
planetStringTable.put(Planet.P_MARS, "Mars");
planetStringTable.put(Planet.P_JUPITER, "Jupiter");
planetStringTable.put(Planet.P_SATURN, "Saturn");
planetStringTable.put(Planet.P_URANUS, "Uranus");
planetStringTable.put(Planet.P_NEPTUNE, "Neptune");
planetStringTable.put(Planet.P_PLUTO, "Pluto");
```

```
}
```

```
}
```

```
public void actionPerformed(ActionEvent event) {
    String line = textField.getText();
    if (Maps.planetTable.containsKey(line.toLowerCase())) {
        Planet planet = Maps.planetTable.get(line.toLowerCase());
        String planetString = Maps.planetStringTable.get(planet);
        switch (planet) {
            case P_MERCURY:
            case P_VENUS:
                System.out.printf("%s is close to the sun.\n", planetString);
                break;
            case P_EARTH:
                System.out.printf("The %s is indeed a planet.\n", planetString);
                break;
            case P_MARS:
                System.out.printf("Planet %s is red.\n", planetString);
                break;
            case P_JUPITER:
            case P_SATURN:
                System.out.printf("%s is a big planet.\n", planetString);
                break;
            case P_URANUS:
            case P_NEPTUNE:
            case P_PLUTO:
                System.out.printf("%s is far from the sun.\n", planetString);
        }
    }
}
```

```
        System.out.printf("Enumerated output: %s\n", planet);
        System.out.printf("Ordinal output: %d\n", planet.ordinal());
    } else {
        System.out.println(line + " is not a planet.");
    }
}
}
```

## A language translator

## Input

```
set (Time, 15)
set (  Accel, 3)
set (TSquared  , Time)
    MUL ( TSquared, Time)
set ( Position, TSquared)
mul (Position, Accel)
dIV(Position,2)
stop
end
```

## Output

Object code:

```
Time <- 15
Accel <- 3
TSquared <- Time
TSquared <- TSquared * Time
Position <- TSquared
Position <- Position * Accel
Position <- Position / 2
stop
```

Program listing:

```
set (Time, 15)
set (Accel, 3)
set (TSquared, Time)
mul (TSquared, Time)
set (Position, TSquared)
mul (Position, Accel)
div (Position, 2)
stop
end
```

## Input

```
set (Alpha,, 123)
set (Alpha)
sit (Alpha, 123)
set, (Alpha)
mul (Alpha, Beta
set (123, Alpha)
neg (Alpha, Beta)
set (Alpha, 123) x
```

## Output

9 errors were detected.

Program listing:

```
ERROR: Second argument not an identifier or integer.
ERROR: Comma expected after first argument.
ERROR: Line must begin with function identifier.
ERROR: Left parenthesis expected after function.
ERROR: Right parenthesis expected after argument.
ERROR: First argument not an identifier.
ERROR: Right parenthesis expected after argument.
ERROR: Illegal trailing character.
ERROR: Missing "end" sentinel.
```

```
public enum Mnemon {
    M_ADD, M_SUB, M_MUL, M_DIV, M_NEG, M_ABS, M_SET, M_STOP, M_END
}

public final class Maps {

    public static final Map<String, Mnemon> unaryMnemonicTable;
    public static final Map<String, Mnemon> nonUnaryMnemonicTable;
    public static final Map<Mnemon, String> mnemonicStringTable;

    static {
        unaryMnemonicTable = new HashMap<>();
        unaryMnemonicTable.put("stop", Mnemon.M_STOP);
        unaryMnemonicTable.put("end", Mnemon.M_END);

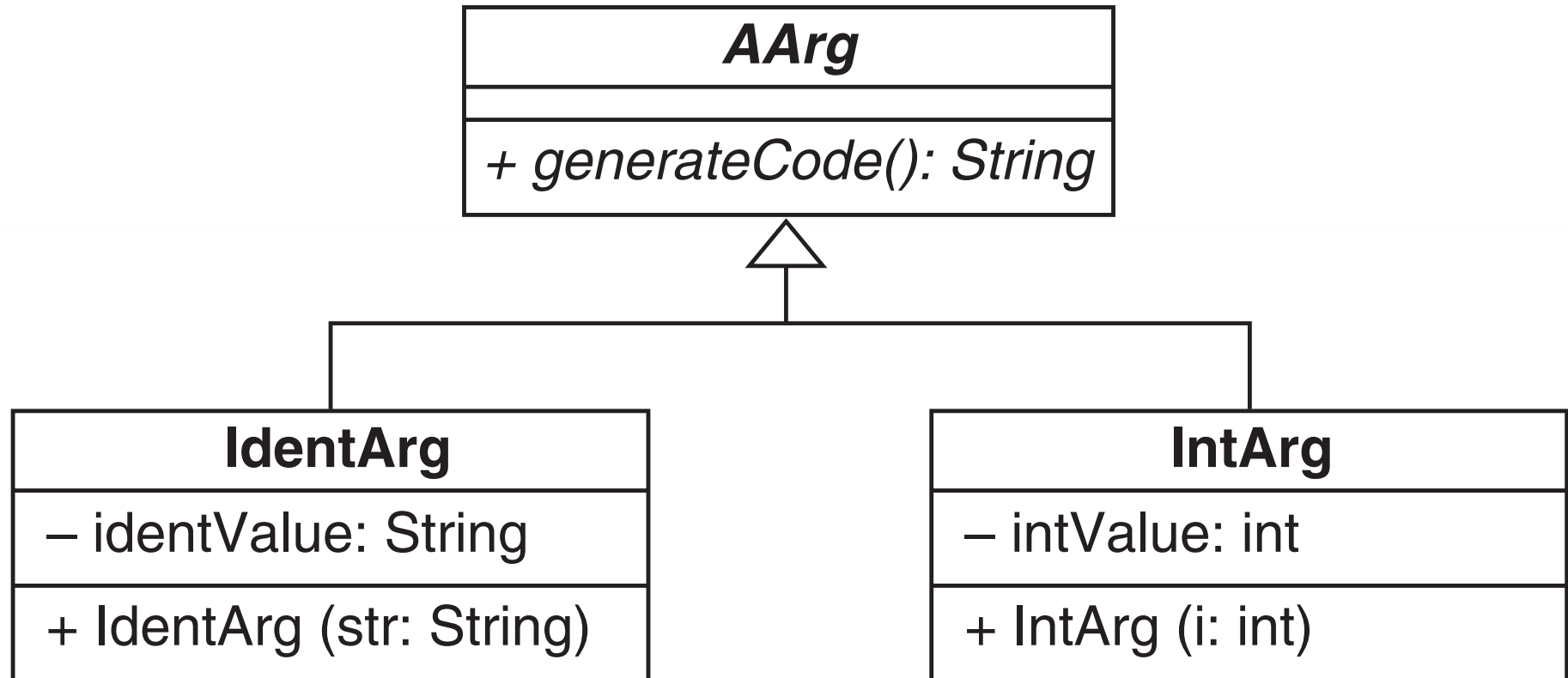
        nonUnaryMnemonicTable = new HashMap<>();
        nonUnaryMnemonicTable.put("neg", Mnemon.M_NEG);
        nonUnaryMnemonicTable.put("abs", Mnemon.M_ABS);
        nonUnaryMnemonicTable.put("add", Mnemon.M_ADD);
        nonUnaryMnemonicTable.put("sub", Mnemon.M_SUB);
        nonUnaryMnemonicTable.put("mul", Mnemon.M_MUL);
        nonUnaryMnemonicTable.put("div", Mnemon.M_DIV);
        nonUnaryMnemonicTable.put("set", Mnemon.M_SET);
    }
}
```



```
mnemonStringTable = new EnumMap<>(Mnemon.class);  
mnemonStringTable.put(Mnemon.M_NEG, "neg");  
mnemonStringTable.put(Mnemon.M_ABS, "abs");  
mnemonStringTable.put(Mnemon.M_ADD, "add");  
mnemonStringTable.put(Mnemon.M_SUB, "sub");  
mnemonStringTable.put(Mnemon.M_MUL, "mul");  
mnemonStringTable.put(Mnemon.M_DIV, "div");  
mnemonStringTable.put(Mnemon.M_SET, "set");  
mnemonStringTable.put(Mnemon.M_STOP, "stop");  
mnemonStringTable.put(Mnemon.M_END, "end");
```

```
}
```

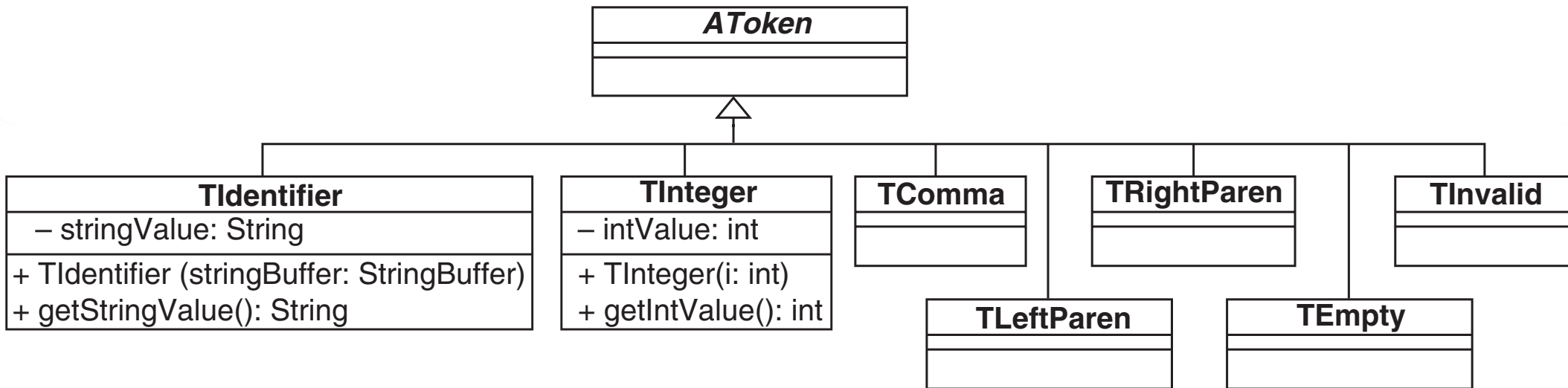
```
}
```



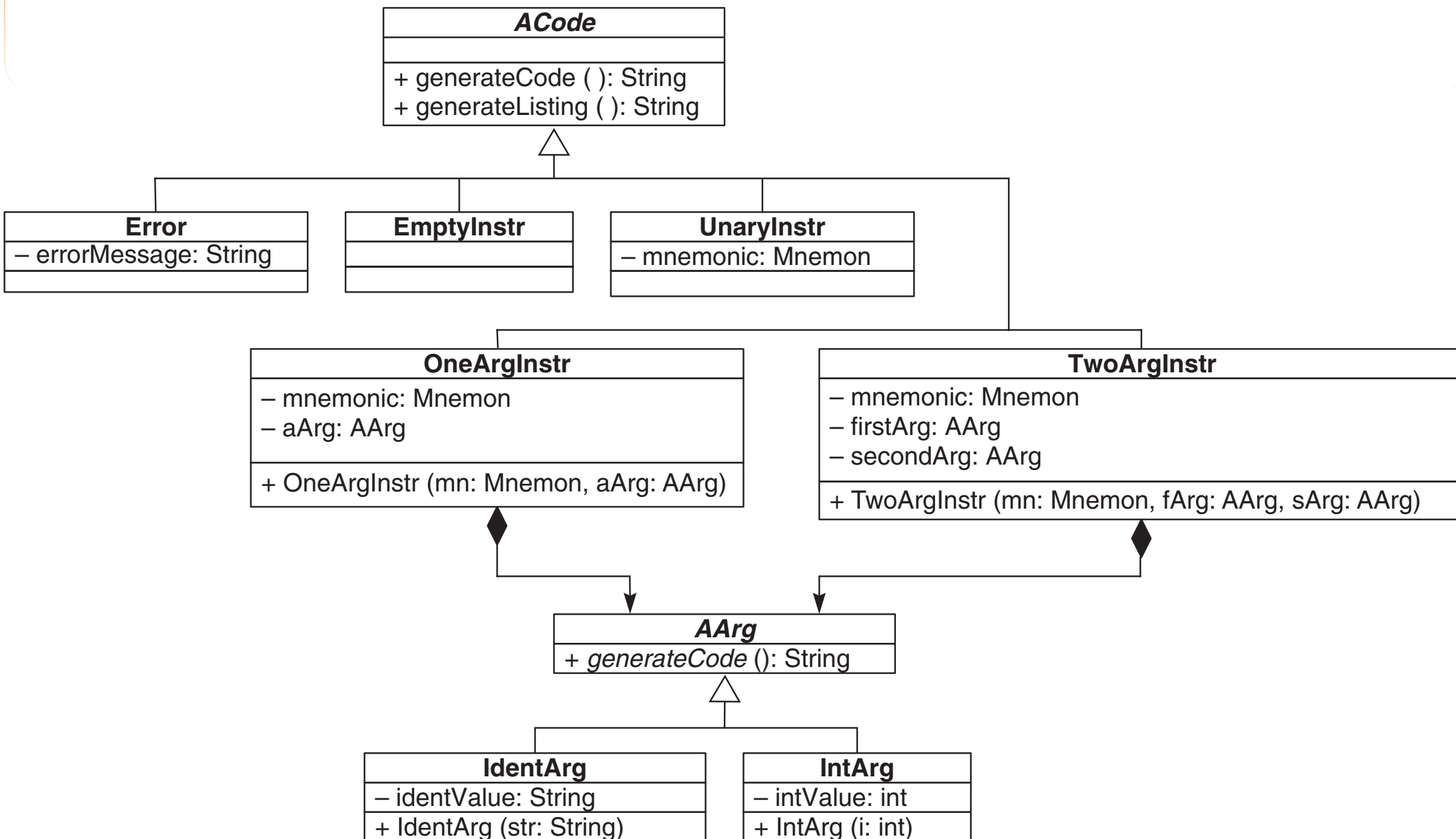
```
abstract public class AArg {
    abstract public String generateCode();
}

public class IdentArg extends AArg {
    private final String identValue;
    public IdentArg(String str) {
        identValue = str;
    }
    @Override
    public String generateCode() {
        return identValue;
    }
}

public class IntArg extends AArg {
    private final int intValue;
    public IntArg(int i) {
        intValue = i;
    }
    @Override
    public String generateCode() {
        return String.format("%d", intValue);
    }
}
```



```
abstract public class AToken {  
}  
  
public class TIdentifier extends AToken {  
    private final String stringValue;  
    public TIdentifier(StringBuffer stringBuffer) {  
        stringValue = new String(stringBuffer);  
    }  
    public String getStringValue() {  
        return stringValue;  
    }  
}  
  
public class TInteger extends AToken {  
    private final int intValue;  
    public TInteger(int i) {  
        intValue = i;  
    }  
    public int getIntValue() {  
        return intValue;  
    }  
}  
  
public class TComma extends AToken {  
}
```



```
abstract public class ACode {
    abstract public String generateCode();
    abstract public String generateListing();
}

public class Error extends ACode {
    private final String errorMessage;
    public Error(String errMessage) {
        errorMessage = errMessage;
    }

    @Override
    public String generateListing() {
        return "ERROR: " + errorMessage + "\n";
    }

    @Override
    public String generateCode() {
        return "";
    }
}
```

```
public class EmptyInstr extends ACode {  
    // For an empty source line.  
  
    @Override  
    public String generateListing() {  
        return "\n";  
    }  
  
    @Override  
    public String generateCode() {  
        return "";  
    }  
}
```



```
public class UnaryInstr extends ACode {
    private final Mnemon mnemonic;
    public UnaryInstr(Mnemon mn) {
        mnemonic = mn;
    }

    @Override
    public String generateListing() {
        return Maps.mnemonStringTable.get(mnemonic) + "\n";
    }

    @Override
    public String generateCode() {
        switch (mnemonic) {
            case M_STOP:
                return "stop\n";
            case M_END:
                return "";
            default:
                return ""; // Should not occur.
        }
    }
}
```

```
public class OneArgInstr extends ACode {
    private final Mnemon mnemonic;
    private final AArg aArg;
    public OneArgInstr(Mnemon mn, AArg aArg) {
        mnemonic = mn;
        this.aArg = aArg;
    }
    @Override
    public String generateListing() {
        return String.format("%s (%s)\n",
                               Maps.mnemonStringTable.get(mnemonic), aArg.generateCode());
    }
    @Override
    public String generateCode() {
        switch (mnemonic) {
            case M_ABS:
                return String.format("%s <- |%s|\n",
                                       aArg.generateCode(), aArg.generateCode());
            case M_NEG:
                return String.format("%s <- -%s\n",
                                       aArg.generateCode(), aArg.generateCode());
            default:
                return ""; // Should not occur.
        }
    }
}
```

```
public class TwoArgInstr extends ACode {
    private final Mnemon mnemonic;
    private final AArg firstArg;
    private final AArg secondArg;
    public TwoArgInstr(Mnemon mn, AArg fArg, AArg sArg) {
        mnemonic = mn;
        firstArg = fArg;
        secondArg = sArg;
    }

    @Override
    public String generateListing() {
        return String.format("%s (%s, %s)\n",
            Maps.mnemonStringTable.get(mnemonic),
            firstArg.generateCode(),
            secondArg.generateCode());
    }
}
```

```
@Override
public String generateCode() {
    switch (mnemonic) {
        case M_SET:
            return String.format("%s <- %s\n",
                                firstArg.generateCode(),
                                secondArg.generateCode());

        case M_ADD:
            return String.format("%s <- %s + %s\n",
                                firstArg.generateCode(),
                                firstArg.generateCode(),
                                secondArg.generateCode());

        case M_SUB:
            return String.format("%s <- %s - %s\n",
                                firstArg.generateCode(),
                                firstArg.generateCode(),
                                secondArg.generateCode());

        case M_MUL:
            return String.format("%s <- %s * %s\n",
                                firstArg.generateCode(),
                                firstArg.generateCode(),
                                secondArg.generateCode());
    }
}
```

```
case M_DIV:
    return String.format("%s <- %s / %s\n",
        firstArg.generateCode(),
        firstArg.generateCode(),
        secondArg.generateCode());
default:
    return ""; // Should not occur.
}
}
}
```

```
public enum LexState {
    LS_START, LS_IDENT, LS_SIGN, LS_INTEGER, LS_STOP
}

public class Tokenizer {

    private final InBuffer b;

    public Tokenizer(InBuffer inBuffer) {
        b = inBuffer;
    }

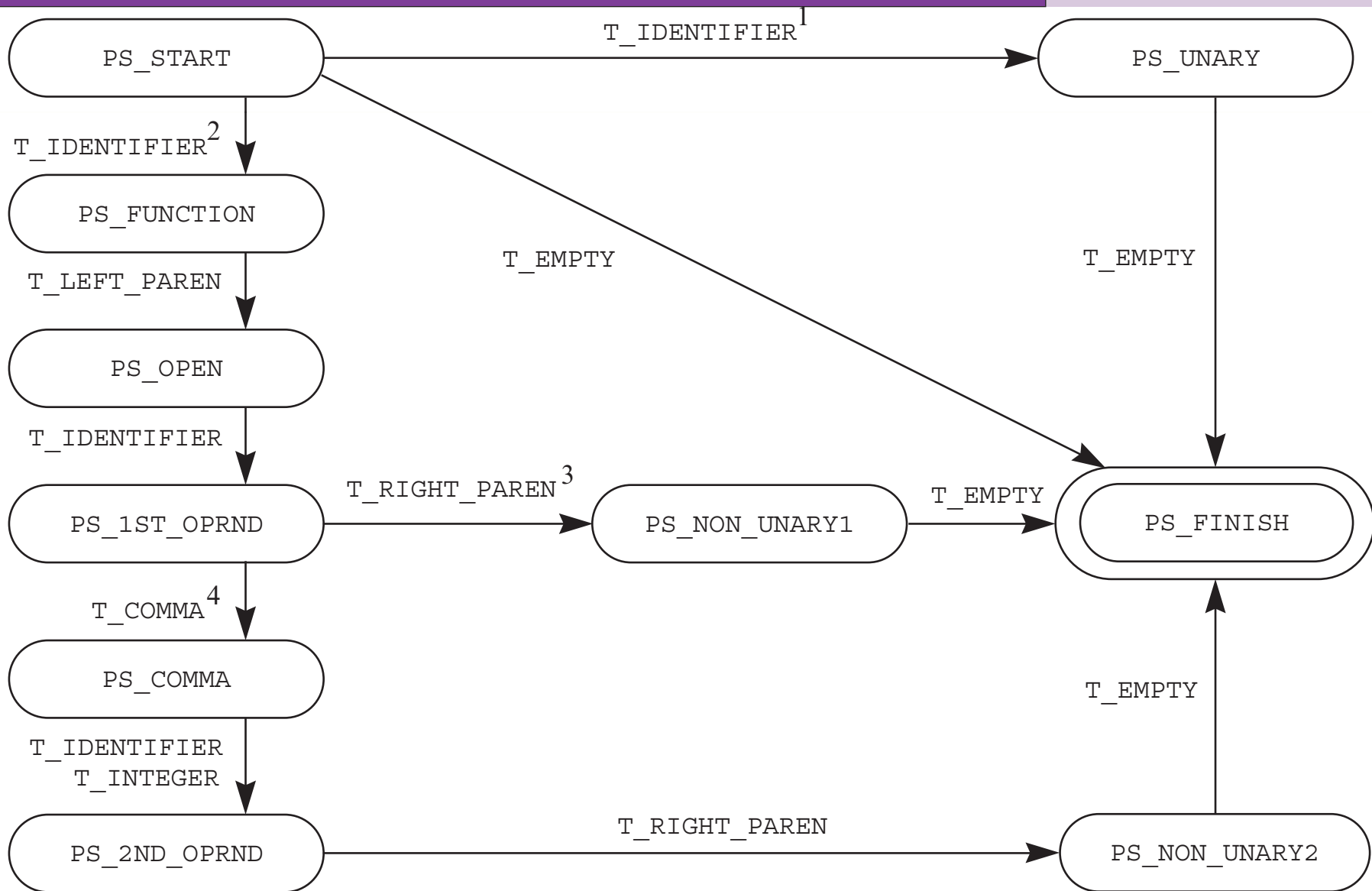
    public AToken getToken() {
        char nextChar;
        StringBuffer localStringValue = new StringBuffer("");
        int localIntValue = 0;
        int sign = +1;
        AToken aToken = new TEmpty();
        LexState state = LexState.LS_START;
```

```
do {
    nextChar = b.advanceInput();
    switch (state) {
        case LS_START:
            if (Util.isAlpha(nextChar)) {
                localStringValue.append(nextChar);
                state = LexState.LS_IDENT;
            } else if (nextChar == '-') {
                sign = -1;
                state = LexState.LS_SIGN;
            } else if (nextChar == '+') {
                sign = +1;
                state = LexState.LS_SIGN;
            } else if (Util.isDigit(nextChar)) {
                localIntValue = nextChar - '0';
                state = LexState.LS_INTEGER;
            } else if (nextChar == ',') {
                aToken = new TComma();
                state = LexState.LS_STOP;
            } else if (nextChar == '(') {
                aToken = new TLeftParen();
                state = LexState.LS_STOP;
            } else if (nextChar == ')') {
                aToken = new TRightParen();
                state = LexState.LS_STOP;
            }
    }
}
```

```
    } else if (nextChar == '\n') {
        state = LexState.LS_STOP;
    } else if (nextChar != ' ') {
        aToken = new TInvalid();
    }
    break;
case LS_IDENT:
    if (Util.isAlpha(nextChar) || Util.isDigit(nextChar)) {
        localStringValue.append(nextChar);
    } else {
        b.backUpInput();
        aToken = new TIdentifier(localStringValue);
        state = LexState.LS_STOP;
    }
    break;
case LS_SIGN:
    if (Util.isDigit(nextChar)) {
        localStringValue.append(nextChar);
        state = LexState.LS_INTEGER;
    } else {
        aToken = new TInvalid();
    }
    break;
```



```
        case LS_INTEGER:
            if (Util.isDigit(nextChar)) {
                localIntValue = 10 * localIntValue + nextChar - '0';
            } else {
                b.backUpInput();
                aToken = new TInteger(localIntValue);
                state = LexState.LS_STOP;
            }
            break;
    }
} while ((state != LexState.LS_STOP) && !(aToken instanceof TInvalid));
return aToken;
}
}
```



Note 1: Only the identifiers stop and end.

Note 2: Only the identifiers set, add, sub, mul, div, neg, and abs.

Note 3: Only for mnemonics M\_NEG and M\_ABS.

Note 4: Only for mnemonics M\_SET, M\_ADD, M\_SUB, and M\_MUL, M\_DIV.

```
public enum ParseState {
    PS_START, PS_UNARY, PS_FUNCTION, PS_OPEN, PS_1ST_OPRND, PS_NONUNARY1,
    PS_COMMA, PS_2ND_OPRND, PS_NON_UNARY2, PS_FINISH
}

public class Translator {
    private final InBuffer b;
    private Tokenizer t;
    private ACode aCode;

    public Translator(InBuffer inBuffer) {
        b = inBuffer;
    }

    // Sets aCode and returns boolean true if end statement is processed.
    private boolean parseLine() {
        boolean terminate = false;
        AArg localFirstArg = new IntArg(0);
        AArg localSecondArg;
        // Compiler requires following useless initialization.
        Mnemon localMnemon = Mnemon.M_END;
        AToken aToken;
        aCode = new EmptyInstr();
        ParseState state = ParseState.PS_START;
    }
}
```

```
do {
    aToken = t.getToken();
    switch (state) {
        case PS_START:
            if (aToken instanceof TIdentifier) {
                TIdentifier localTIdentifier = (TIdentifier) aToken;
                String tempStr = localTIdentifier.getStringValue();
                if (Maps.unaryMnemonTable.containsKey(
                    tempStr.toLowerCase())) {
                    localMnemon = Maps.unaryMnemonTable.get(
                        tempStr.toLowerCase());
                    aCode = new UnaryInstr(localMnemon);
                    terminate = localMnemon == Mnemon.M_END;
                    state = ParseState.PS_UNARY;
                } else if (Maps.nonUnaryMnemonTable.containsKey(
                    tempStr.toLowerCase())) {
                    localMnemon = Maps.nonUnaryMnemonTable.get(
                        tempStr.toLowerCase());
                    state = ParseState.PS_FUNCTION;
                } else {
                    aCode = new Error(
                        "Line must begin with function identifier.");
                }
            }
        }
    }
```

```
    } else if (aToken instanceof TEmpty) {  
        aCode = new EmptyInstr();  
        state = ParseState.PS_FINISH;  
    } else {  
        aCode = new Error(  
            "Line must begin with function identifier.");  
    }  
    break;
```

...

```
case PS_FUNCTION:
    if (aToken instanceof TLeftParen) {
        state = ParseState.PS_OPEN;
    } else {
        aCode = new Error(
            "Left parenthesis expected after function.");
    }
    break;
case PS_OPEN:
    if (aToken instanceof TIdentifier) {
        TIdentifier localTIdentifier = (TIdentifier) aToken;
        localFirstArg = new IdentArg(
            localTIdentifier.getStringValue());
        state = ParseState.PS_1ST_OPRND;
    } else {
        aCode = new Error("First argument not an identifier.");
    }
    break;
```

```
case PS_1ST_OPRND:
    if (localMnemon == Mnemon.M_NEG
        || localMnemon == Mnemon.M_ABS) {
        if (aToken instanceof TRightParen) {
            aCode = new OneArgInstr(localMnemon, localFirstArg);
            state = ParseState.PS_NONUNARY1;
        } else {
            aCode = new Error(
                "Right parenthesis expected after argument.");
        }
    } else if (aToken instanceof TComma) {
        state = ParseState.PS_COMMA;
    } else {
        aCode = new Error(
            "Comma expected after first argument.");
    }
    break;
```

```
case PS_COMMA:
    if (aToken instanceof TIdentifier) {
        TIdentifier localTIdentifier = (TIdentifier) aToken;
        localSecondArg = new IdentArg(
            localTIdentifier.getStringValue());
        aCode = new TwoArgInstr(
            localMnemon, localFirstArg, localSecondArg);
        state = ParseState.PS_2ND_OPRND;
    } else if (aToken instanceof TInteger) {
        TInteger localTInteger = (TInteger) aToken;
        localSecondArg = new IntArg(localTInteger.getIntValue());
        aCode = new TwoArgInstr(
            localMnemon, localFirstArg, localSecondArg);
        state = ParseState.PS_2ND_OPRND;
    } else {
        aCode = new Error(
            "Second argument not an identifier or integer.");
    }
    break;
```



```
case PS_2ND_OPRND:
    if (aToken instanceof TRightParen) {
        state = ParseState.PS_NON_UNARY2;
    } else {
        aCode = new Error(
            "Right parenthesis expected after argument.");
    }
    break;
```

```
    case PS_NON_UNARY2:
        if (aToken instanceof TEmpty) {
            state = ParseState.PS_FINISH;
        } else {
            aCode = new Error("Illegal trailing character.");
        }
        break;
    }
} while (state != ParseState.PS_FINISH && !(aCode instanceof Error));
return terminate;
}
```

```
public void translate() {
    ArrayList<ACode> codeTable = new ArrayList<>();
    int numErrors = 0;
    t = new Tokenizer(b);
    boolean terminateWithEnd = false;
    b.getLine();
    while (b.inputRemains() && !terminateWithEnd) {
        terminateWithEnd = parseLine(); // Sets aCode and returns boolean.
        codeTable.add(aCode);
        if (aCode instanceof Error) {
            numErrors++;
        }
        b.getLine();
    }
    if (!terminateWithEnd) {
        aCode = new Error("Missing \"end\" sentinel.");
        codeTable.add(aCode);
        numErrors++;
    }
}
```

```
if (numErrors == 0) {
    System.out.printf("Object code:\n");
    for (int i = 0; i < codeTable.size(); i++) {
        System.out.printf("%s", codeTable.get(i).generateCode());
    }
}
if (numErrors == 1) {
    System.out.printf("One error was detected.\n");
} else if (numErrors > 1) {
    System.out.printf("%d errors were detected.\n", numErrors);
}
System.out.printf("\nProgram listing:\n");
for (int i = 0; i < codeTable.size(); i++) {
    System.out.printf("%s", codeTable.get(i).generateListing());
}
}
```

```
public void actionPerformed(ActionEvent event) {  
    InBuffer inBuffer = new InBuffer(textArea.getText());  
    Translator tr = new Translator(inBuffer);  
    tr.translate();  
}
```

## Translation phases

- Lexical analyzer – `getToken()`
- Parser – `parseLine()`
- Code generator – `generateCode()`

$$N = \{ A, B \}$$

$$T = \{ 0, 1 \}$$

$P$  = the productions

1.  $A \rightarrow 0 B$

2.  $B \rightarrow 1 0 B$

3.  $B \rightarrow \epsilon$

$$S = A$$

$$N = \{ C \}$$

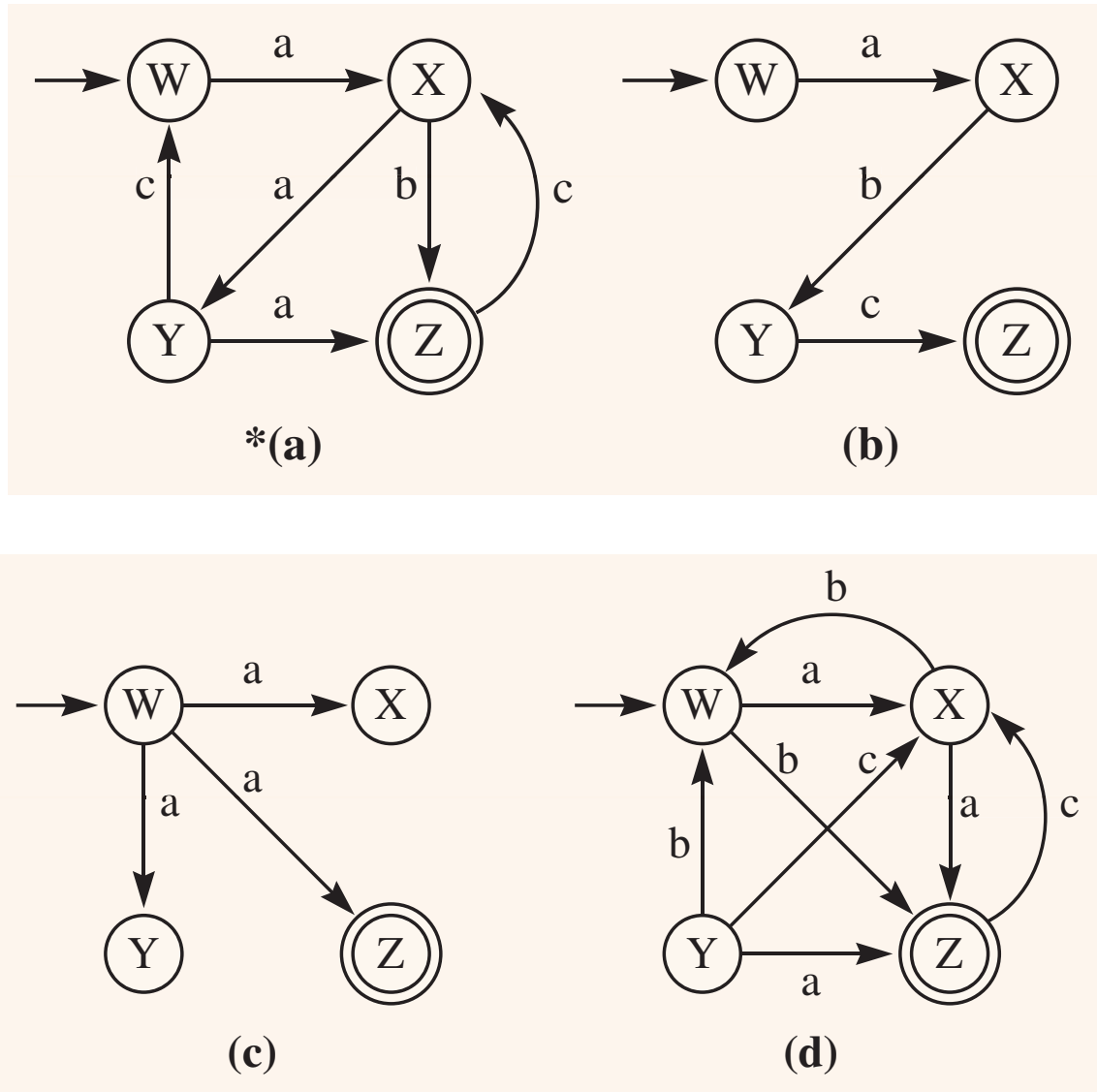
$$T = \{ 0, 1 \}$$

$P$  = the productions

1.  $C \rightarrow C 1 0$

2.  $C \rightarrow 0$

$$S = C$$





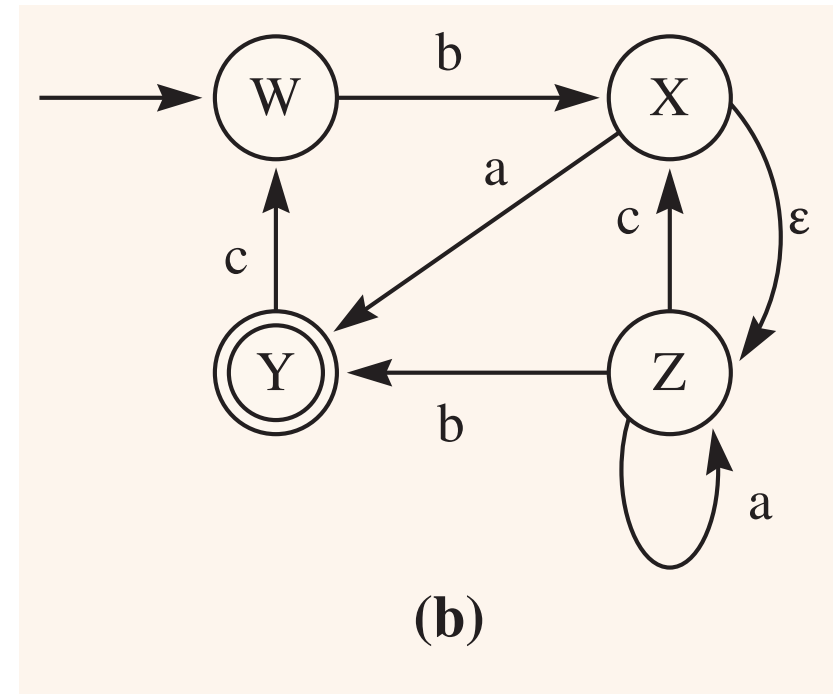
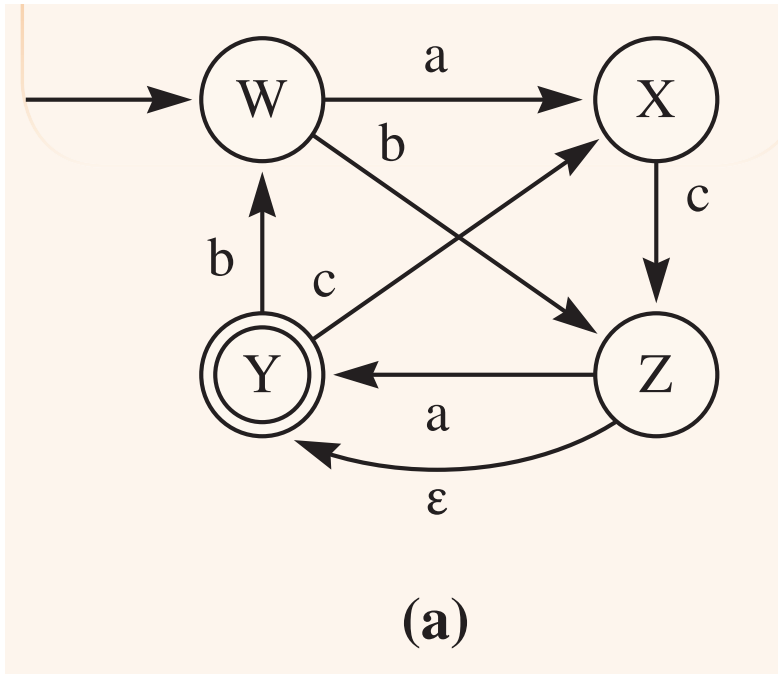


Figure 7.53

